

# Inferring Astrophysical Channels with Neutron Star-Black Hole Mergers

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 **N3AS** Network for Neutrinos,  
Nuclear Astrophysics,  
and Symmetries  
PHYSICS FRONTIER CENTER



# Research Interests

Using simulated and observed gravitational-wave events for

Forecasting the multi-messenger capabilities of next-generation observatories

Inference of astrophysical formation scenarios

Cosmological inference with binary mergers

Inferring neutron star properties

Testing general relativity

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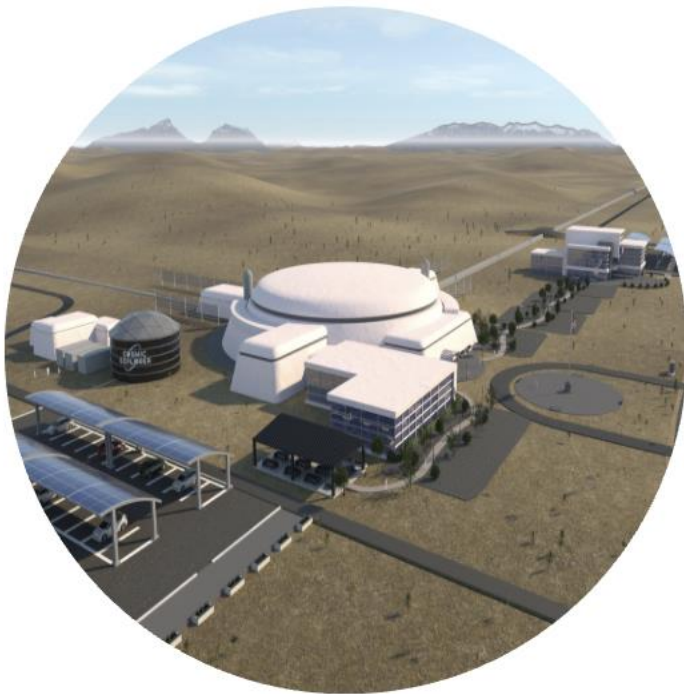
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**Neutron star-black hole mergers in next generation gravitational-wave observatories**

*Gupta et al., Phys.Rev.D 107 (2023) 12, 124007.*

**Characterizing Gravitational Wave Detector Networks: From A# to Cosmic Explorer**

*Gupta et al., CQG 41 (2024).*

**The Critical Role of LIGO-India in the Era of Next-Generation Observatories**

*Pandey, Gupta et al., Accepted in ApJL, 2025.*



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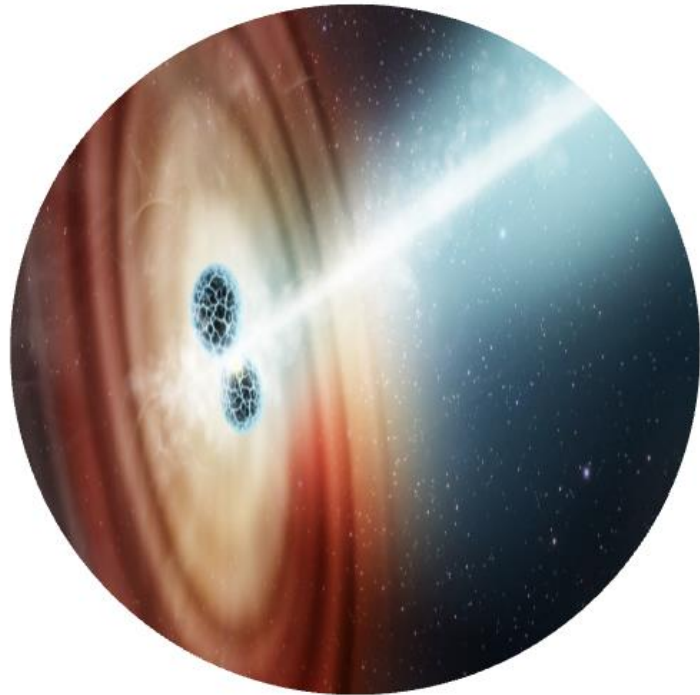
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**Measuring the neutron star spin with neutron star-black hole mergers.**

*Gupta. Astrophys J. 970 (2024)*

**On the Origins, Remnant, and Multimessenger Prospects of the Compact Binary Merger GW230529**

*Chandra, Gupta, et al., Astrophys J. (2025)*

**Foreground signals minimally affect inference of high-mass binary black holes in next generation gravitational-wave detectors**

*Gupta et al., Submitted to PRD, 2025.*

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## **Using Gray Sirens to Resolve the Hubble-Lemaître Tension**

*Gupta. Mon.Not.Roy.Astron.Soc. 524 (2023) 3, 3537-3558*

## **Cosmography with XG gravitational wave detectors**

*Gupta, Chen and Ezquiaga. Class. Quantum Grav. 41, 125004 (2024).*

## **Effect of precession on golden dark siren measurements**

*In preparation. (2025)*

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Using simulated and observed gravitational-wave events for

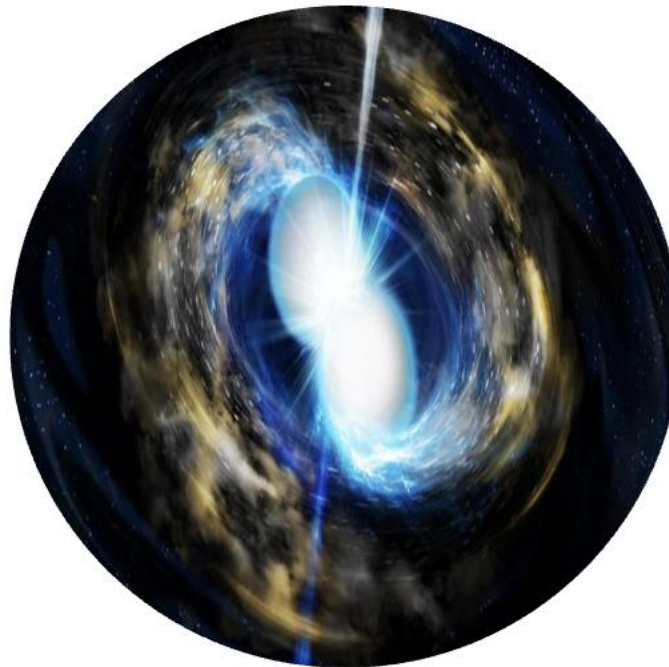
Forecasting the multi-messenger capabilities of next-generation observatories

Inference of astrophysical formation scenarios

Cosmological inference with binary mergers

Inferring neutron star properties

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**Detectability of QCD phase transitions in binary neutron star mergers**

*Prakash, Gupta, et al., Phys. Rev. D 109, 103008 (2023)*

**Cosmic Calipers: Precise and Accurate Neutron Star Radius Measurements with Next-Generation Gravitational Wave Detectors**

*Khadkikar, Gupta et al., Submitted to PRD, 2025.*

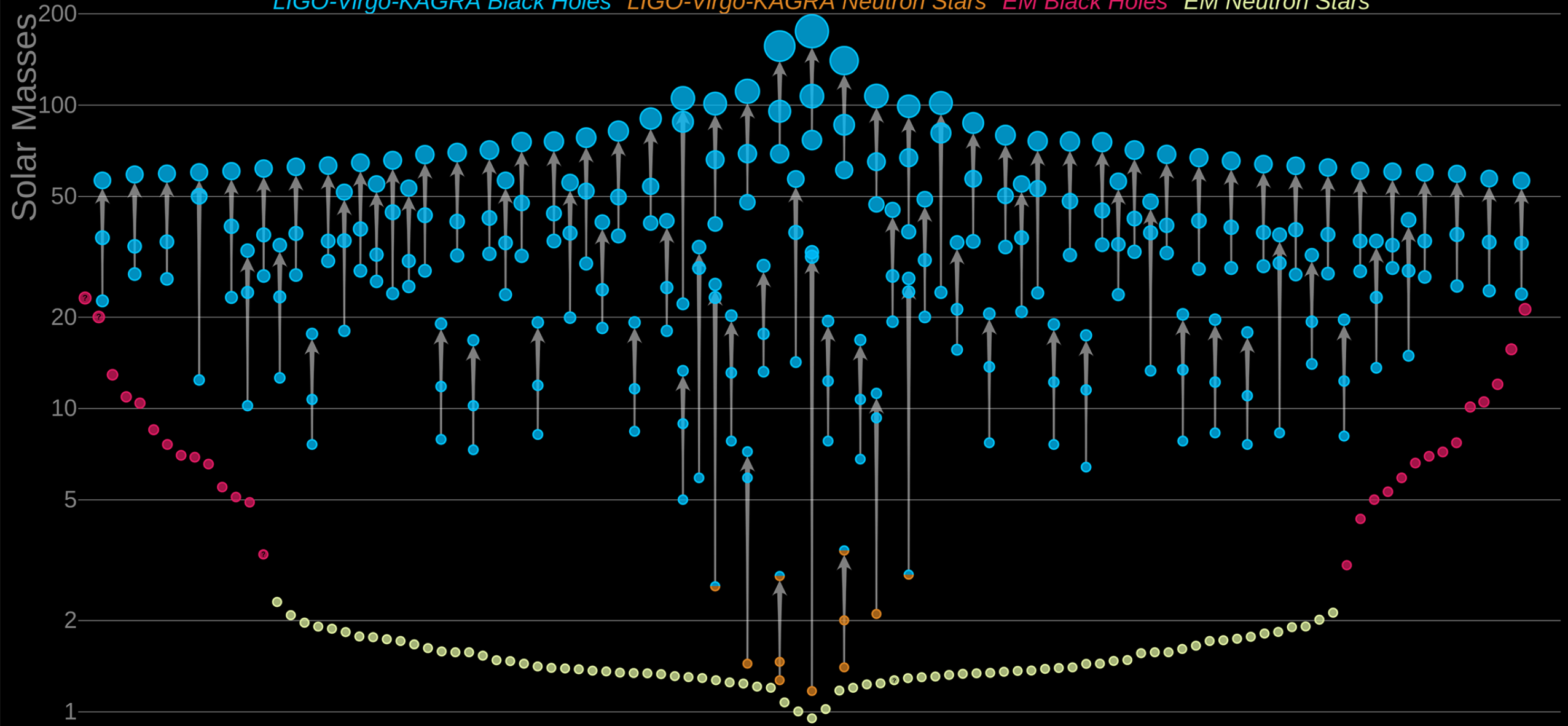
**Optimizing Bayesian model selection for equation of state of cold neutron stars**  
*Kashyap, Gupta et al., Submitted to PRD, 2025.*

**Testing general relativity with sub-dominant mode amplitudes**

*Gupta, et al., In preparation. (2025)*

# Masses in the Stellar Graveyard

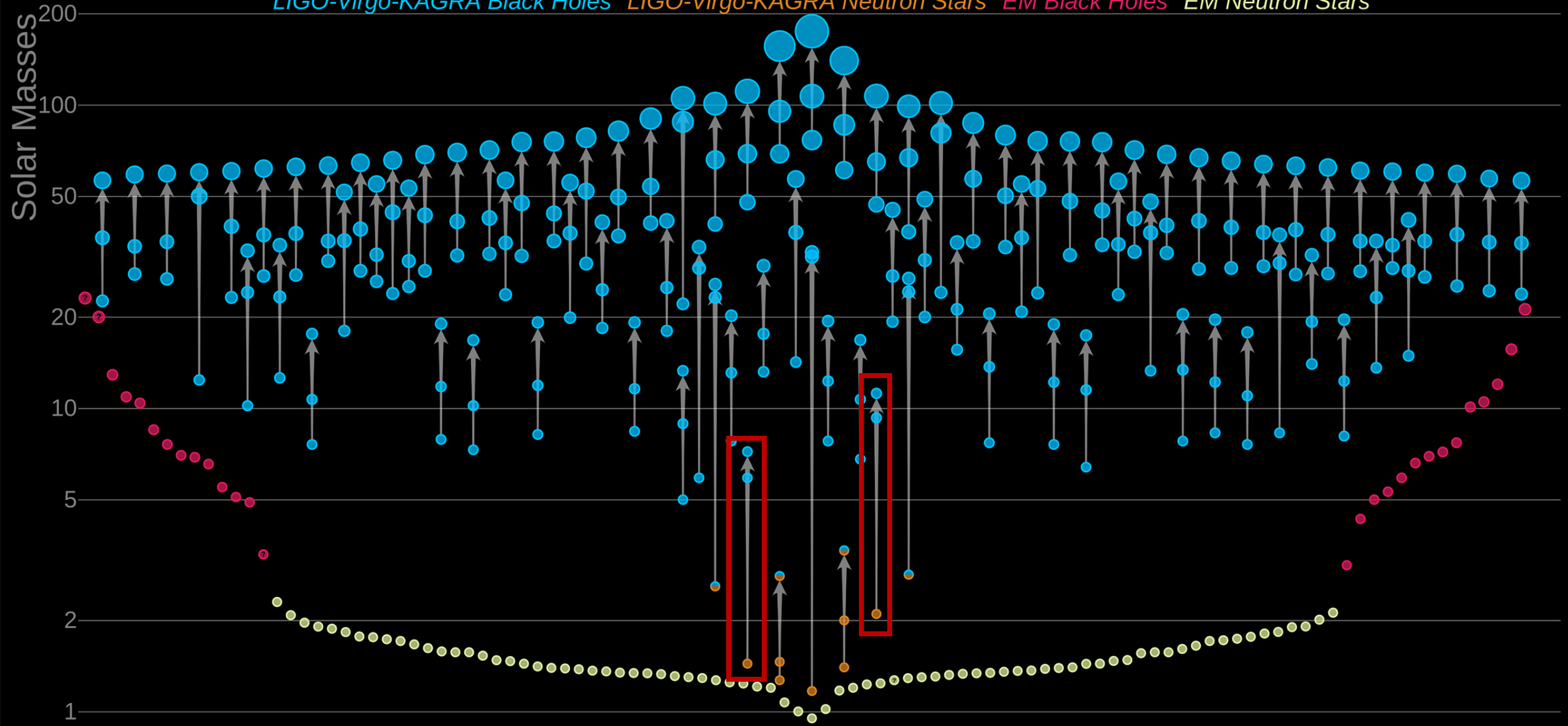
*LIGO-Virgo-KAGRA Black Holes*   *LIGO-Virgo-KAGRA Neutron Stars*   *EM Black Holes*   *EM Neutron Stars*





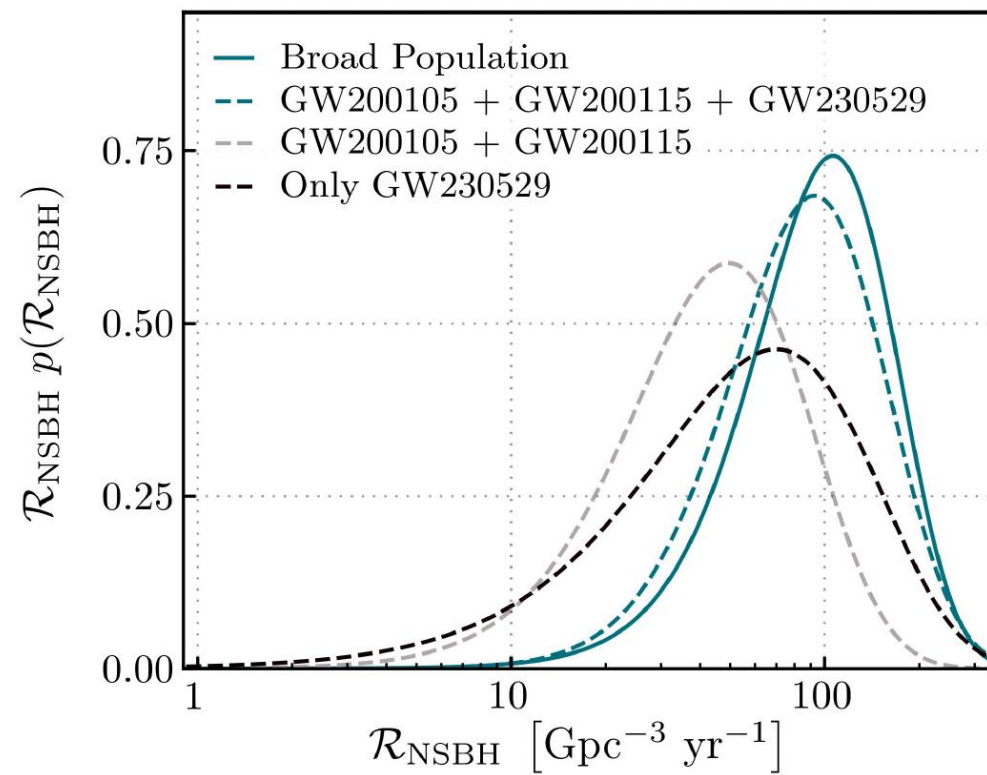
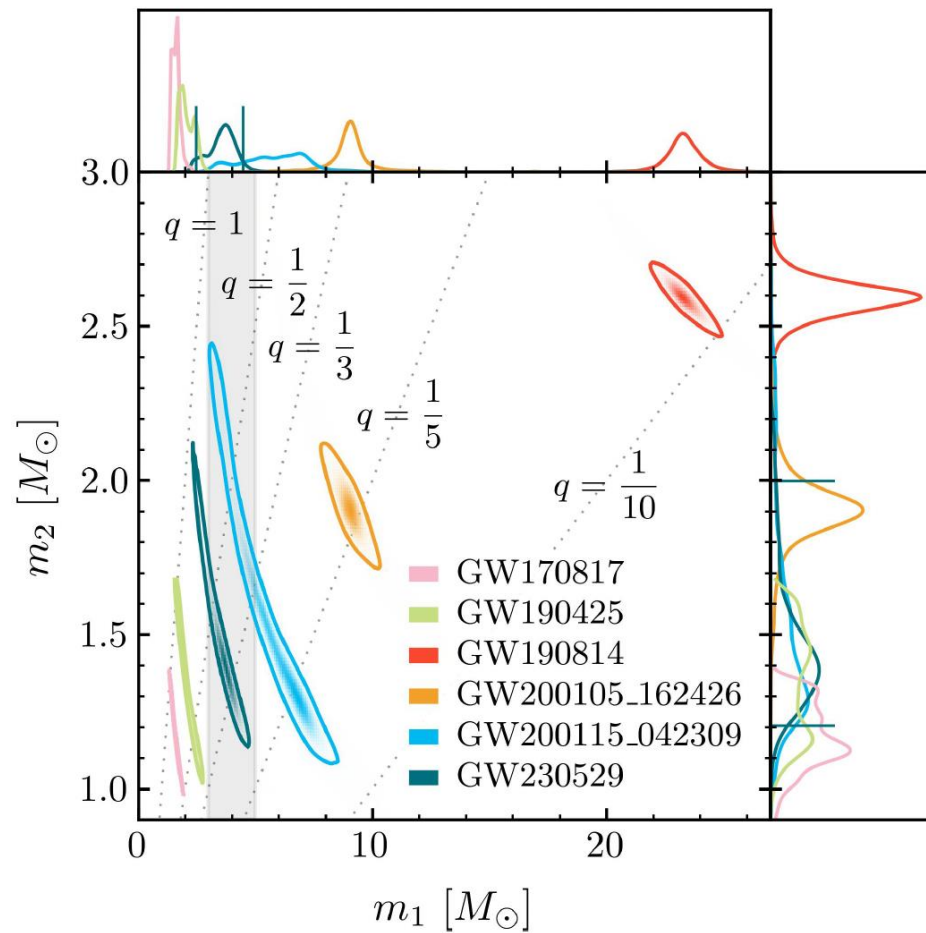
# Masses in the Stellar Graveyard

*LIGO-Virgo-KAGRA Black Holes*   *LIGO-Virgo-KAGRA Neutron Stars*   *EM Black Holes*   *EM Neutron Stars*





# The observed population

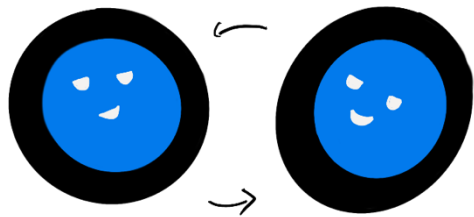


## Usefulness of neutron star-black holes

$$h(t) = \sum_{l=2}^{\infty} \sum_{m=-l}^l h_{lm}(t, \lambda) Y_{lm}^{-2}(\iota, \phi_0)$$

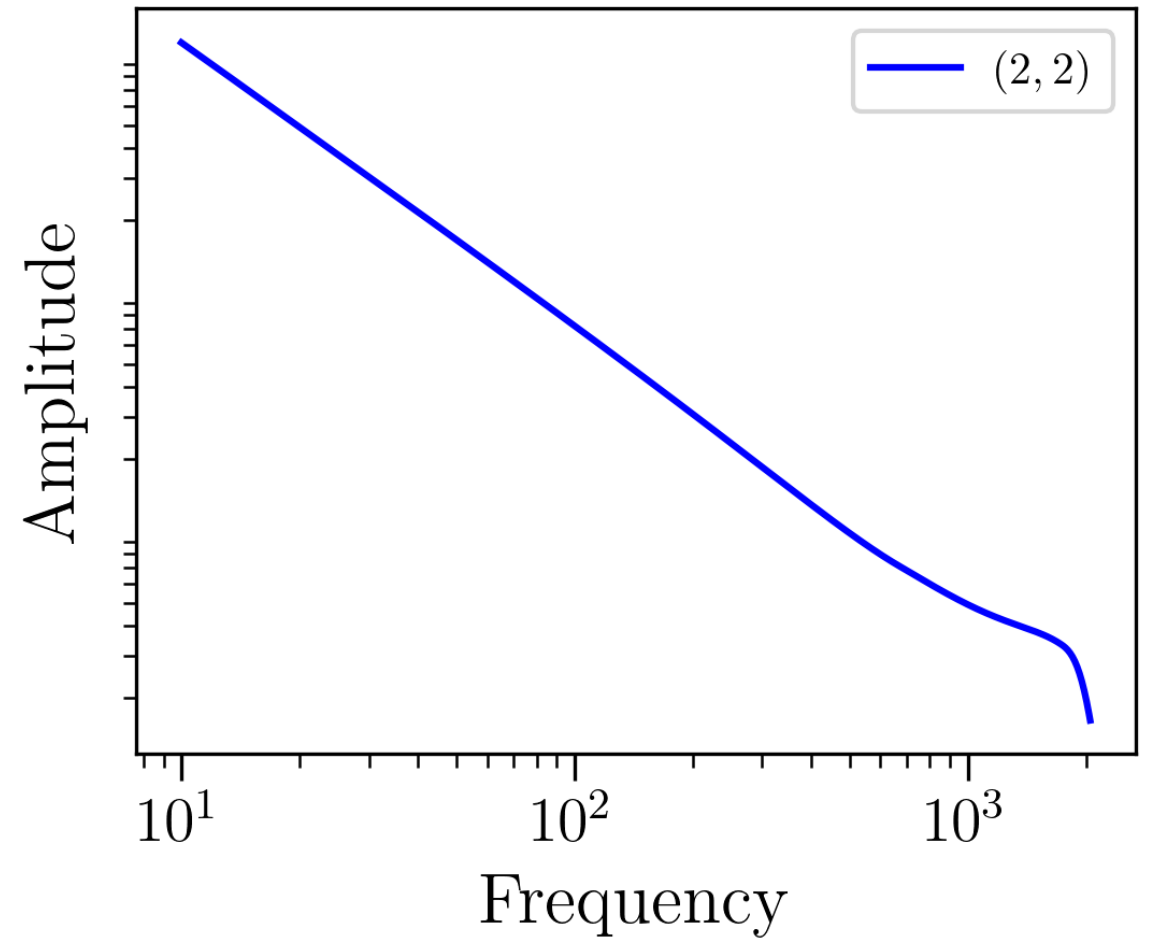
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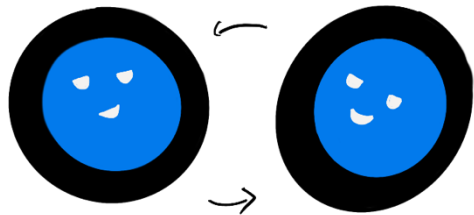
Mass symmetric

$(2, \pm 2)$



# Usefulness of neutron star-black holes

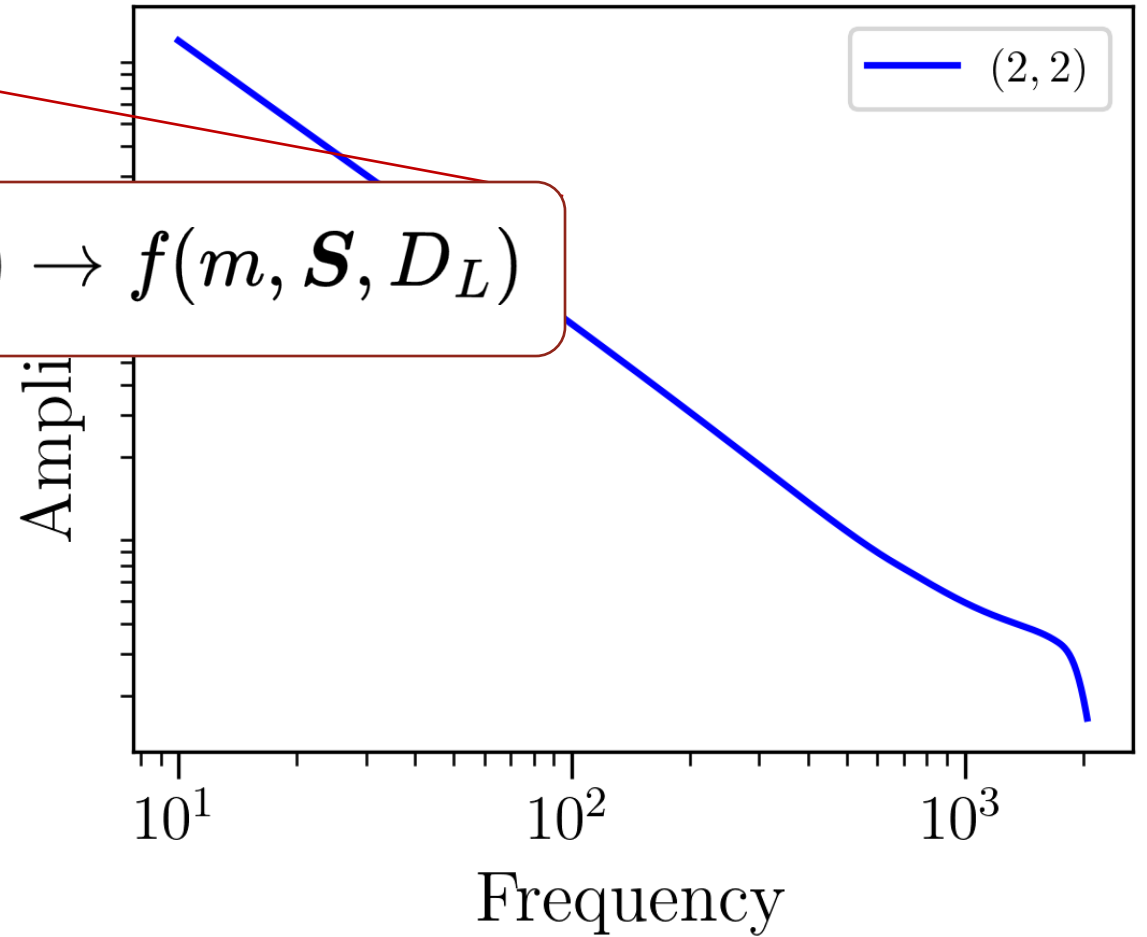
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Mass symmetric

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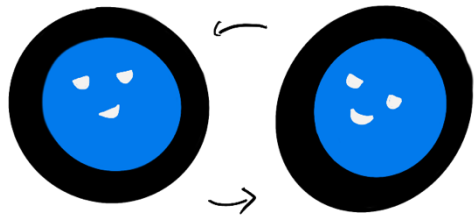
$$h(t, \lambda) \rightarrow f(m, S, D_L)$$





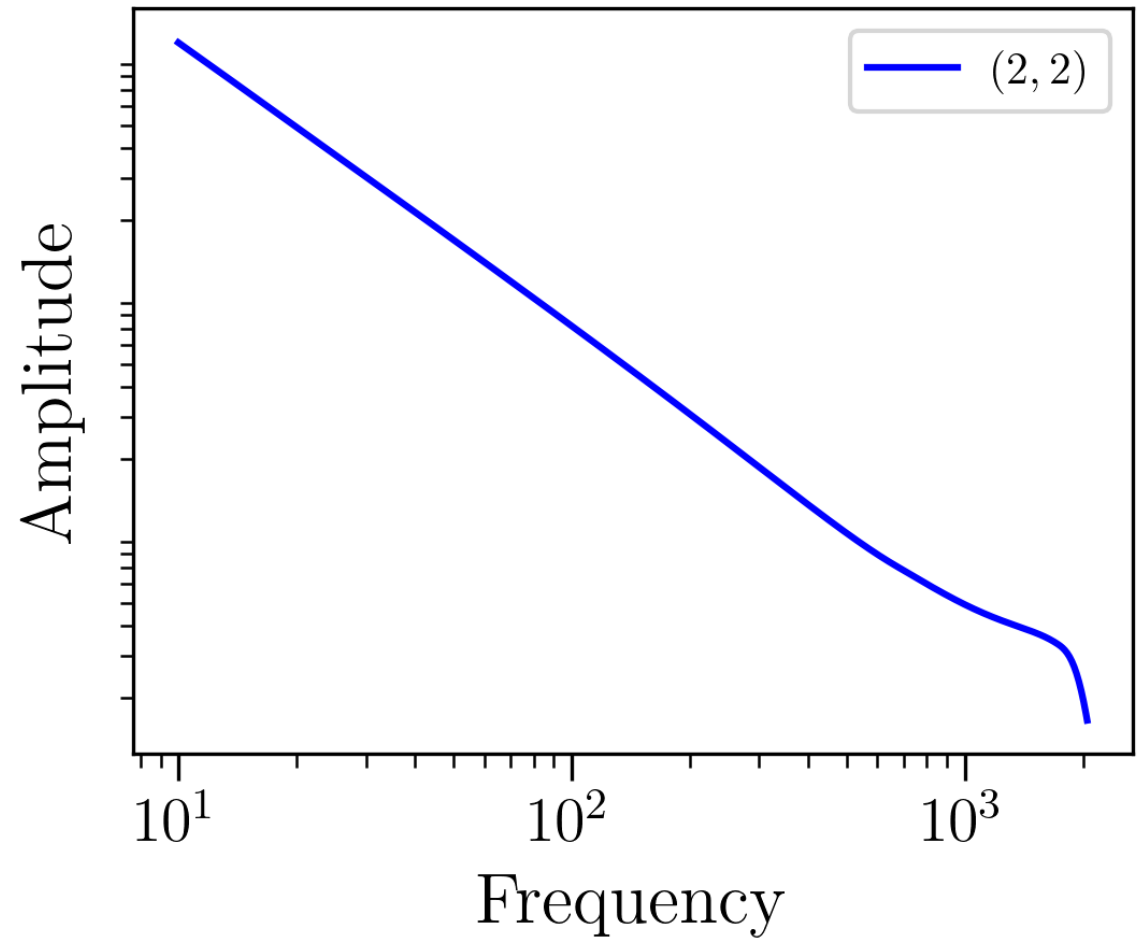
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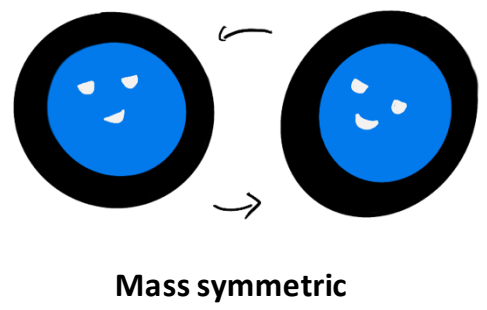
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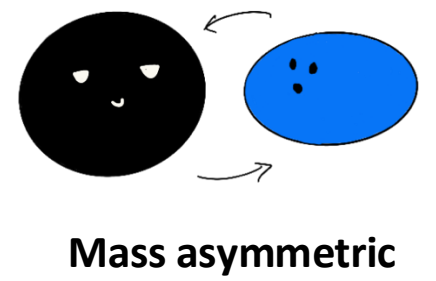


# Usefulness of neutron star-black holes

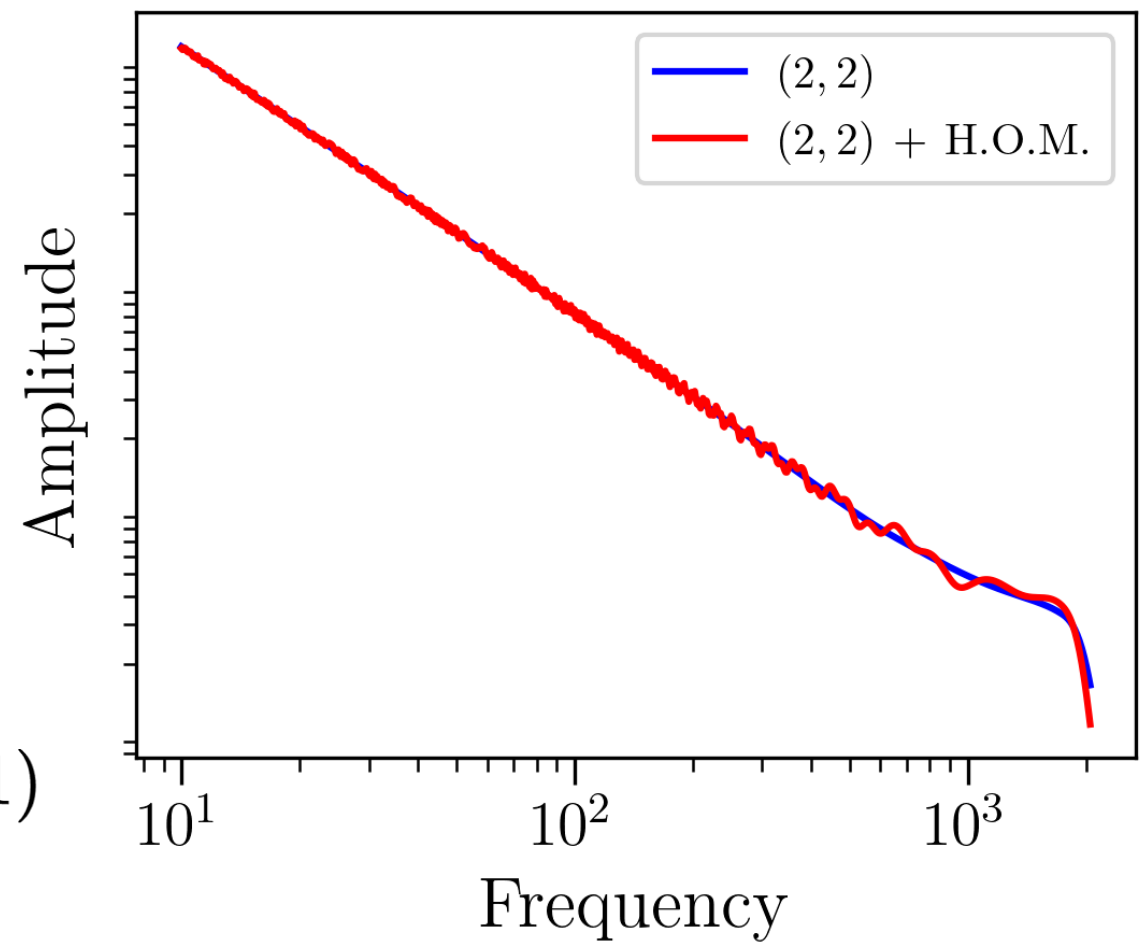
$$h(t) = \sum_{l=2}^{\infty} \sum_{m=-l}^l h_{lm}(t, \lambda) Y_{lm}^{-2}(\iota, \phi_0)$$



$(2, \pm 2)$

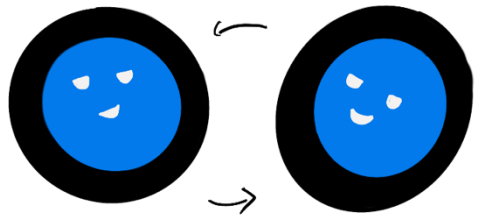


$(2, \pm 2) (3, \pm 3) (2, \pm 1)$   
 $(4, \pm 4) (3, \pm 2) \dots$



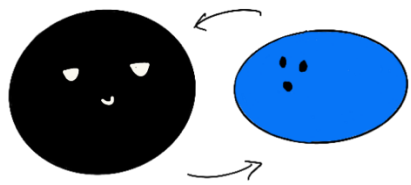
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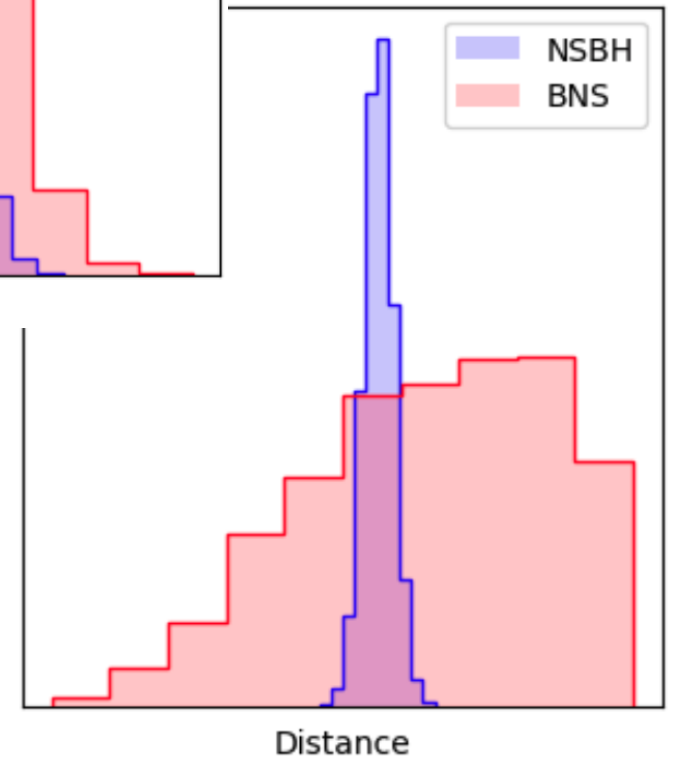
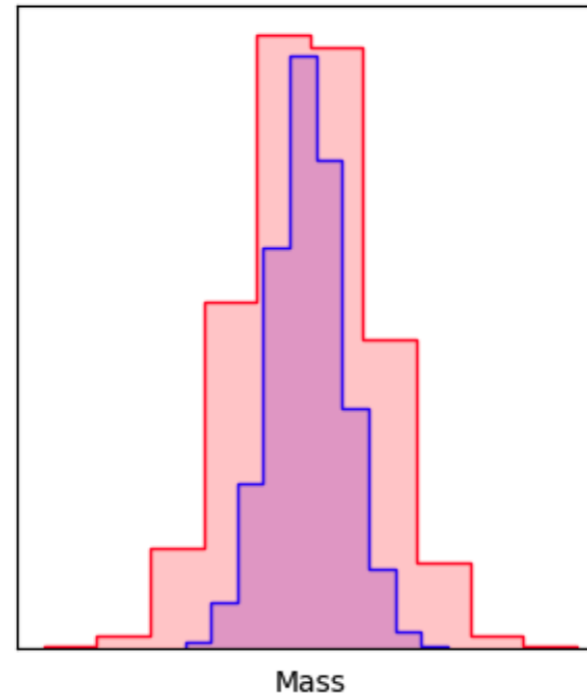
Mass symmetric

$(2, \pm 2)$



Mass asymmetric

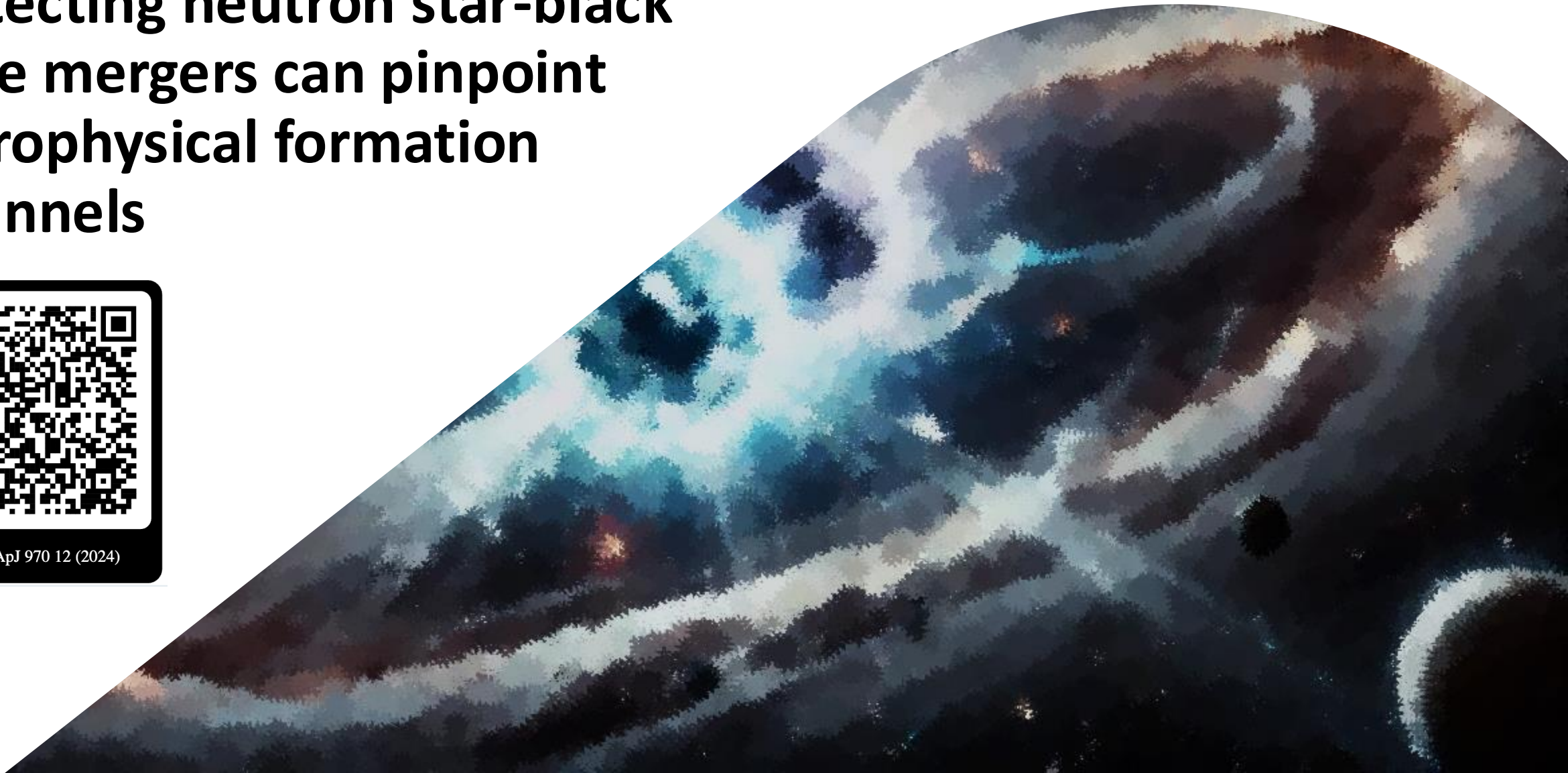
$(2, \pm 2)$   $(3, \pm 3)$   $(2, \pm 1)$   
 $(4, \pm 4)$   $(3, \pm 2)$  ...



# Detecting neutron star-black hole mergers can pinpoint astrophysical formation channels



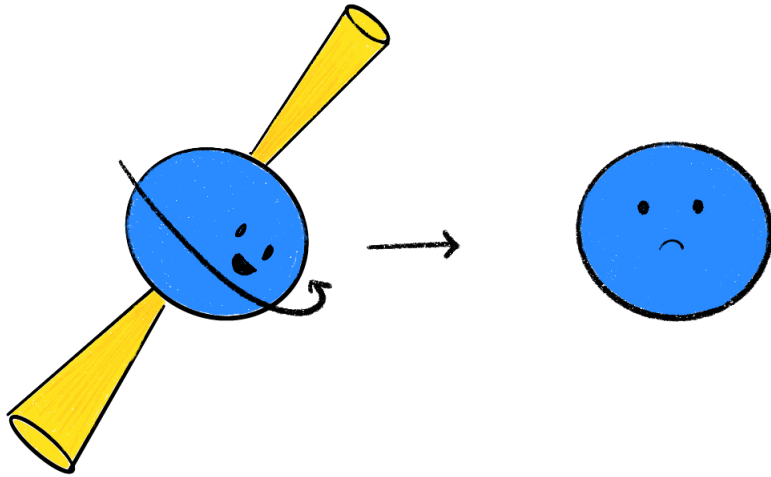
Gupta, ApJ 970 12 (2024)





## Why don't we measure neutron star's spin?

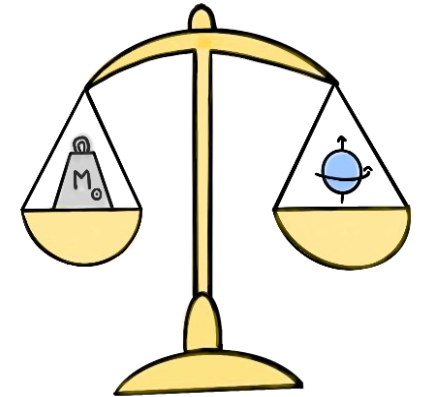
Astrophysically speaking...



Neutron stars that are born as rapidly spinning pulsars radiate away their energy and angular momentum, slowing down.

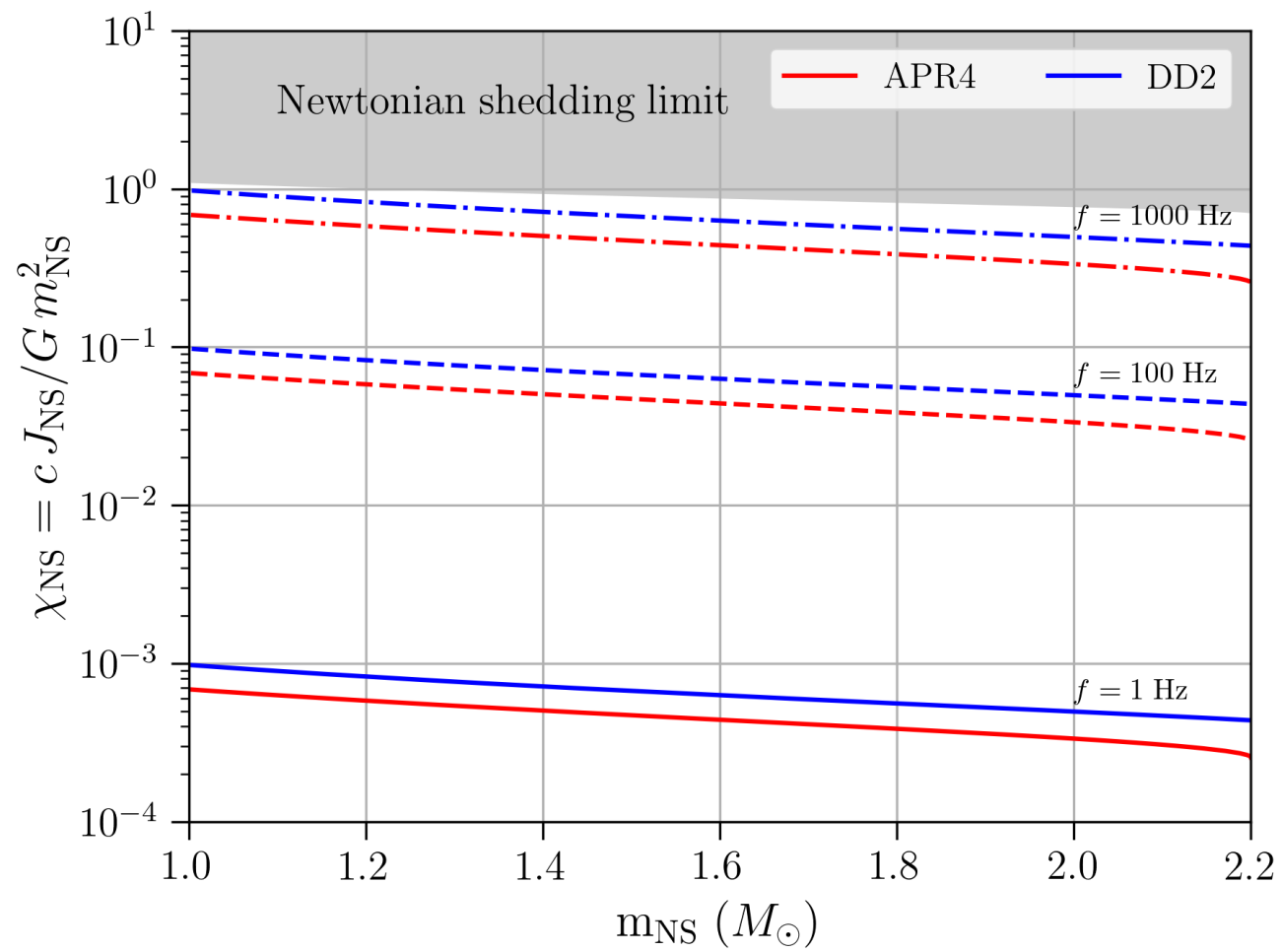
Theoretically speaking...

$$\Delta\Psi \approx \frac{55}{9}\eta + \frac{113\nu}{3}\chi_{\text{PN}} \longrightarrow$$
$$\chi_{\text{eff}} = \frac{\chi_1 + q\chi_2}{1+q}$$

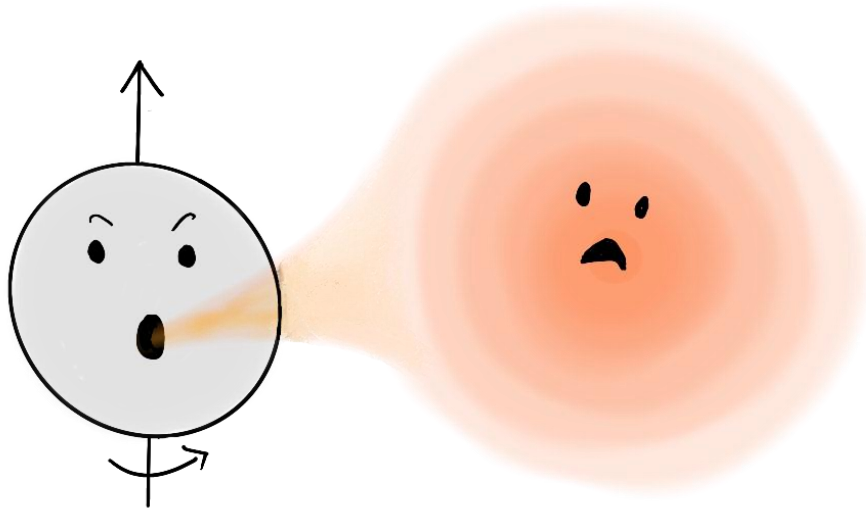


In the gravitational wave phase, the degeneracy between mass and spin parameters makes it difficult to measure component spins.

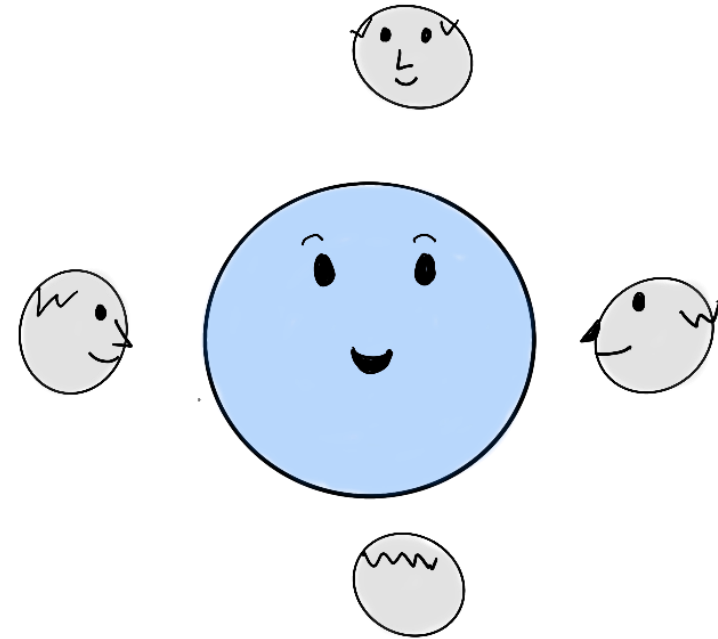
# Why don't we measure neutron star's spin?



## Can the universe form such systems?



The first-born accretes mass from the companion Helium star and spins up.



The second-born can get spun-up by tidal synchronization.

Under the constraints of the isolated binary formation, a limited number of scenarios have been proposed that can lead to a rapidly spinning neutron star at merger.

**Higher order modes to the rescue!**



## Higher order modes to the rescue!

Mode	Leading order spin terms
(2, 1)	$\frac{4i}{R} \sqrt{\frac{\pi}{5}} \eta M \tilde{\chi}$
(2, 2)	$\frac{32}{3R} \sqrt{\frac{\pi}{5}} \eta M (\chi_{\text{eff}} - \eta \chi_s)$
(3, 2)	$\frac{32}{3R} \sqrt{\frac{\pi}{7}} \eta^2 M \chi_s$
(3, 3)	$\frac{3i}{2R} \sqrt{\frac{6\pi}{7}} \eta M ((4 - 5\eta)\tilde{\chi} - 14\eta\chi_a)$
(4, 4)	$\frac{256}{9R} \sqrt{\frac{\pi}{7}} \eta M \left[ \left(-\frac{2}{3} + \frac{13}{5}\eta\right) \chi_{\text{eff}} + \frac{2\eta}{5} \left(\frac{1}{3} - 7\eta\right) \chi_s \right]$



Positive spin combinations

$$\chi_{\text{eff}} = \frac{\chi_1 + q \chi_2}{1 + q}$$

$$\chi_s = \frac{\chi_1 + \chi_2}{2}$$

## Higher order modes to the rescue!

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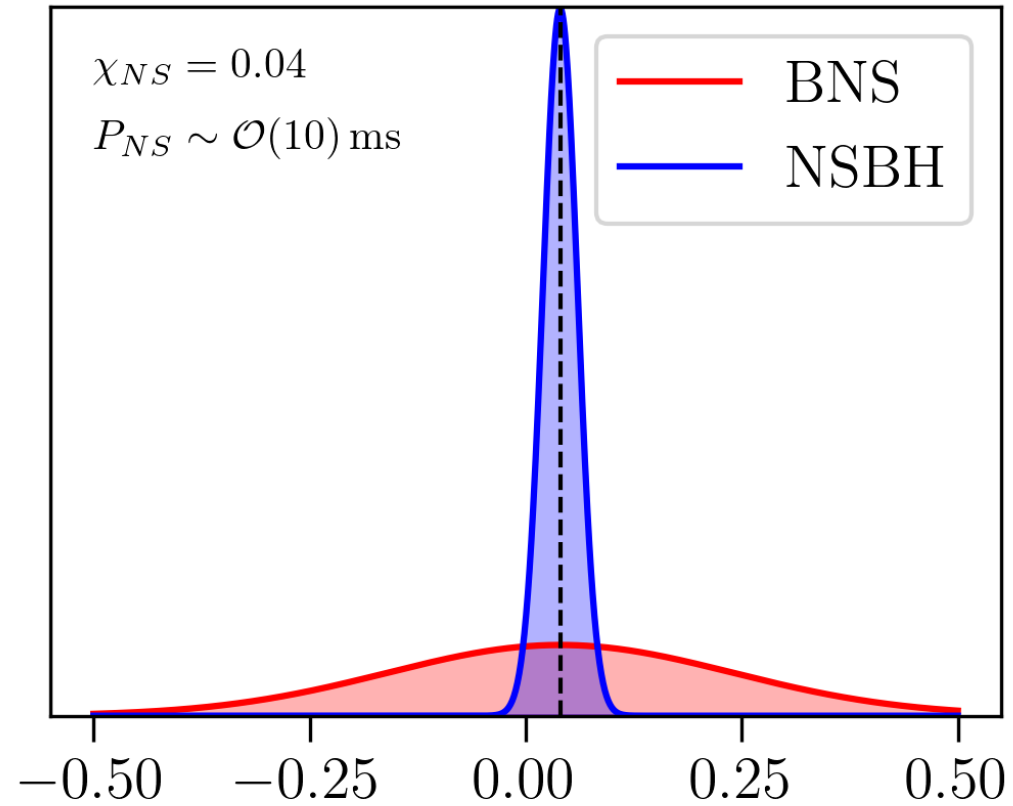


Negative spin combinations

$$\tilde{\chi} = \frac{\chi_1 - q \chi_2}{1 + q}$$

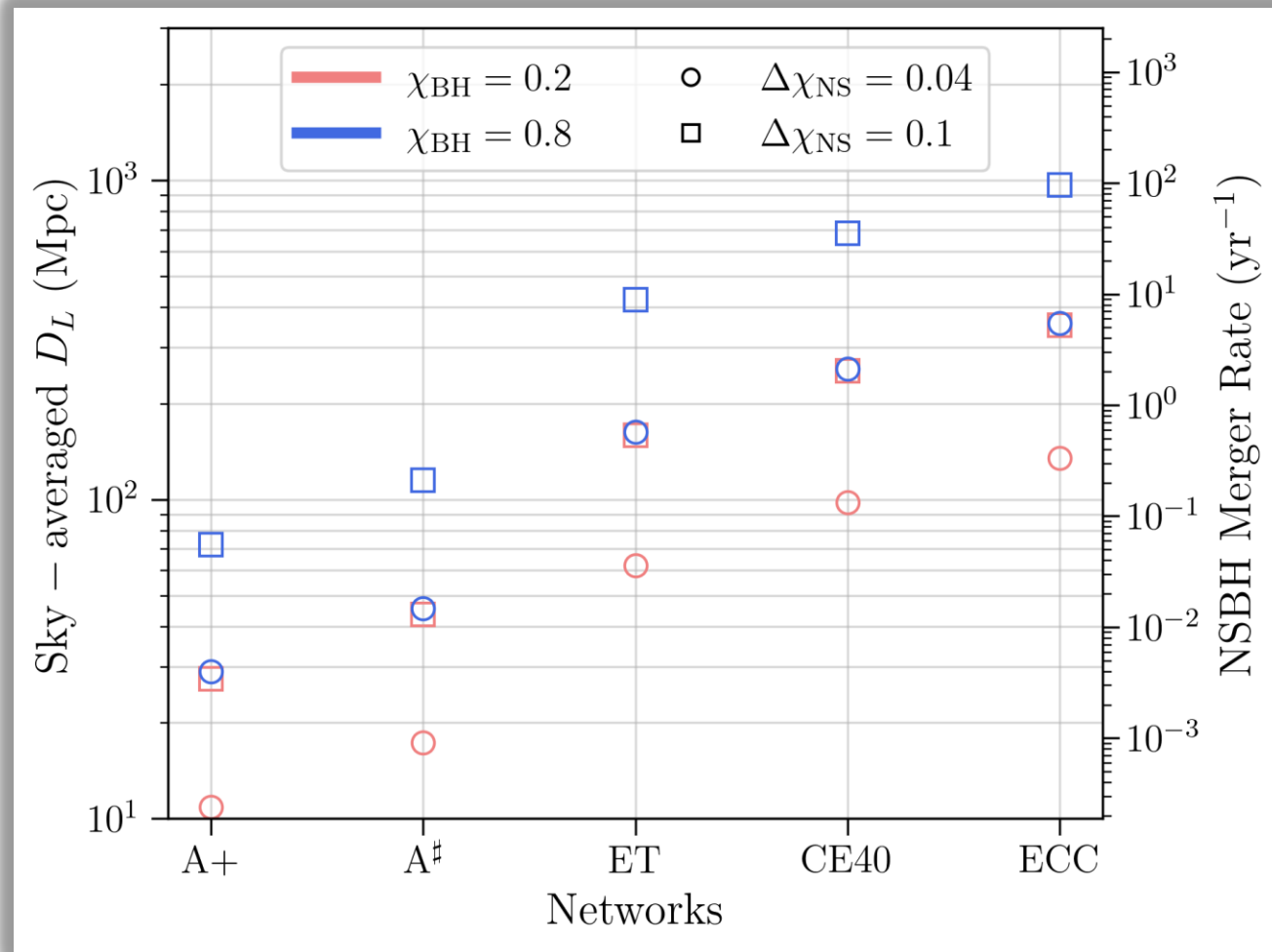
$$\chi_a = \frac{\chi_1 - \chi_2}{2}$$

## Can we measure it?



*The spin of a neutron star is much more precisely measured with a neutron star-black hole merger detection compared to a binary neutron star detection.*

## Can we measure it?

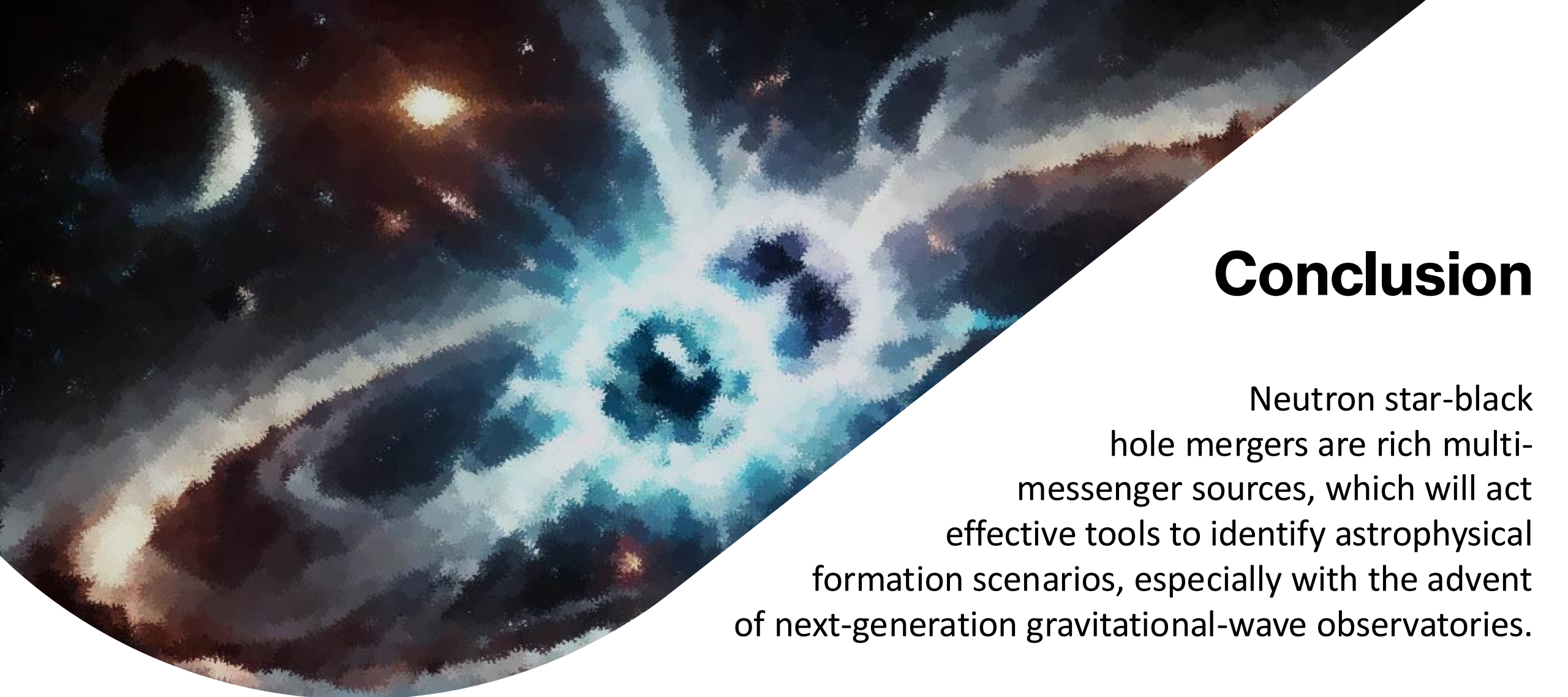


*Next-generation observatories can precisely measure the spin of a neutron star with neutron star-black hole mergers, even if they were to happen a Gpc away.*





# Conclusion



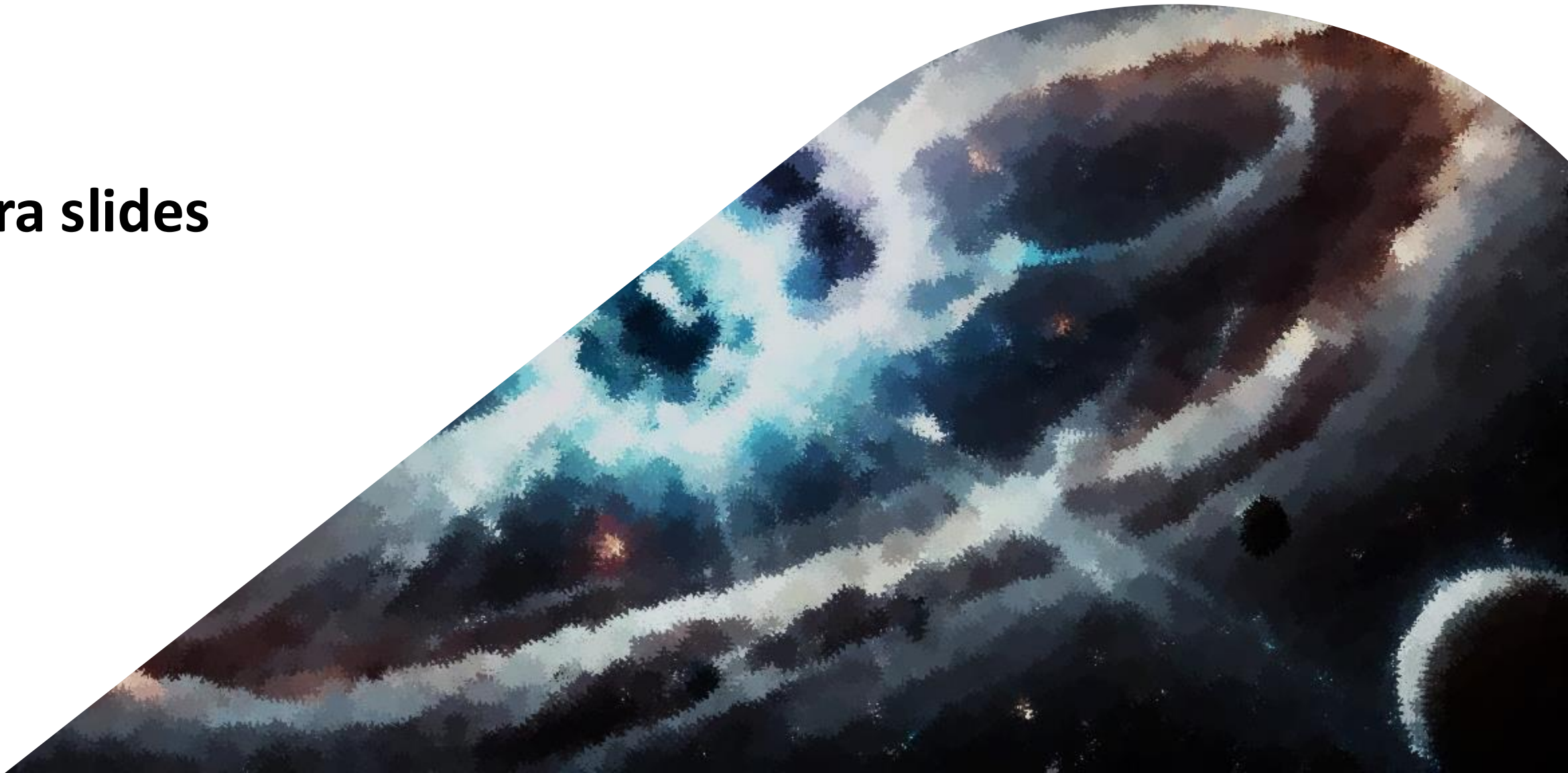
## Conclusion

Neutron star-black hole mergers are rich multi-messenger sources, which will act effective tools to identify astrophysical formation scenarios, especially with the advent of next-generation gravitational-wave observatories.

*Let's not sleep on neutron star-black hole mergers!*



**Extra slides**



## Using gravitational-wave detections

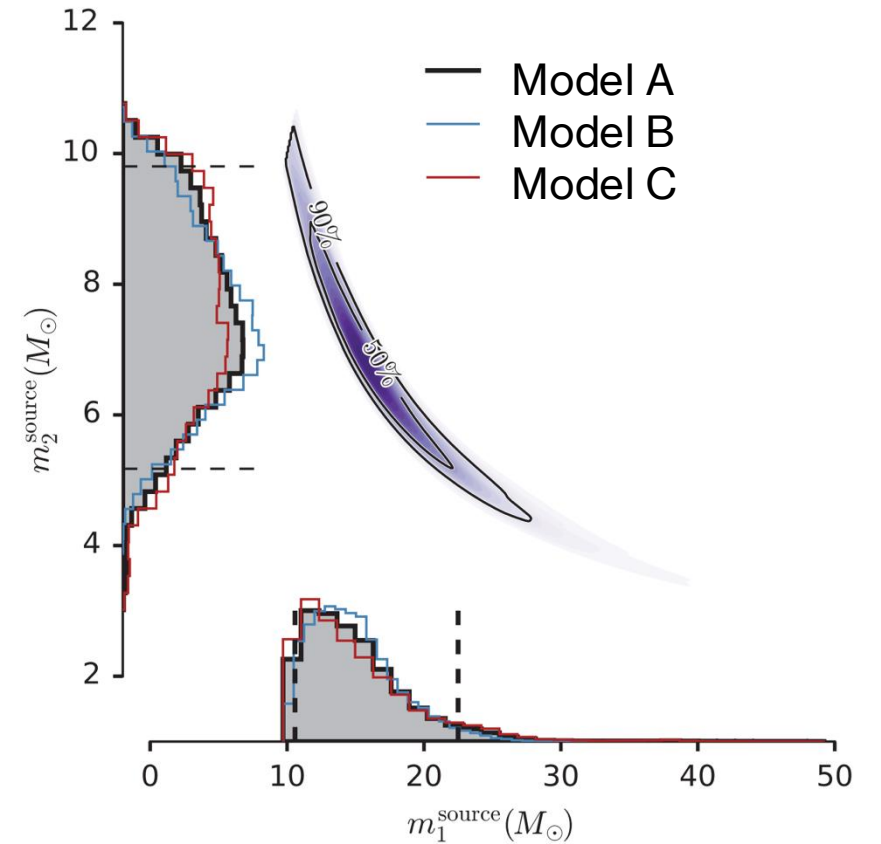
$$p(\boldsymbol{\theta} \mid \mathbf{d}, H) = \frac{p(\mathbf{d} \mid \boldsymbol{\theta}, H) p(\boldsymbol{\theta} \mid H)}{p(\mathbf{d} \mid H)}$$

**Likelihood** (points to  $p(\mathbf{d} \mid \boldsymbol{\theta}, H)$ )

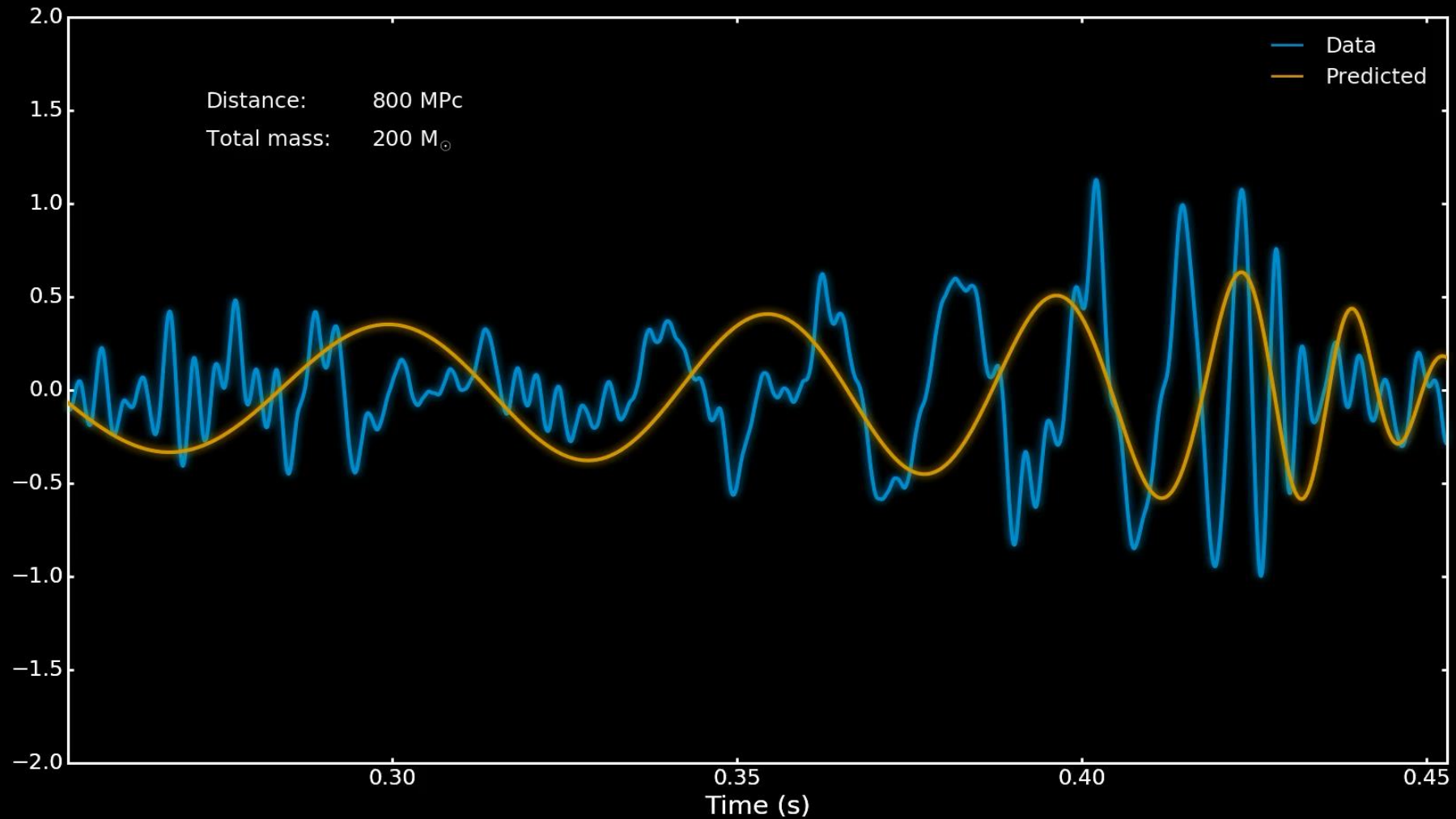
**Prior** (points to  $p(\boldsymbol{\theta} \mid H)$ )

**Evidence** (points to  $p(\mathbf{d} \mid H)$ )

**Posterior** (points to  $p(\boldsymbol{\theta} \mid \mathbf{d}, H)$ )

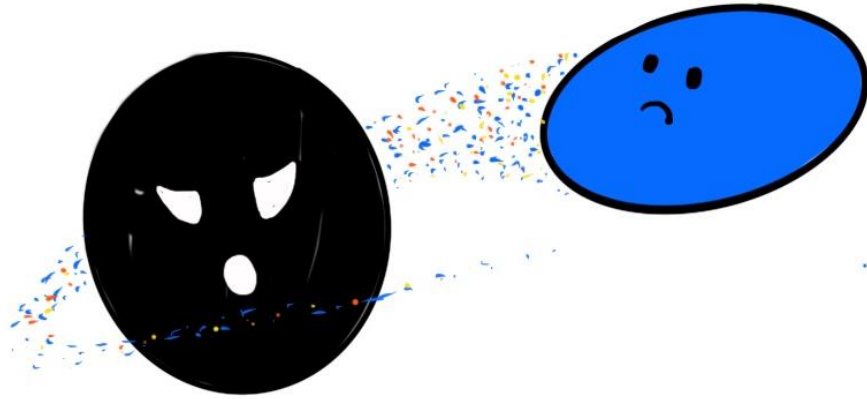


## Using gravitational-wave detections

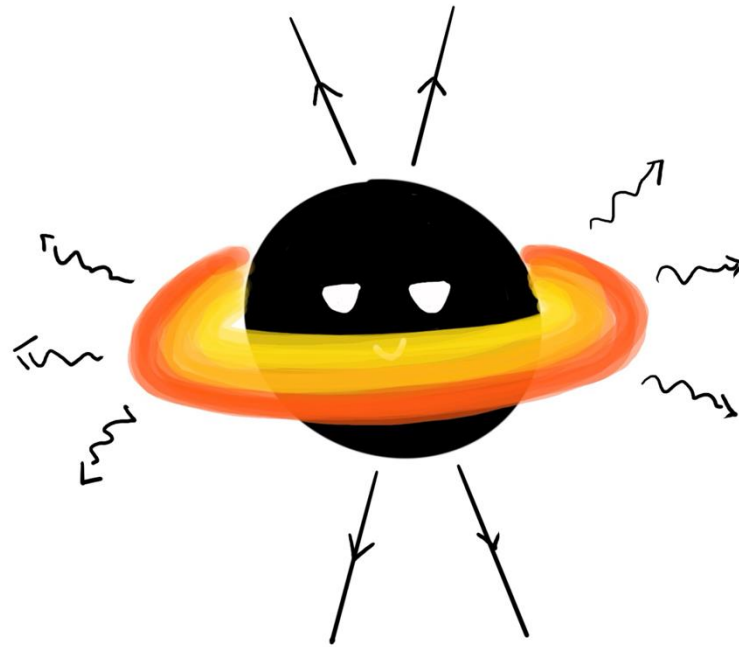
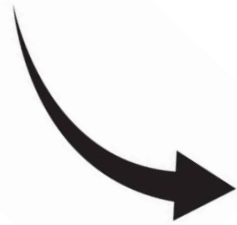


Data & Best-fit Waveform: LIGO Open Science Center ([losc.ligo.org](http://losc.ligo.org)); Prediction & Animation: C.North/M.Hannam (Cardiff University)

## Usefulness of neutron star-black holes



$$\frac{r_{ms}}{r_{ISCO}} \propto q^{-2/3} C^{-1} \hat{r}_{ISCO}^{-1}(\chi)$$

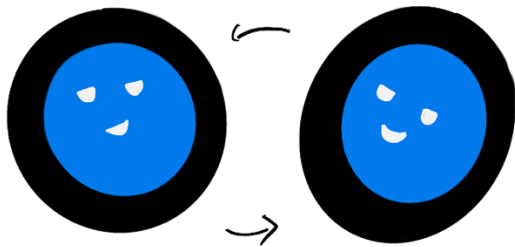


$$q = \frac{m_{BH}}{m_{NS}}$$

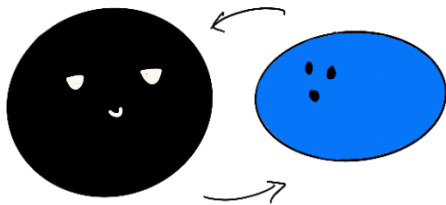
$$C = \frac{Gm_{NS}}{c^2 R_{NS}}$$



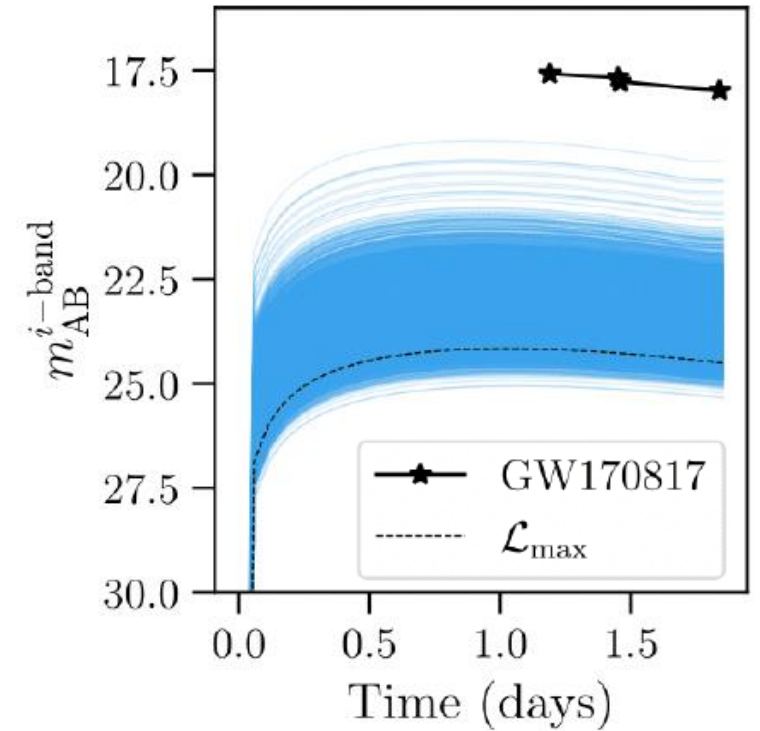
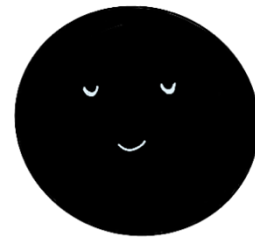
## Usefulness of neutron star-black holes



Mass symmetric



Mass asymmetric

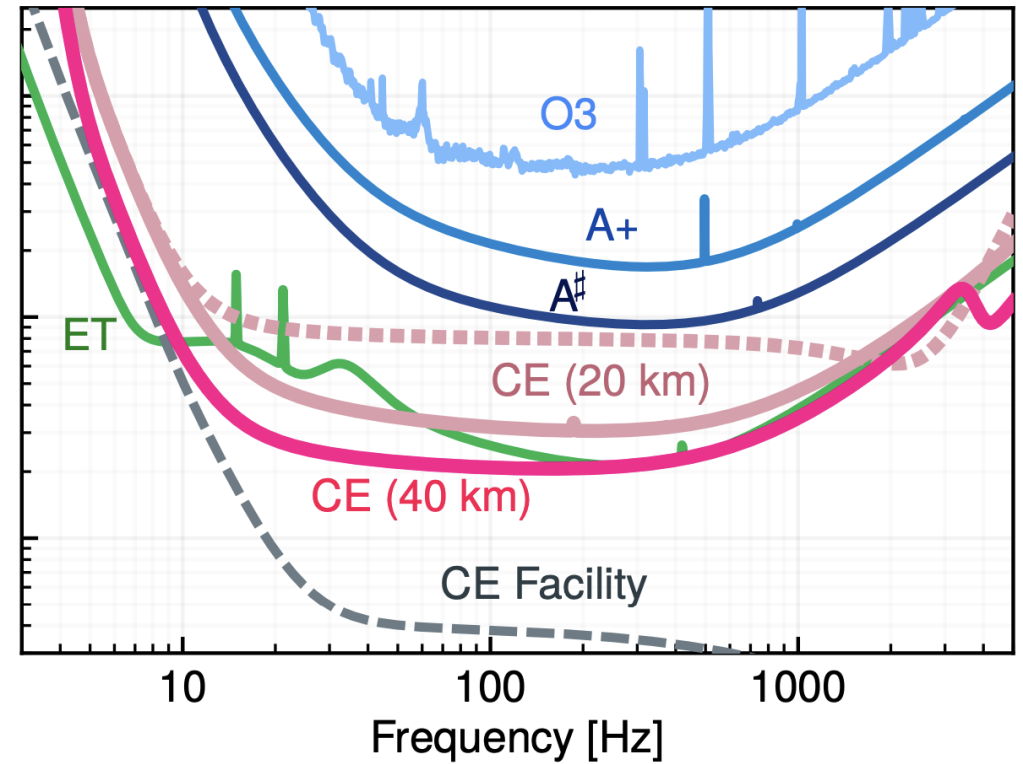
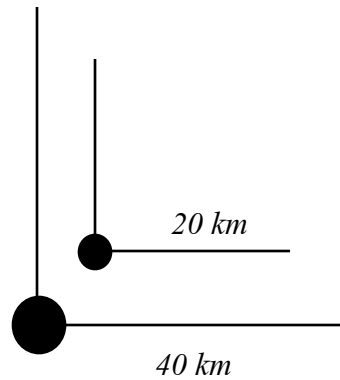
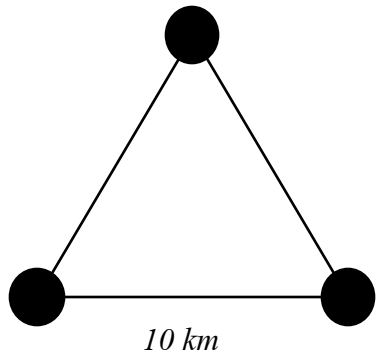


The probably  $i$ -band kilonovae light curves for GW230529. (Chandra, **Gupta**, et al. *ApJ* 977, 2024)

# Looking toward the future

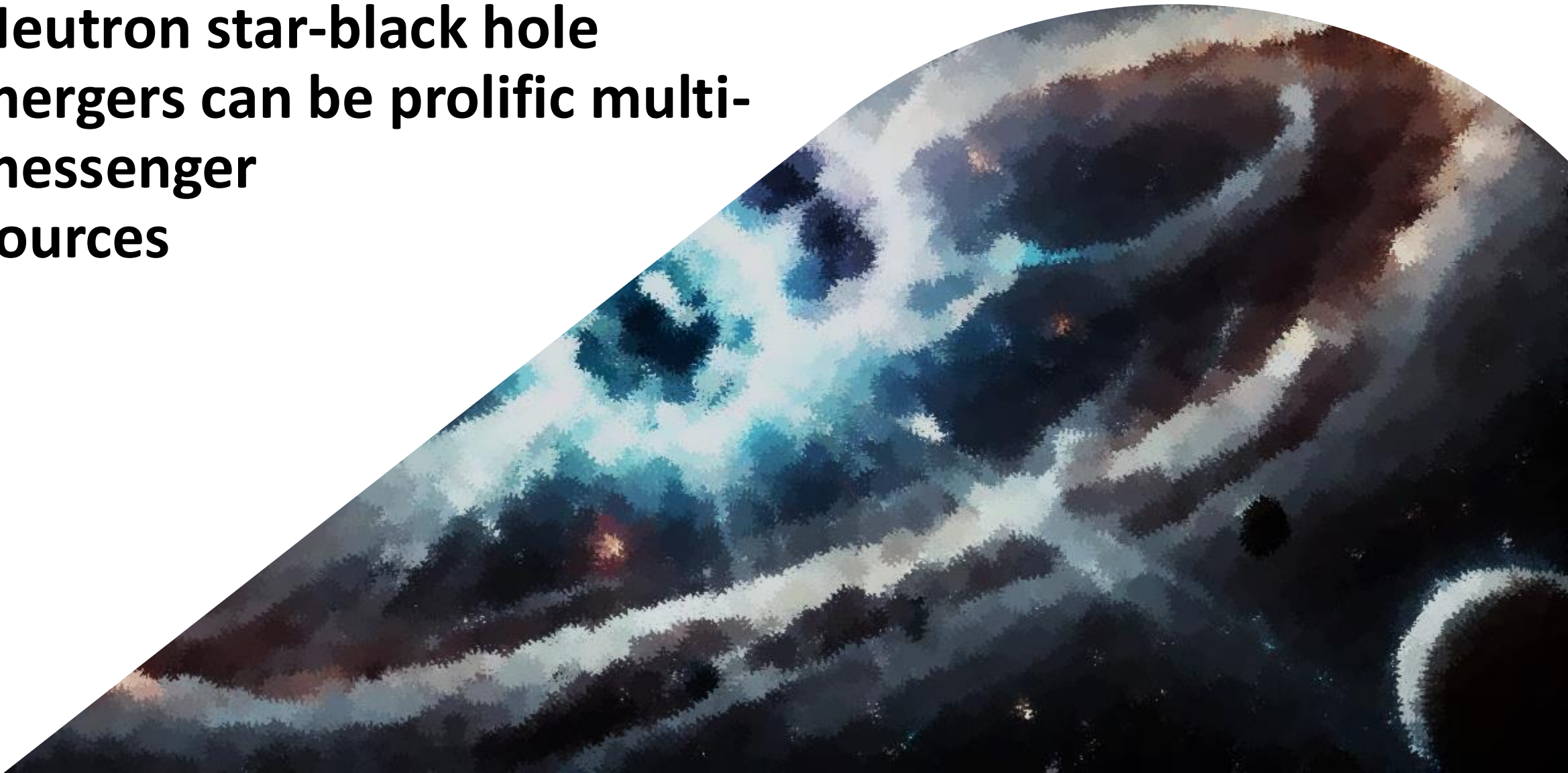
More observations

Louder signals



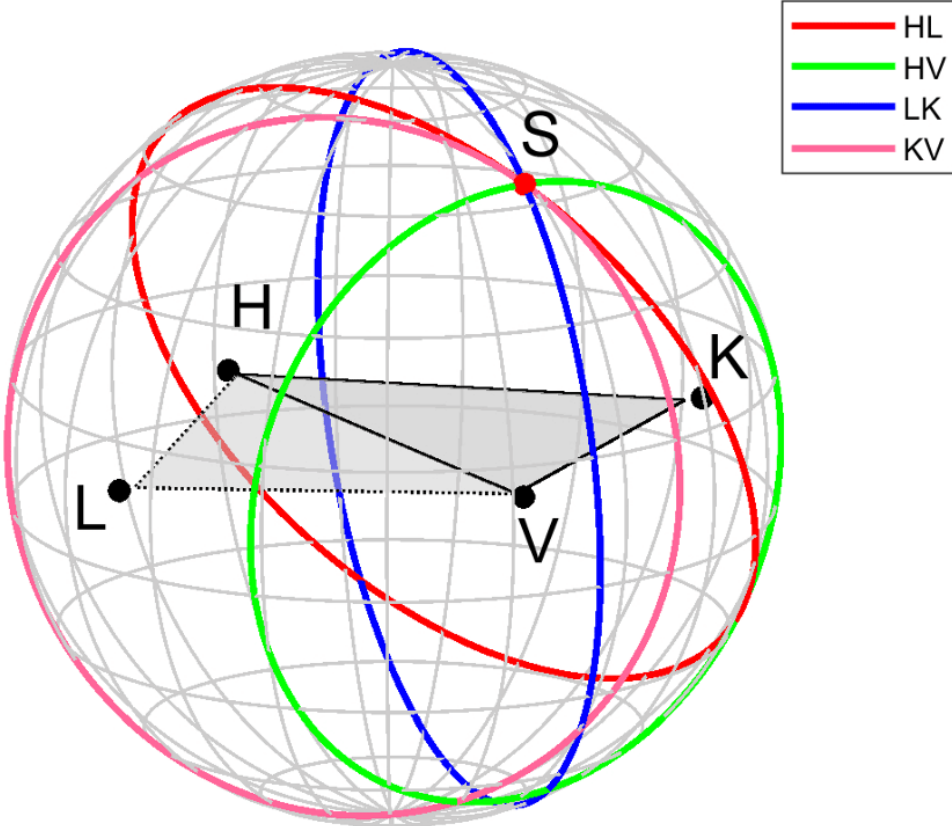
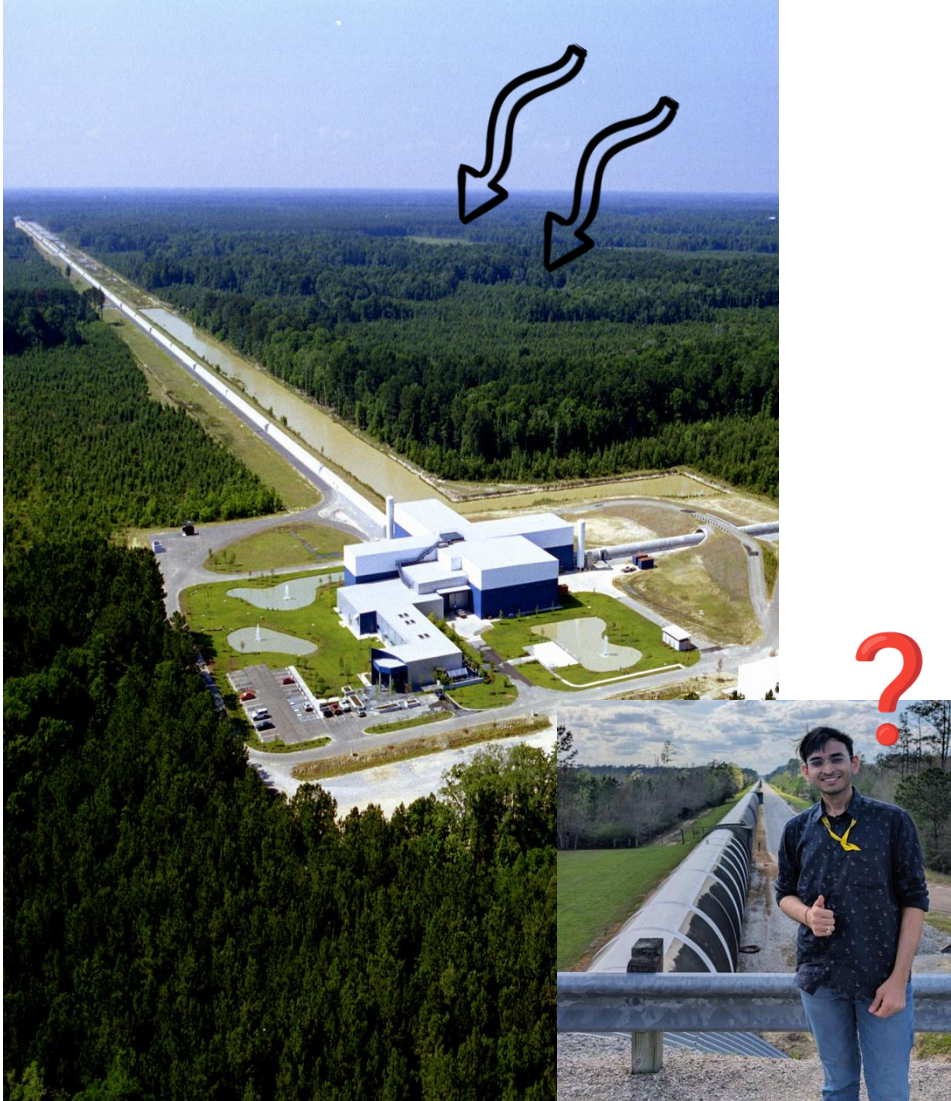
The sensitivity curves of different detectors. (Gupta et al. CQG 41, 2024)

**Neutron star-black hole  
mergers can be prolific multi-  
messenger  
sources**

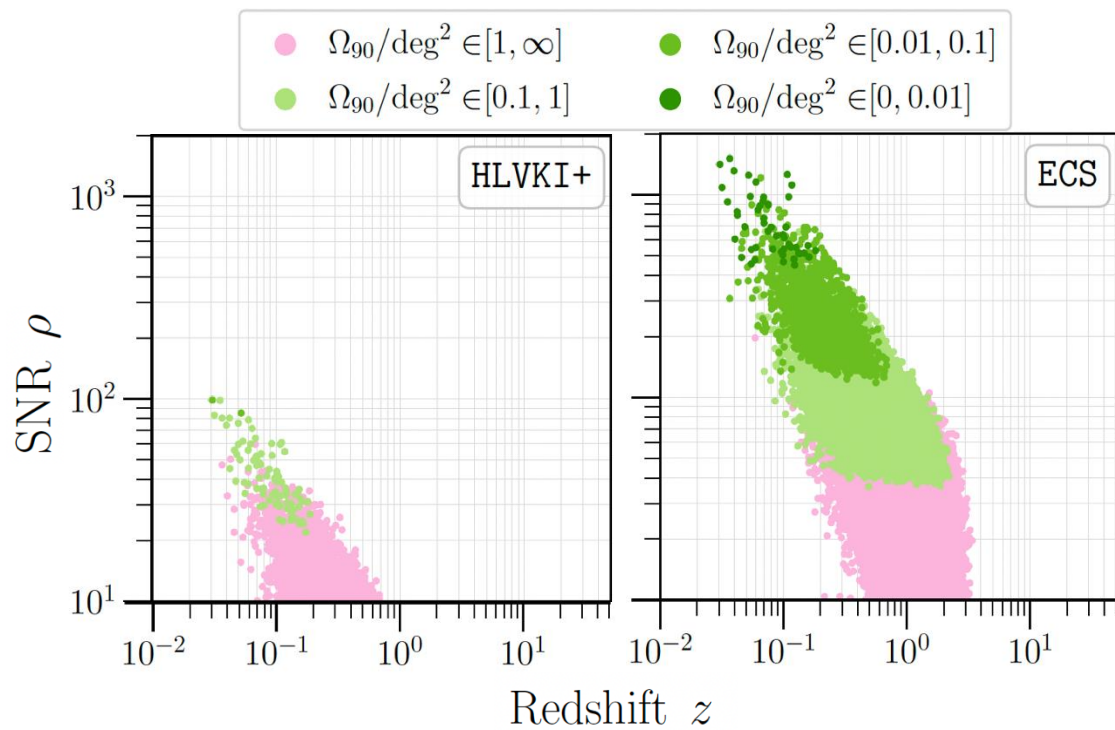




# Localization of events in the sky

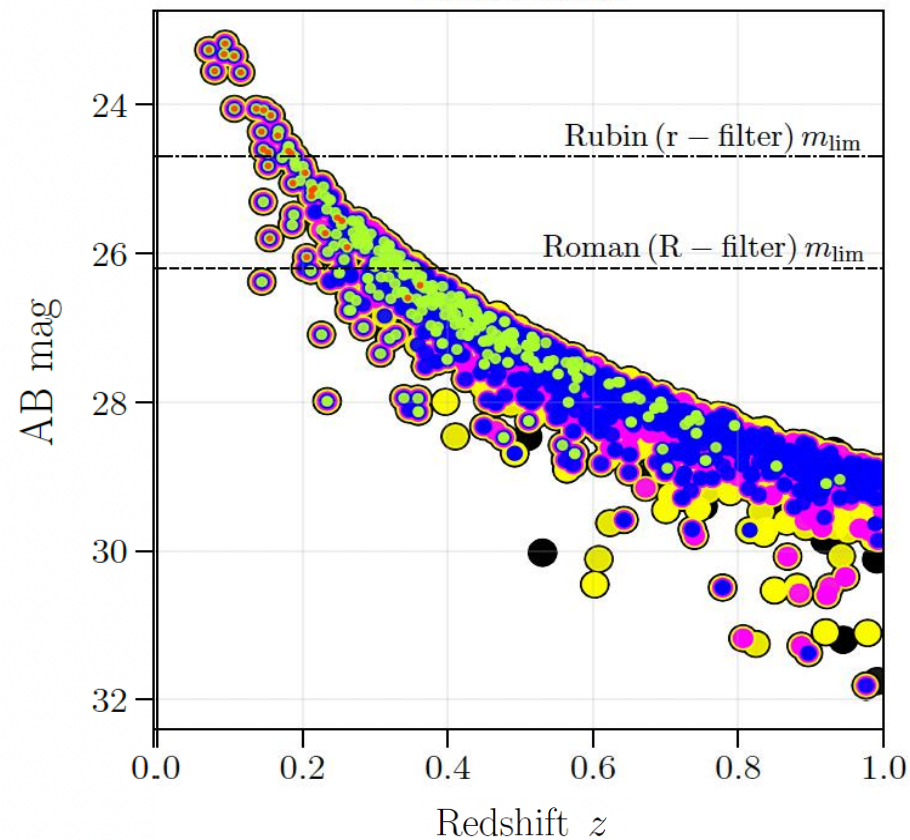


# Localization of events in the sky



- ECS
- KI+EC
- HLKI+E
- VKI+C
- VK+HLI<sub>v</sub>
- HLVKI+

EOS : DD2



## Measuring the cosmic expansion

Gravitational waves already provide distance, all we need is redshift.

$$D_L = \frac{1+z}{H_0} \int_{1/(1+z)}^1 \frac{dx}{x^2 \sqrt{\Omega_\Lambda + \Omega_m x^{-3}}}$$

Planck 2018

$$H_0 = 67.4 \pm 0.5 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

Using cosmic microwave background measurements

**TENSION**

SHOES

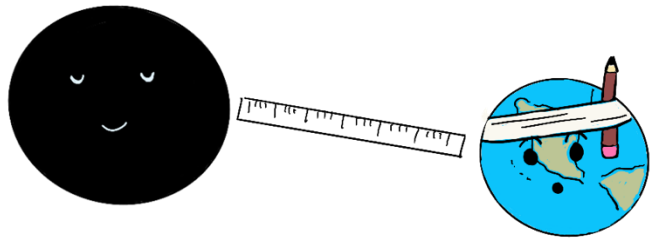
$$H_0 = 73.30 \pm 1.04 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

Using Type 1A supernovae

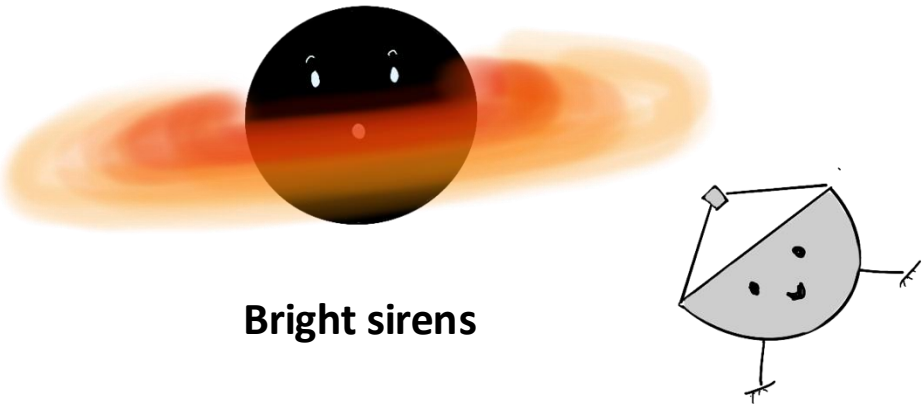
Gravitational waves can provide an independent measure of  $H_0$  and resolve the Hubble tension.



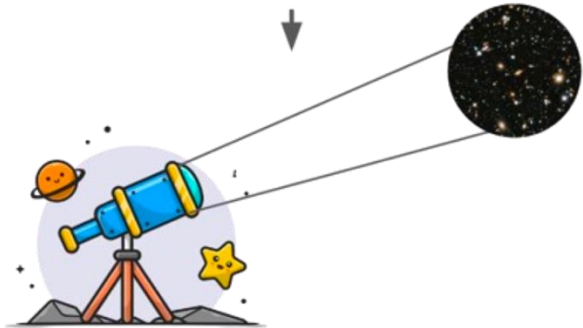
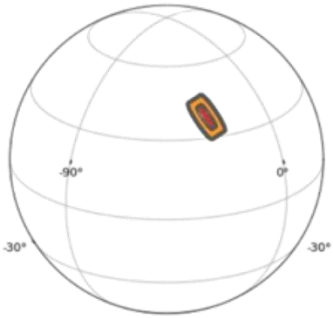
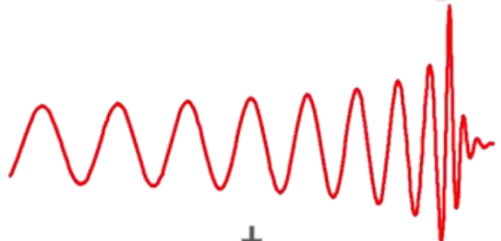
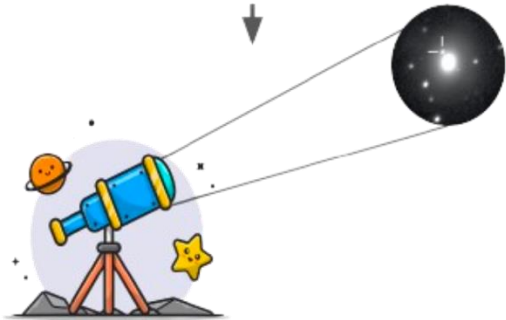
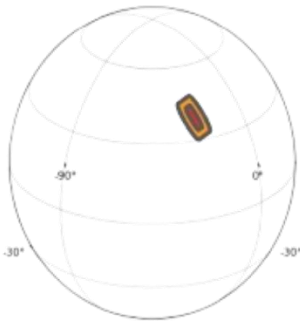
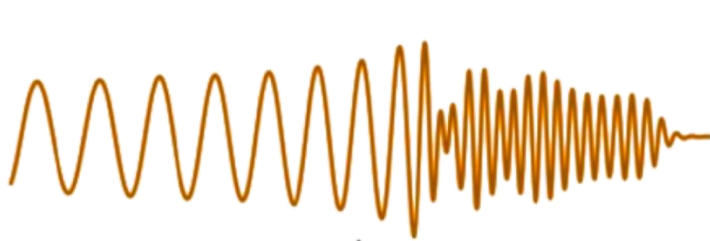
# Gravitational-wave sirens



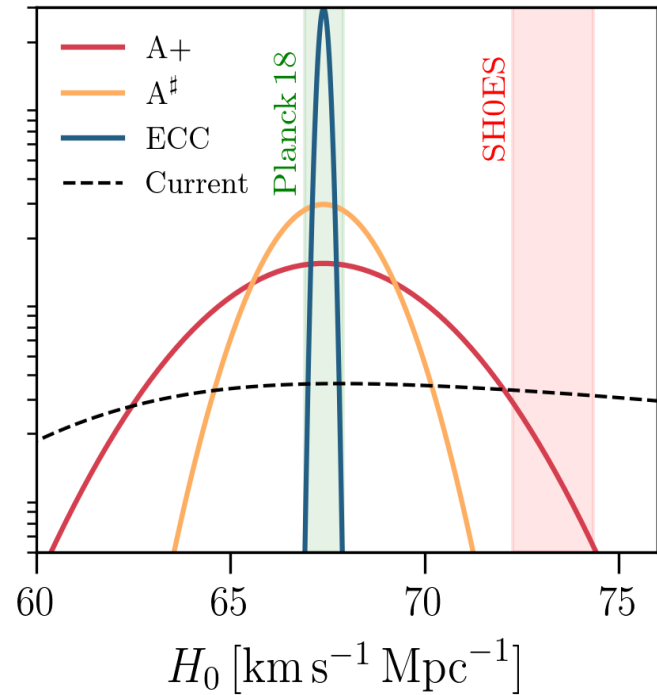
Dark sirens



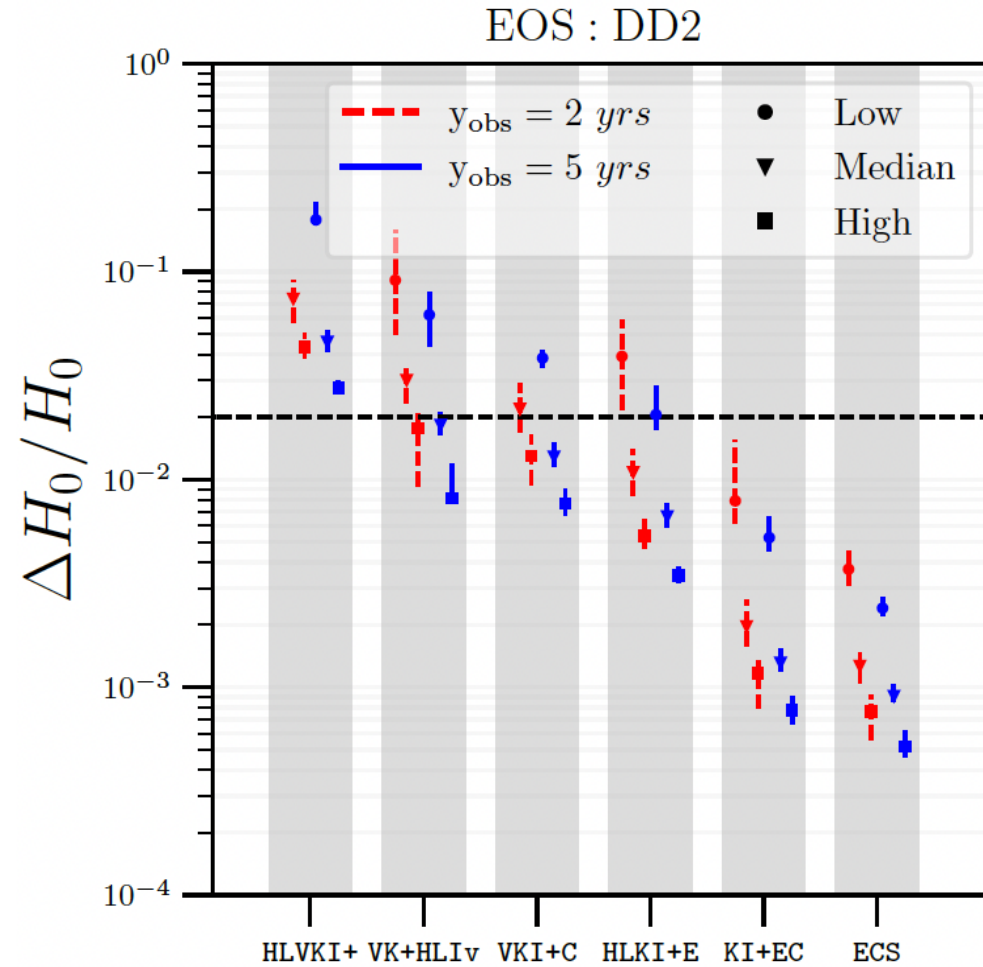
Bright sirens



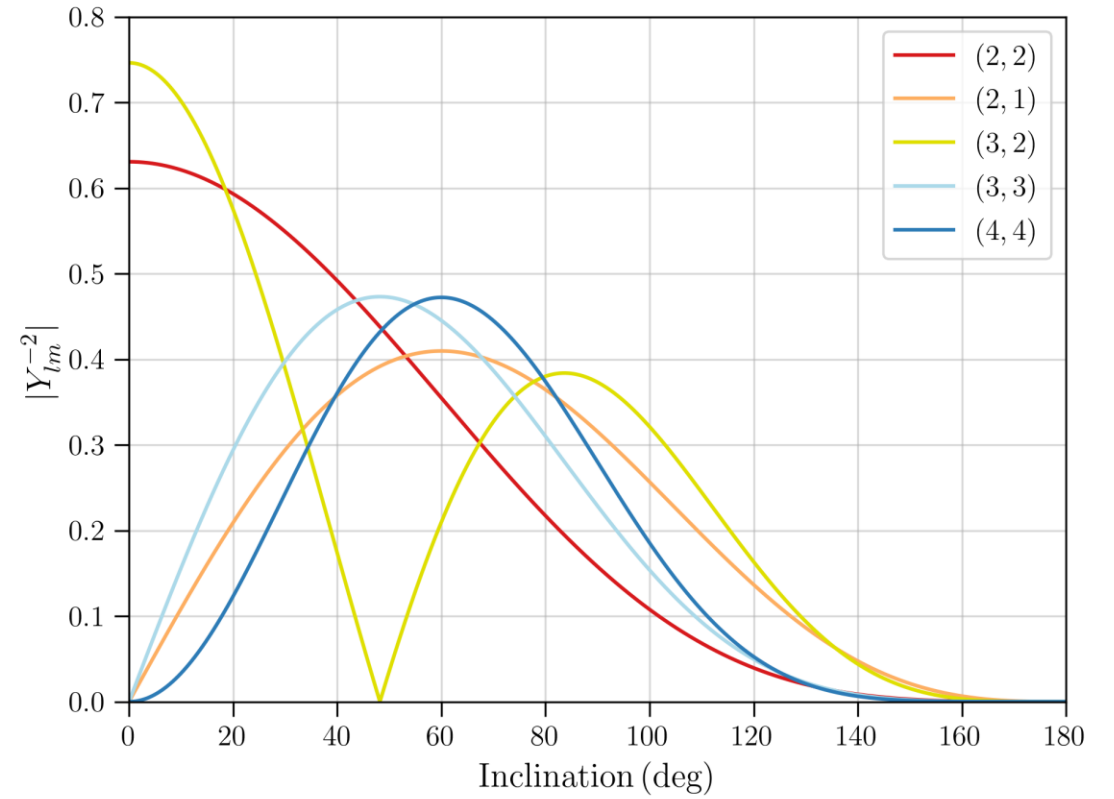
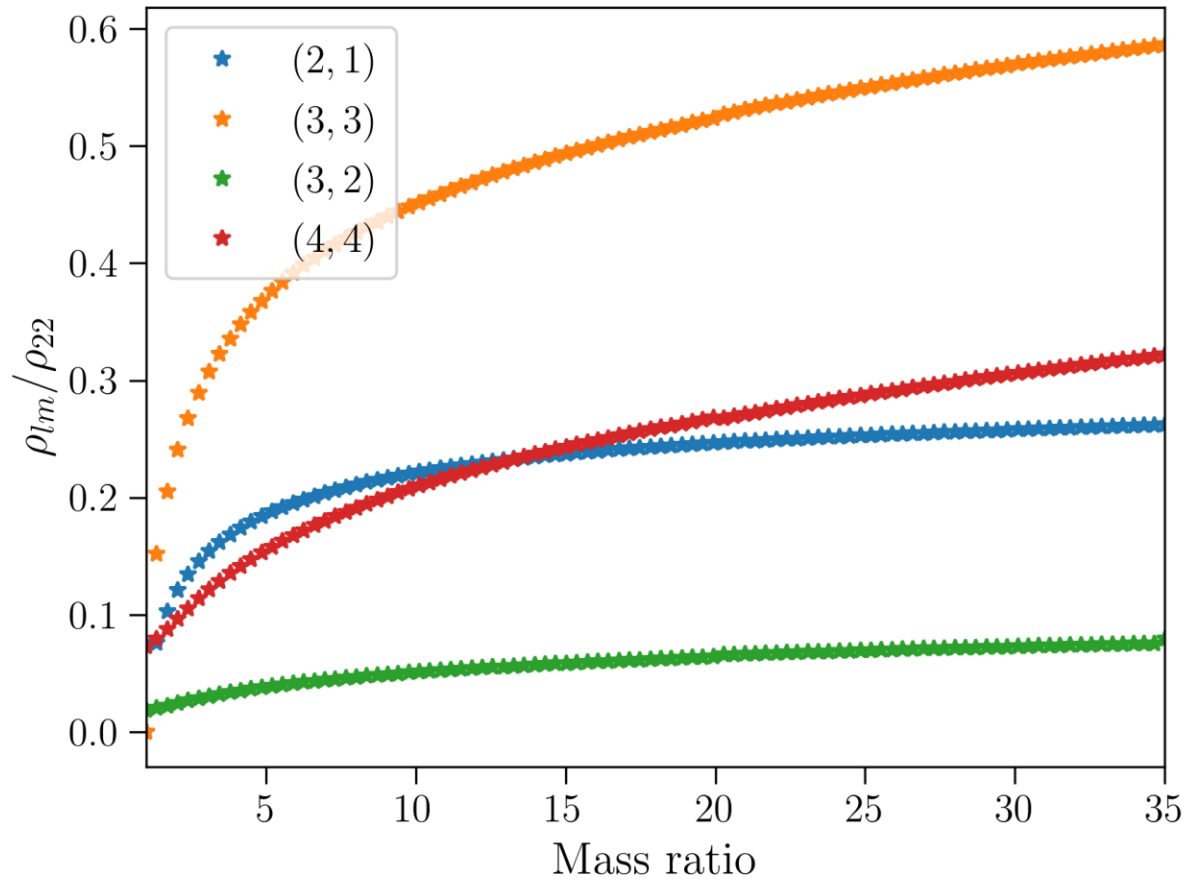
# Resolving the Hubble tension



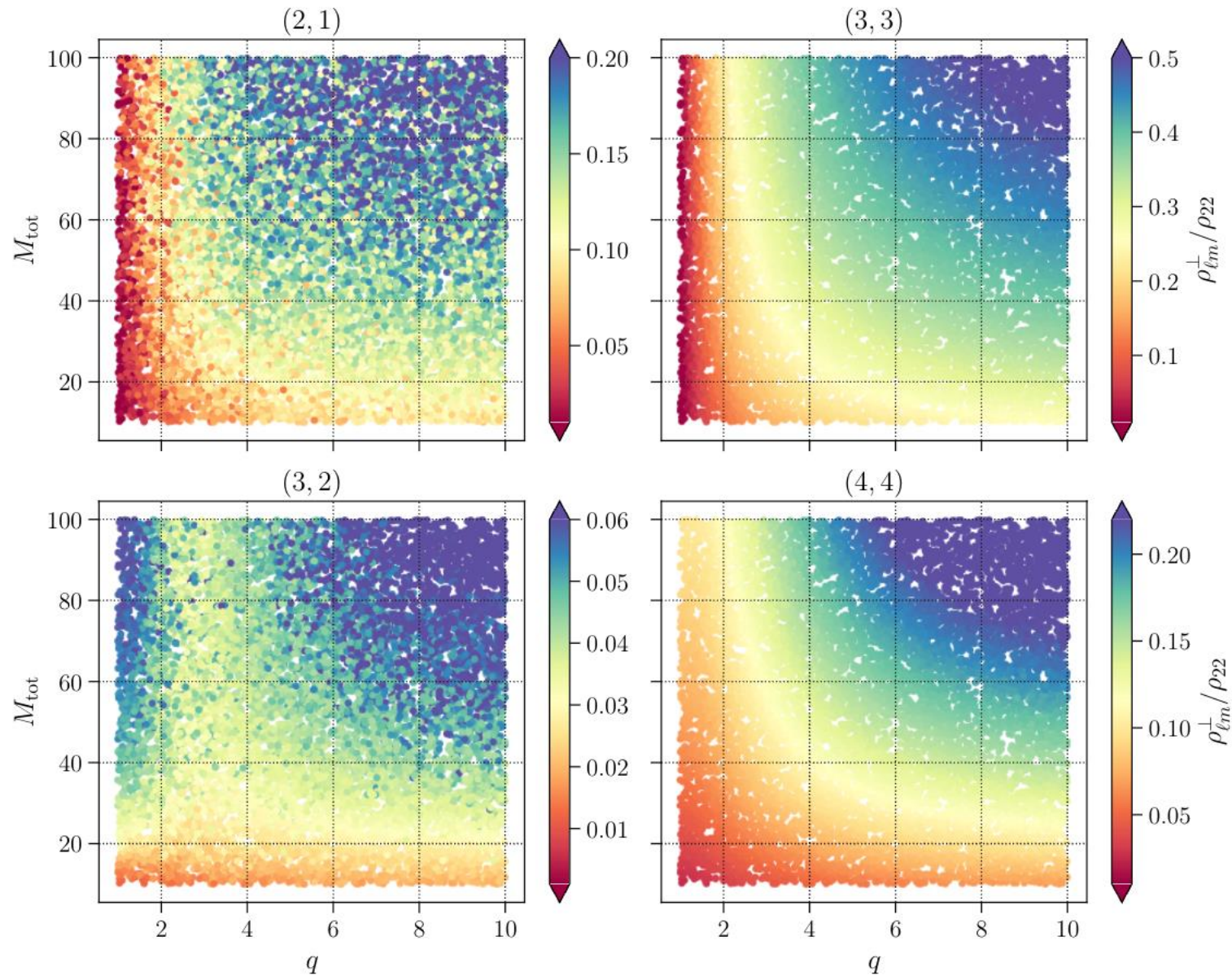
*Neutron star-black hole mergers make excellent cosmological probes.*



## Higher order modes

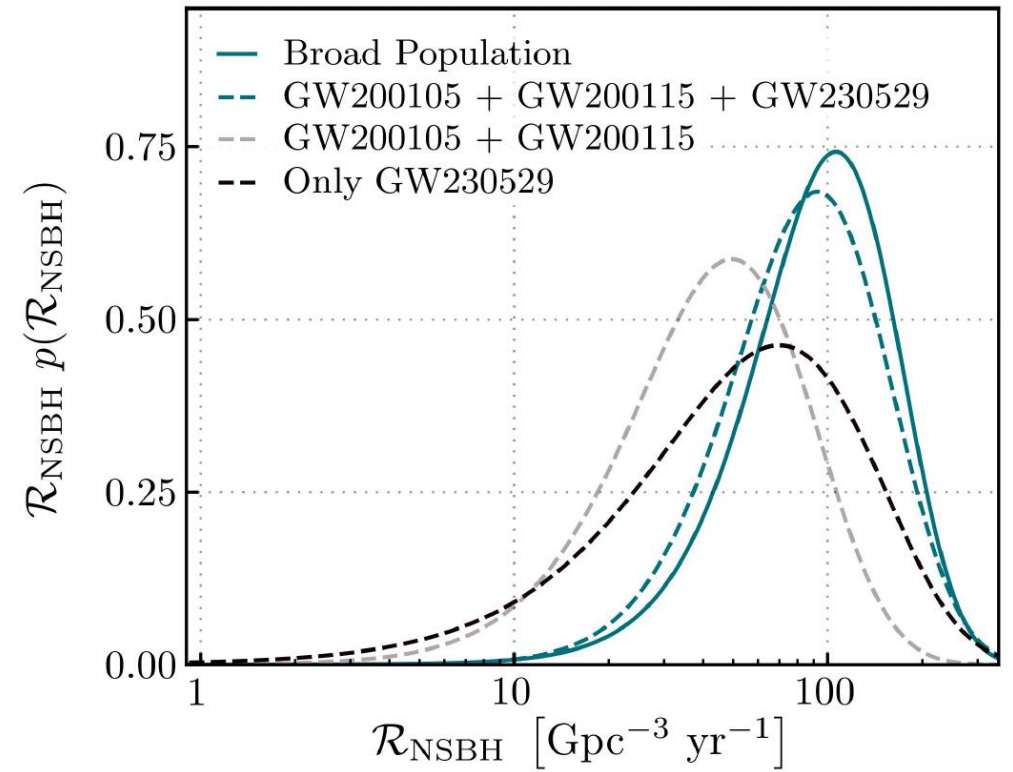
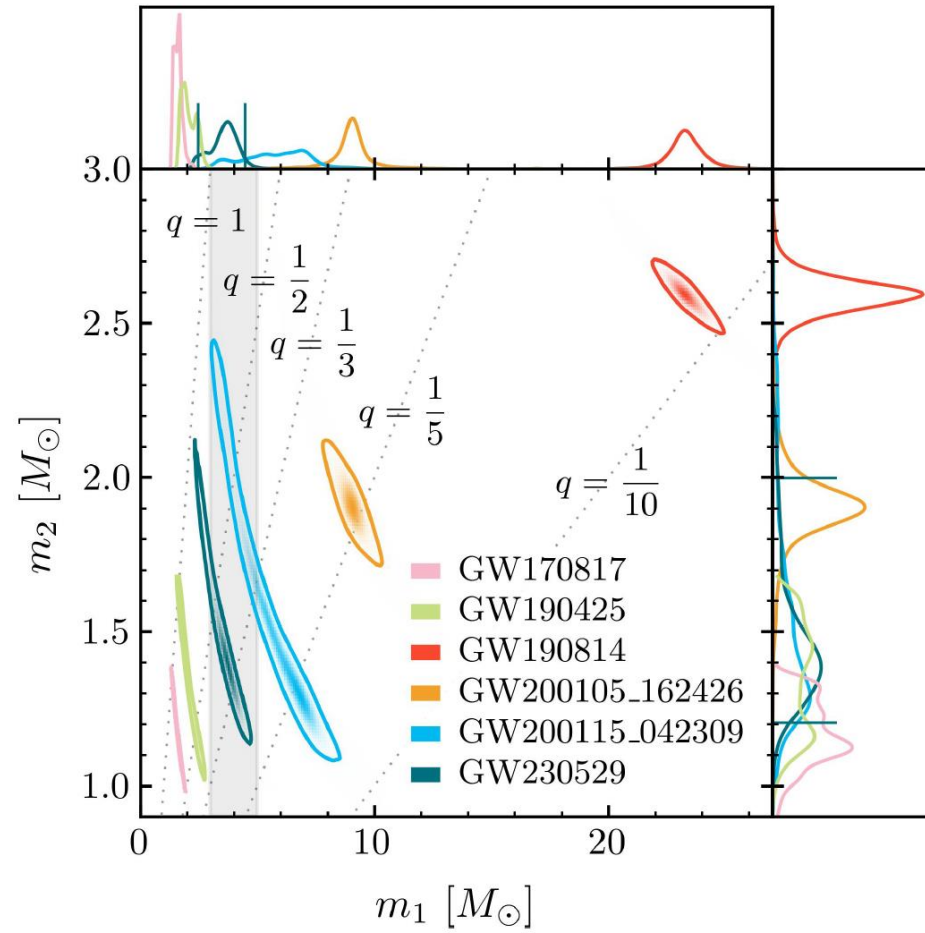


## Higher order modes

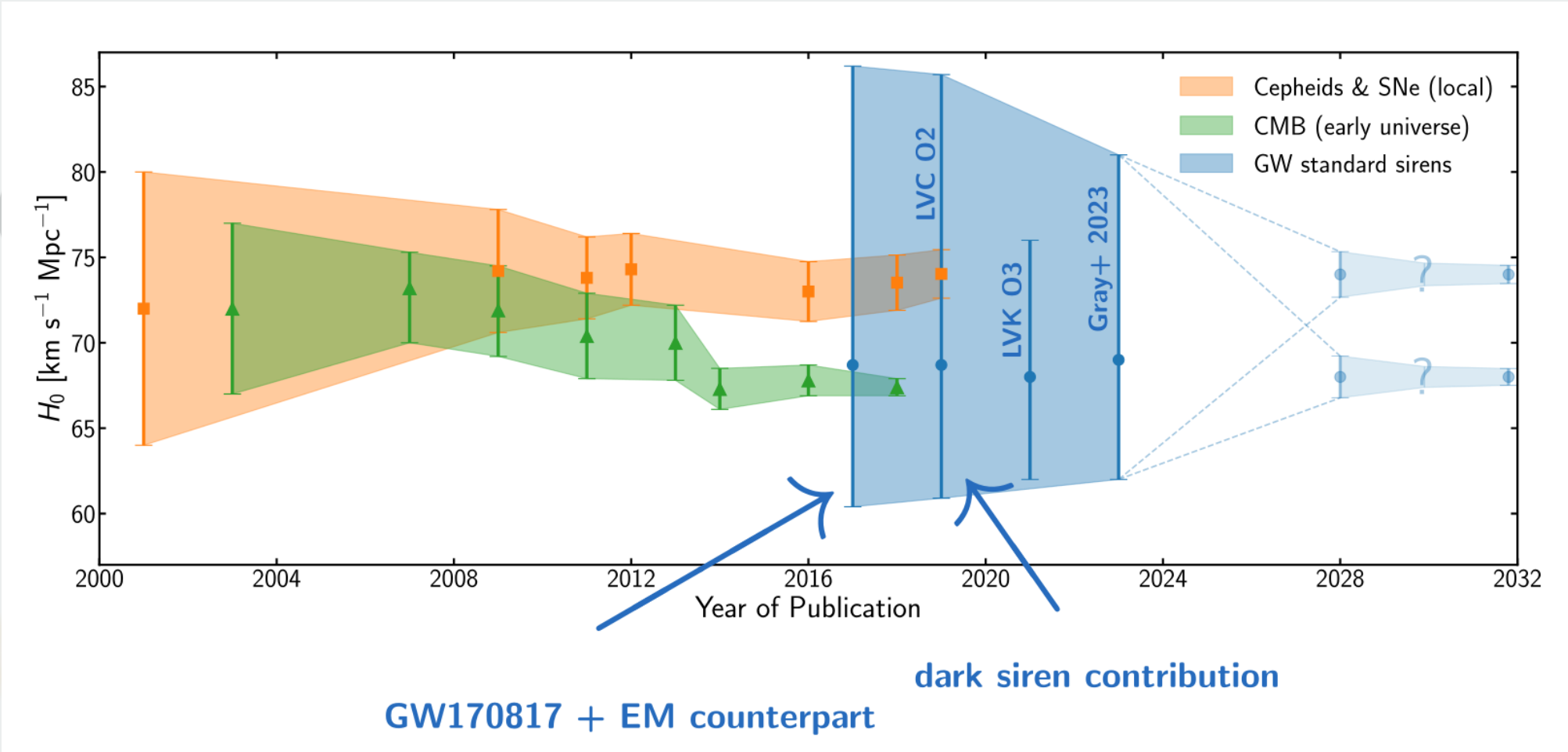




# Observed NSBH population



# Gravitational-wave sirens



Bright sirens

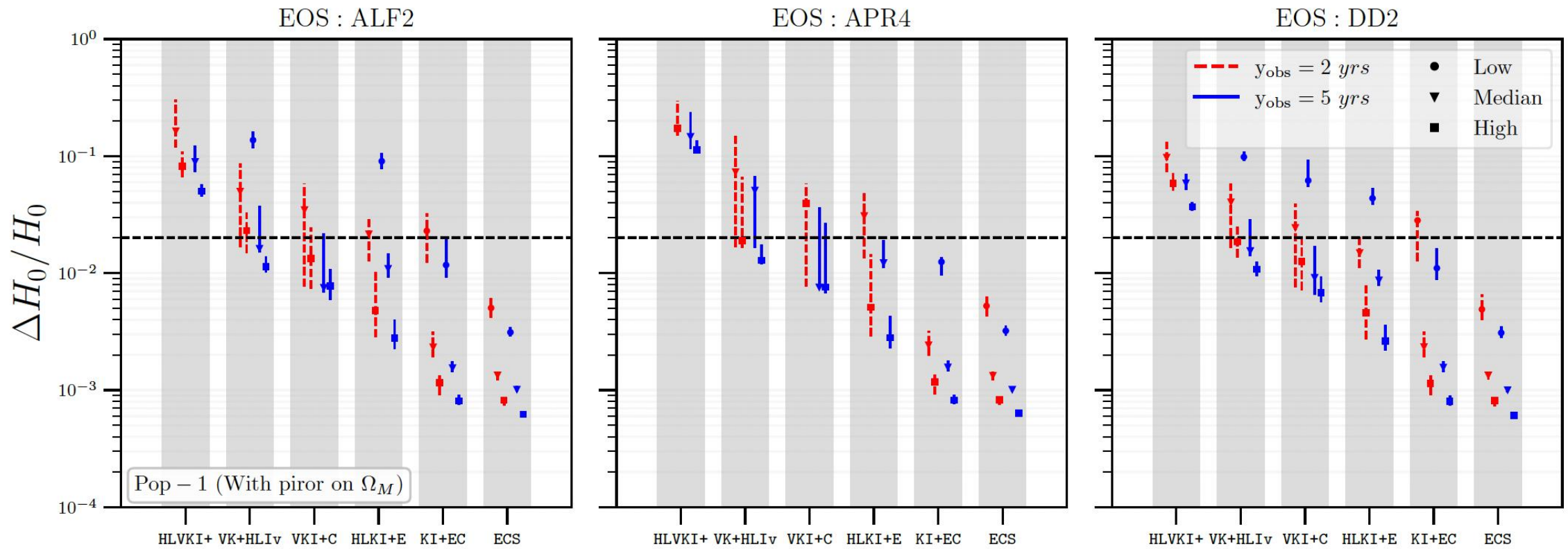
GW170817 + EM counterpart

dark siren contribution

*Current constraints on the Hubble constant with gravitational sirens.*



# Resolving the Hubble tension



## Neutron star spin measurements

Mode	Leading order spin terms
(2, 1)	$\frac{4i}{R} \sqrt{\frac{\pi}{5}} \eta M \tilde{\chi}$
(2, 2)	$\frac{32}{3R} \sqrt{\frac{\pi}{5}} \eta M (\chi_{\text{eff}} - \eta \chi_s)$
(3, 2)	$\frac{32}{3R} \sqrt{\frac{\pi}{7}} \eta^2 M \chi_s$
(3, 3)	$\frac{3i}{2R} \sqrt{\frac{6\pi}{7}} \eta M ((4 - 5\eta)\tilde{\chi} - 14\eta\chi_a)$
(4, 4)	$\frac{256}{9R} \sqrt{\frac{\pi}{7}} \eta M \left[ \left(-\frac{2}{3} + \frac{13}{5}\eta\right) \chi_{\text{eff}} + \frac{2\eta}{5} \left(\frac{1}{3} - 7\eta\right) \chi_s \right]$



Positive spin combinations

$$\chi_{\text{eff}} = \frac{\chi_1 + q \chi_2}{1 + q}$$

$$\chi_s = \frac{\chi_1 + \chi_2}{2}$$

## Neutron star spin measurements

Mode	Leading order spin terms
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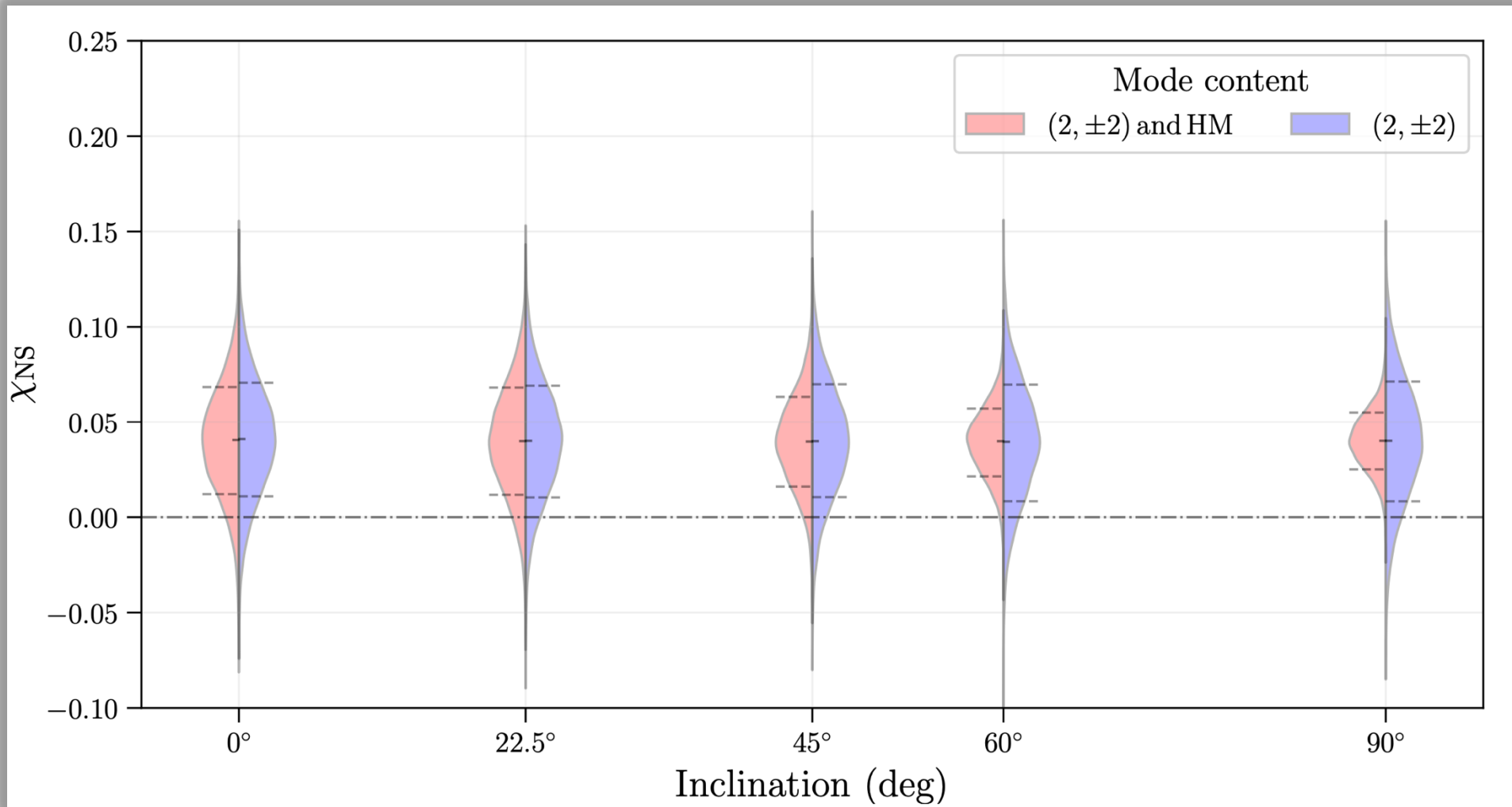


Negative spin combinations

$$\tilde{\chi} = \frac{\chi_1 - q \chi_2}{1 + q}$$

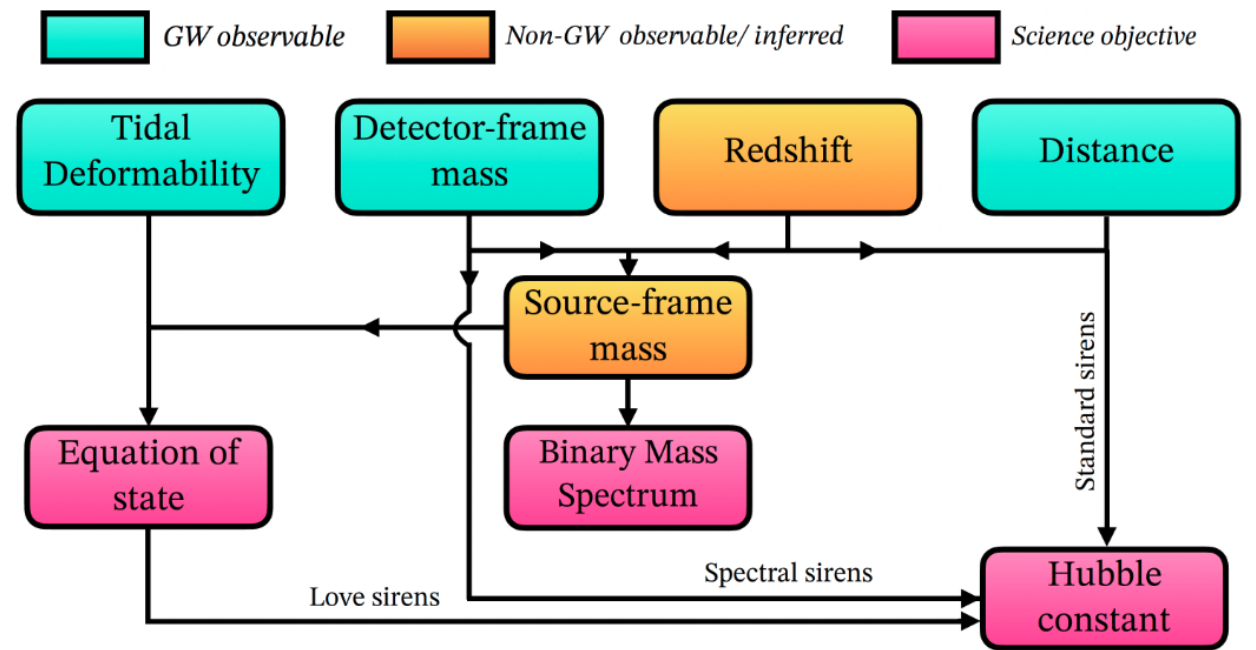
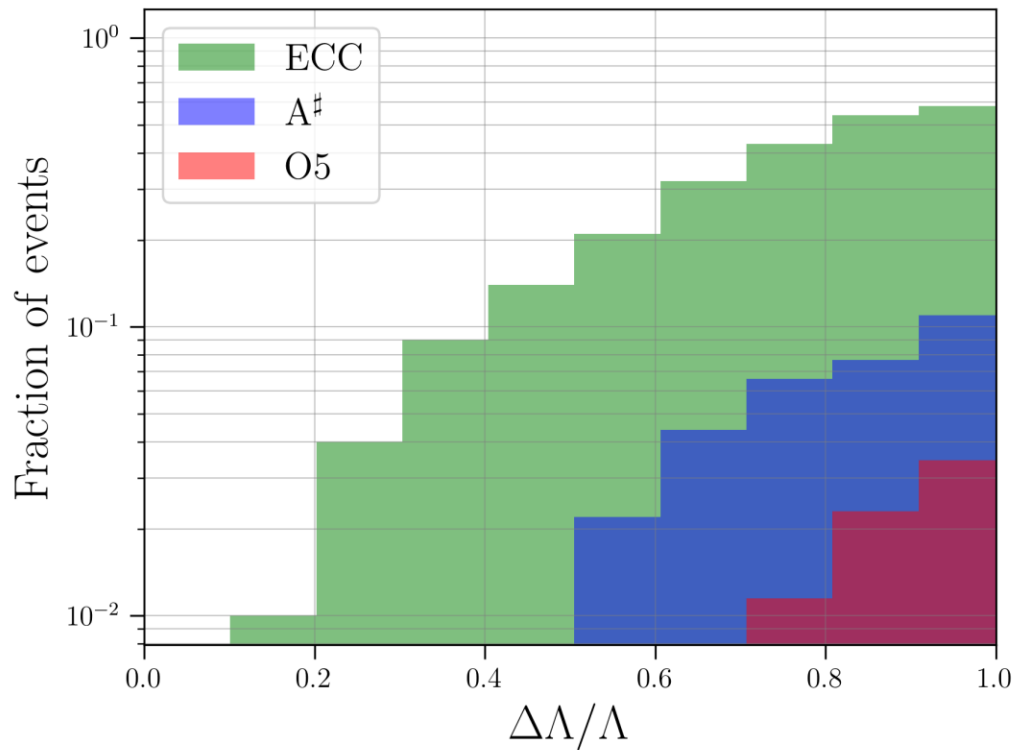
$$\chi_a = \frac{\chi_1 - \chi_2}{2}$$

# Neutron star spin measurements



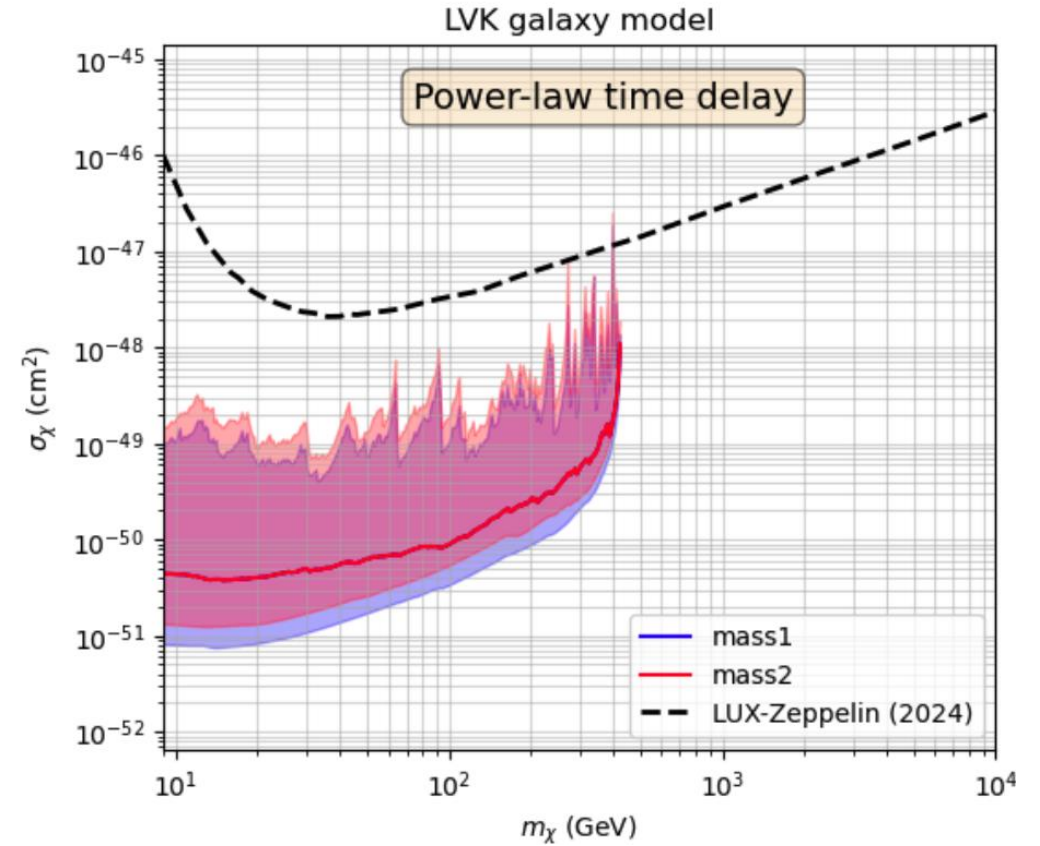
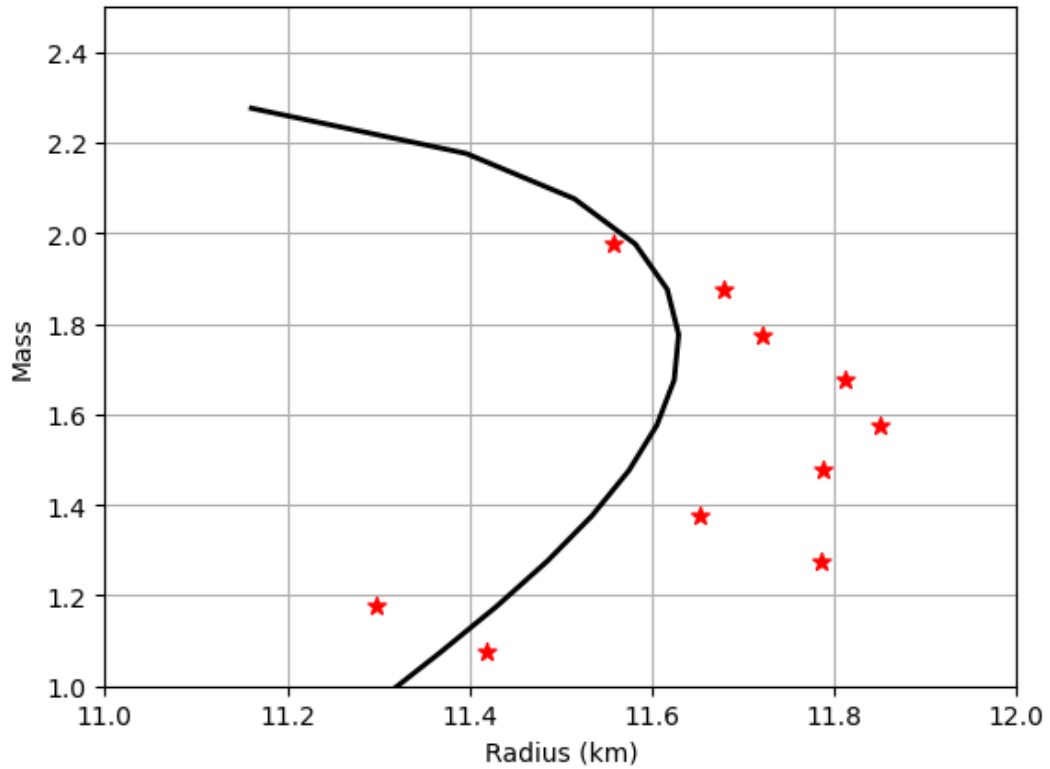
# Comprehensive utilization of neutron star-black hole mergers

Build an infrastructure that jointly infers the binary mass spectrum, the equation of state, and the Hubble constant.



# Neutron stars as dark matter detectors

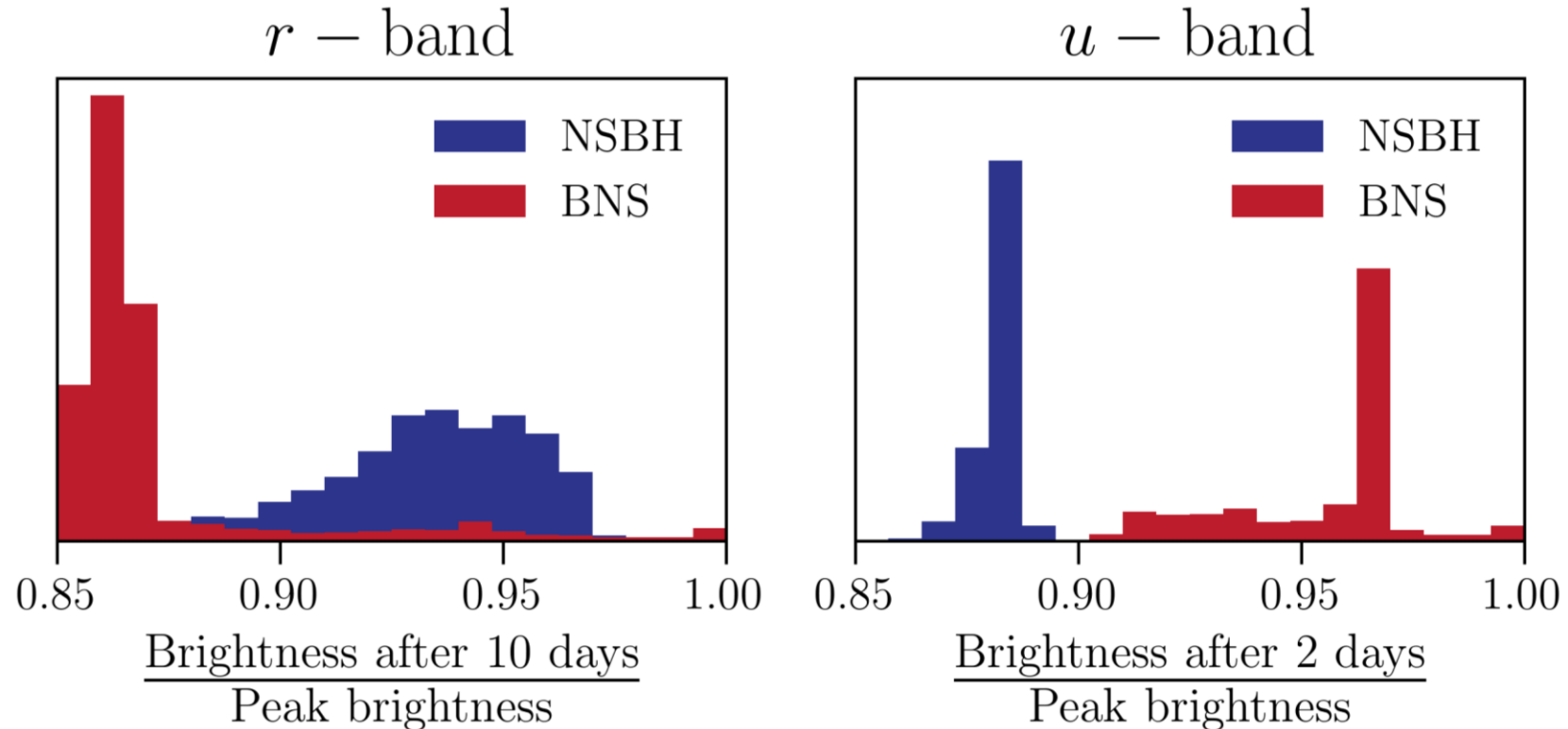
Model realistic levels of dark matter contamination in neutron stars and apply Bayesian model selection.





## The origins of observed kilonovae

Develop a formalism to distinguish between kilonovae from binary neutron stars and neutron star-black hole mergers.

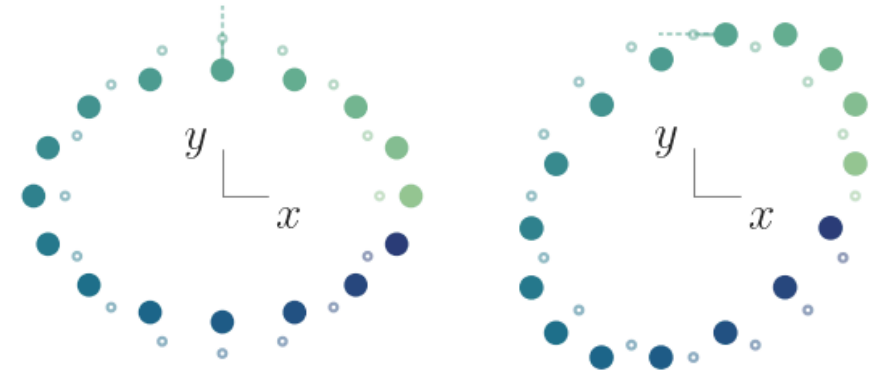


# Gravitational waves

$$h_{ij} = \frac{2G}{c^4} \frac{1}{d} \frac{d^2 Q_{ij}}{dt^2}$$

$$|h_{ij}| = \frac{\Delta L}{L}$$

$$\approx 10^{-22} \left( \frac{100 \text{ Mpc}}{d} \right) \left( \frac{M}{1 M_{\odot}} \right)^{5/3} \left( \frac{\omega}{100 \text{ Hz}} \right)^{2/3}$$



Credit: Max Isi



Credit: SXS



Credit: AAS NOVA

## Detecting gravitational waves

