



# Current and Future Gravitational Wave Detectors

Artist: Eddie Anaya (Cal State Fullerton)

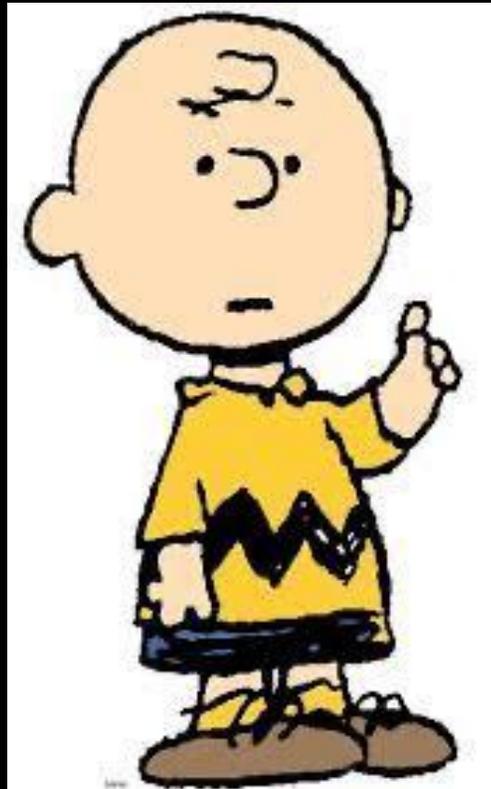
Santa Cruz, CA, July 21/22  
Stefan Ballmer

Sorry for the virtual presence...



# Please do interrupt me with question

- This is your talk
- Zoom makes it hard enough  
So don't hesitate to speak up!

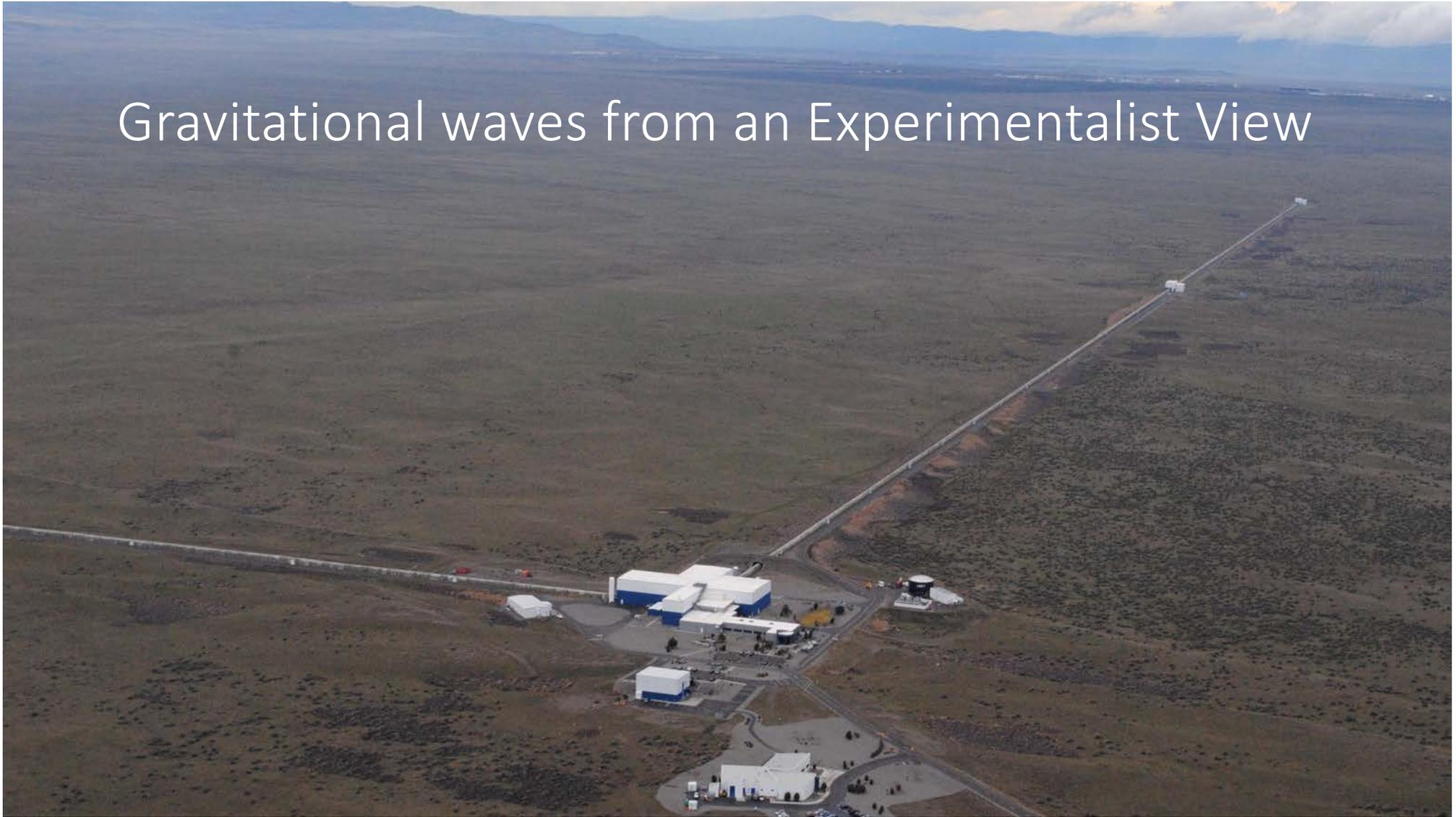


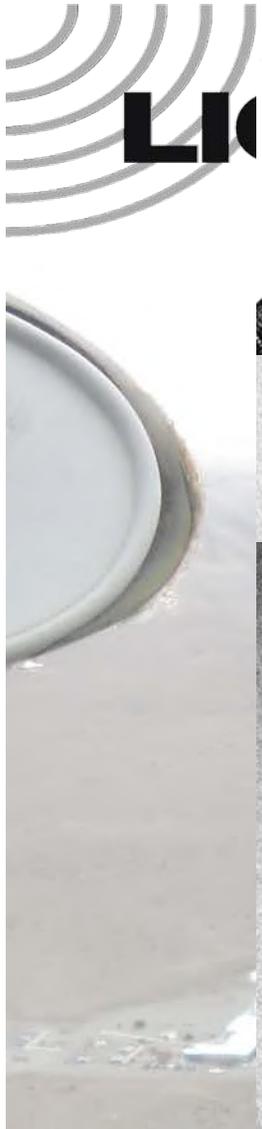
# Outline



- Day 1
  - Gravitational waves from an Experimentalist View
    - History of the field
  - How can you measure them in principle?
    - Scale of effect
    - How to read out such small motions (Classical Shot Noise)
    - How to isolate all other large motion (Seismic isolation, Newtonian noise, Thermal Noise)
  - How is Advanced LIGO doing in O4?
- Day 2
  - Key Technologies for the Future
    - Beyond Quantum Noise (Quantization of EM field, squeezing)
  - Cosmic Explorer: the Next-generation of US GW detectors
- Will not talk about sources
  - See presentations from Jim Lattimer and Neil Cornish for that

# Gravitational waves from an Experimentalist View





697

1916.

XXXIII.

SITZUNGSBERICHTE  
DER  
KÖNIGLICH PREUSSISCHEN  
AKADEMIE DER WISSENSCHAFTEN.



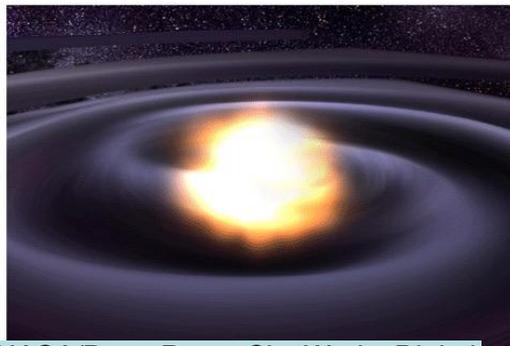
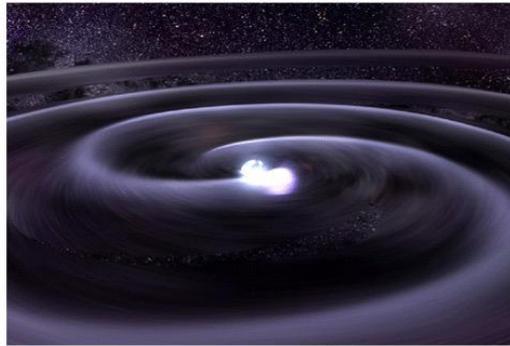
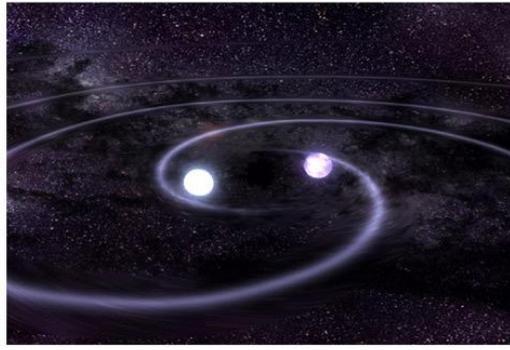
688 Sitzung der physikalisch-mathematischen Klasse vom 22. Juni 1916

AS.A. 311 SCIENCE LIBRARY MIT

Näherungsweise Integration der Feldgleichungen  
der Gravitation.

VON A. EINSTEIN.

“Approximate integration of the field equations of gravitation”



NASA/Dana Berry, Sky Works Digital

# Gravitational Waves Quadrupole Formula



“Curvature of  
Space-Time”

“Matter”

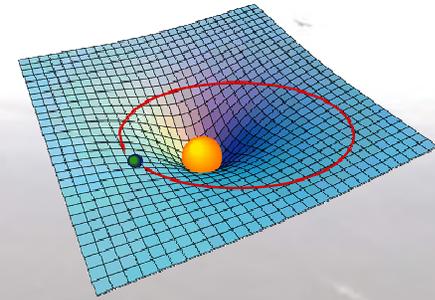
$$G_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$

Linearize

$$-\frac{1}{2}\square\tilde{h}_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$

Emitting source

$$h = \frac{2G}{c^4 r} \ddot{I}$$



I: Quadrupole moment of source

## Über Gravitationswellen.

VON A. EINSTEIN.

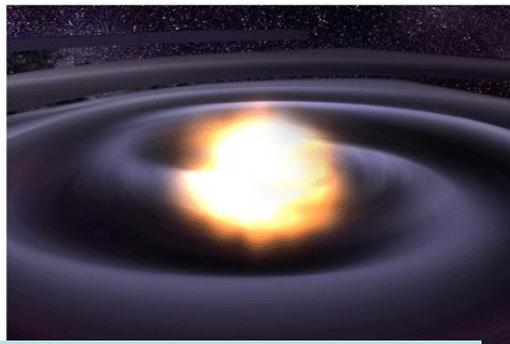
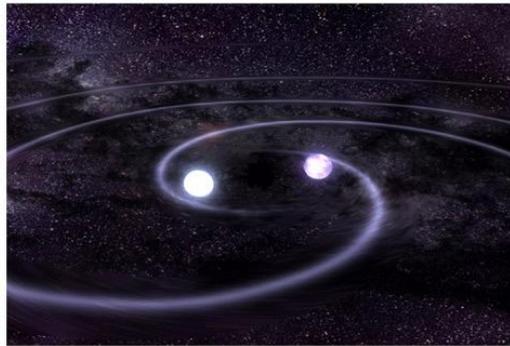
(Vorgelegt am 31. Januar 1918 [s. oben S. 79].)

Die wichtige Frage, wie die Ausbreitung der Gravitationsfelder erfolgt, ist schon vor anderthalb Jahren in einer Akademiearbeit von mir behandelt worden<sup>1</sup>. Da aber meine damalige Darstellung des Gegenstandes nicht genügend durchsichtig und außerdem durch einen bedauerlichen Rechenfehler verunstaltet ist, muß ich hier nochmals auf die Angelegenheit zurückkommen.

Wie damals beschränke ich mich auch hier auf den Fall, daß das betrachtete zeiträumliche Kontinuum sich von einem »galileischen« nur sehr wenig unterscheidet. Um für alle Indizes

“... is disfigured by a regrettable calculation error...”





NASA/Dana Berry, Sky Works Digital

## Signal Amplitude



- For 2  $1.4M_{\text{Sun}}$  Neutron stars, at 1 Mpc (3 million light years):

$$h = \frac{dL}{L} \approx 3 \times 10^{-21}$$



## Signal Amplitude

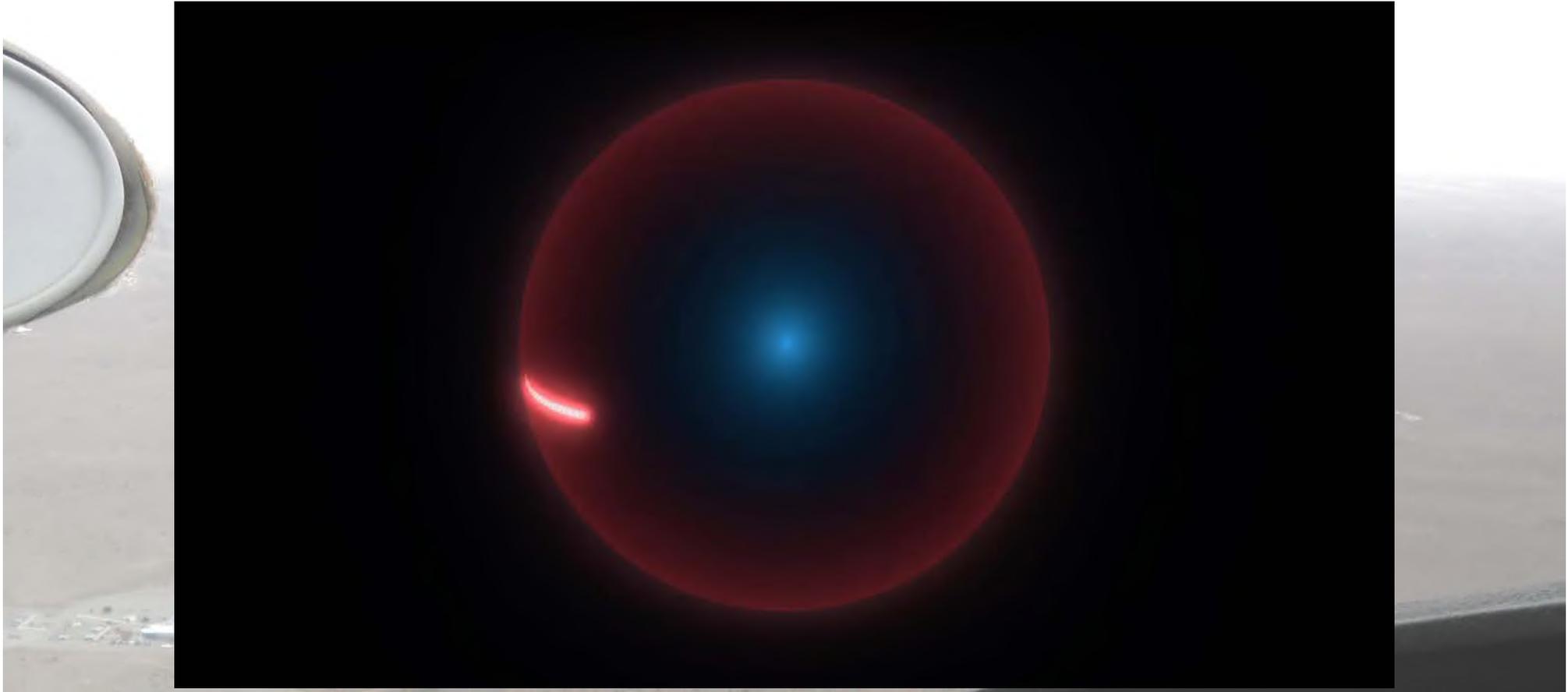


A strain of  $h=3 \times 10^{-21}$  :

- The Center of our Galaxy is  $L=27000\text{lyr}$ :  
 $dL \sim 1 \text{ meter}$
- The nearest star is  $L=4.2$  light years away:  
 $dL \sim 0.1 \text{ millimeter}$
- Over a LIGO arm cavity,  $L=4\text{km}=13\text{usec}$ :  
 $dL \sim 0.01 \text{ femtometer}$



# Signal Amplitude





## Before 1957



“... in all imaginable cases  $A$  must have a practically vanishing value.

ein. Man erhält aus ihm also die Ausstrahlung  $A$  des Systems pro Zeiteinheit durch Multiplikation mit  $4\pi R^2$ :

$$A = \frac{\kappa}{24\pi} \sum_{\alpha\beta} \left( \frac{\partial^3 J_{\alpha\beta}}{\partial t^3} \right)^2. \quad (21)$$

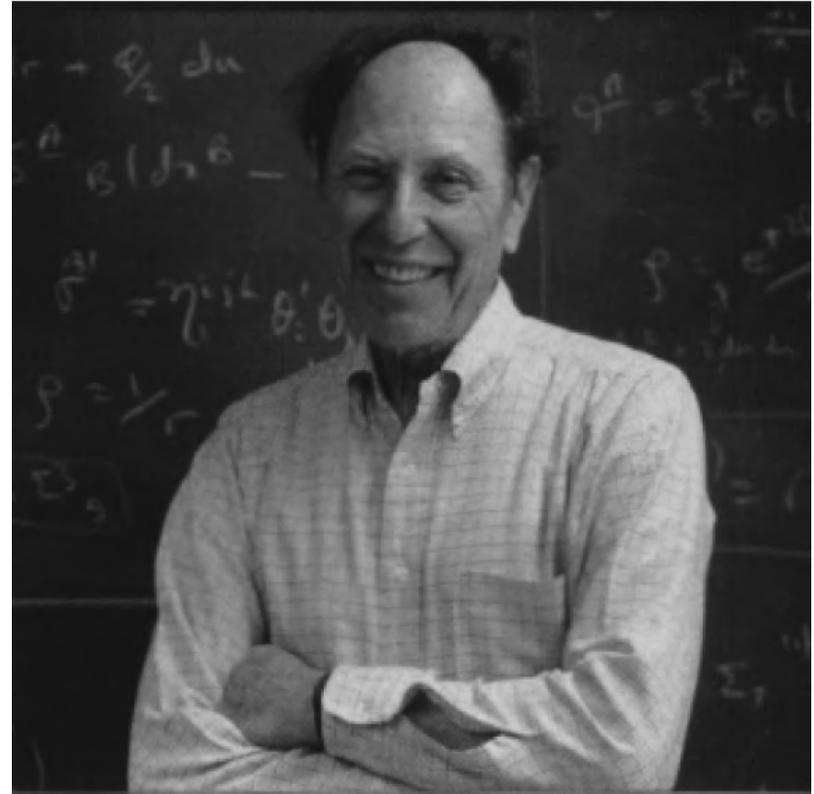
Würde man die Zeit in Sekunden, die Energie in Erg messen, so würde zu diesem Ausdruck der Zahlenfaktor  $\frac{1}{c^4}$  hinzutreten. Berücksichtigt man außerdem, daß  $\kappa = 1.87 \cdot 10^{-27}$ , so sieht man, daß  $A$  in allen nur denkbaren Fällen einen praktisch verschwindenden Wert haben muß.

## Josh Goldberg in 1957

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Josh was working at Wright Patterson AFB. In addition to his own research (searching for anti-gravity?), he was the funding officer for the USAF's support for research in relativity.

Josh made it possible for relativity to thrive worldwide.



Josh Goldberg, Syracuse University



## The Chapel Hill Conference

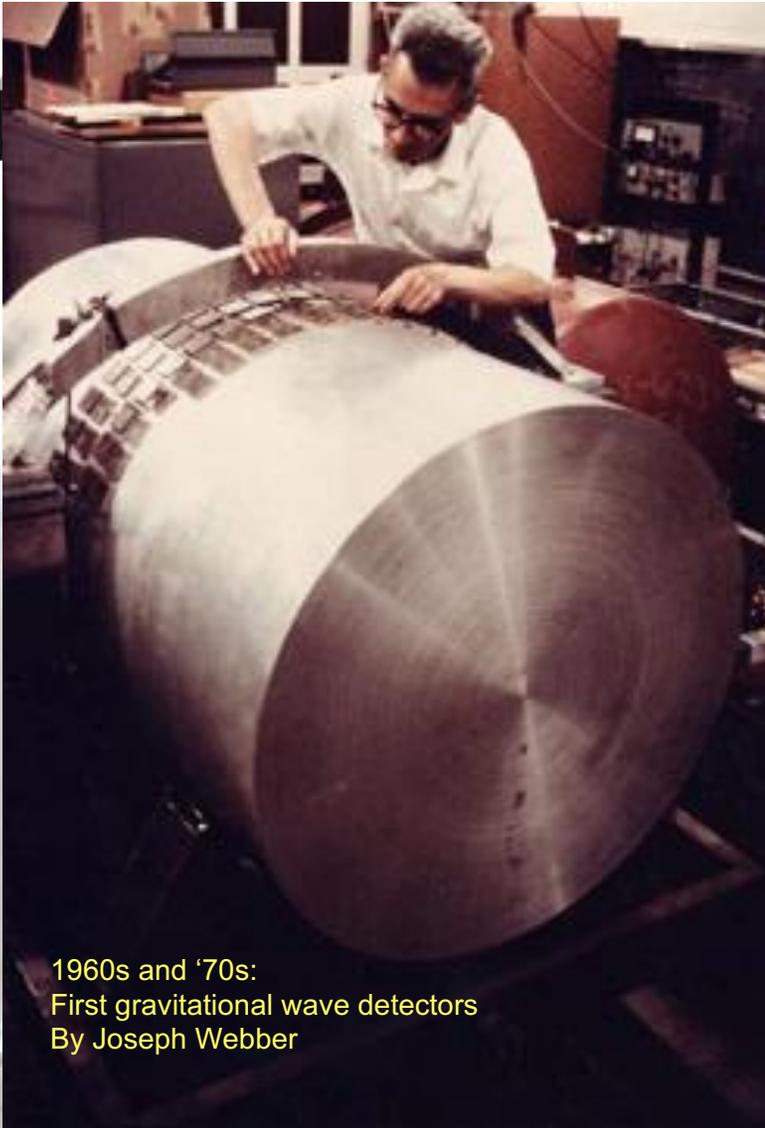


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In January 1957, Josh sponsored the Conference on the Role of Gravitation in Physics, a.k.a. the Chapel Hill Conference, a.k.a. GR1. The organizers were Bryce and Cecile DeWitt. 44 of the world's leading relativists attended.

Much of the future of gravitational physics was launched then. (Numerical relativity was prefigured in a remark by Charles Misner.)

The "gravitational wave problem" was solved there, and the quest to detect gravitational waves was born.



1960s and '70s:  
First gravitational wave detectors  
By Joseph Webber



This Resonant Bar  
Gravitational-Wave Antenna,  
developed by Professor Joseph Weber,  
is a gift from the  
University of Maryland





## 1972: Gravitational Wave Antenna

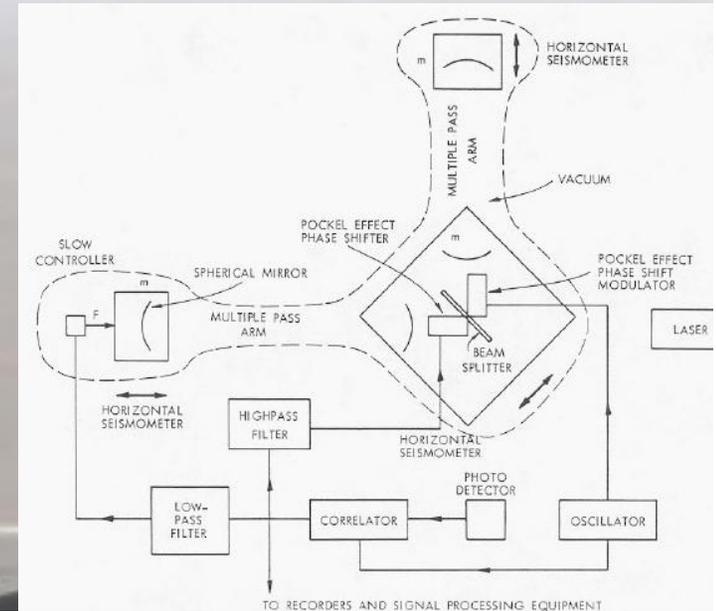
- Electromagnetically coupled broad-band gravitational wave antenna, R.Weiss, MIT RLE QPR 1972



1972

2017

- Use a laser to compare the length of the interferometer arms!





# MIT Research Laboratory of Electronics Quarterly Progress Report 1972



The discovery of the pulsars may have uncovered sources of gravitational radiation which have extremely well-known frequencies and angular positions. The fastest known pulsar is NP 0532, in the Crab Nebula, which rotates at 30.2 Hz. The gravitational flux incident on the Earth from NP 0532 at multiples of 30.2 Hz can be  $10^{-6}$  erg/cm<sup>2</sup>/s at most. This is

The antenna arms can be made as large as is consistent with the condition that the travel time of light in the arm is less than one-half the period of the gravitational wave that is to be detected. This points out the principal feature of electromagnetically coupled antennas relative to acoustically coupled ones such as bars; that an electromagnetic antenna can be longer than this acoustic counterpart in the ratio of the speed of light to the speed of sound in materials, a factor of  $10^5$ . Since it is not the strain but rather the differential displacement that is measured in these gravitational antennas, the proposed antenna can offer a distinct advantage in sensitivity relative to bars in detecting both broadband and single-frequency gravitational radiation. A significant improvement in thermal noise can also be realized.



# Relativistic Binary Pulsar B1913+16

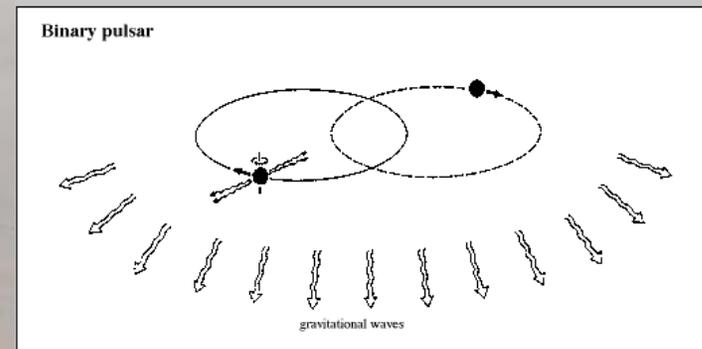
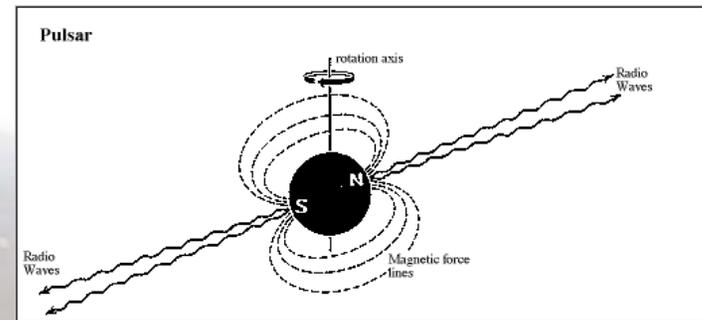


R. A. Hulse

J. H. Taylor



- First binary Pulsar
  - Spinning neutron star with radio beacon
- Discovered in 1974
- Loses energy by radiating gravitational waves



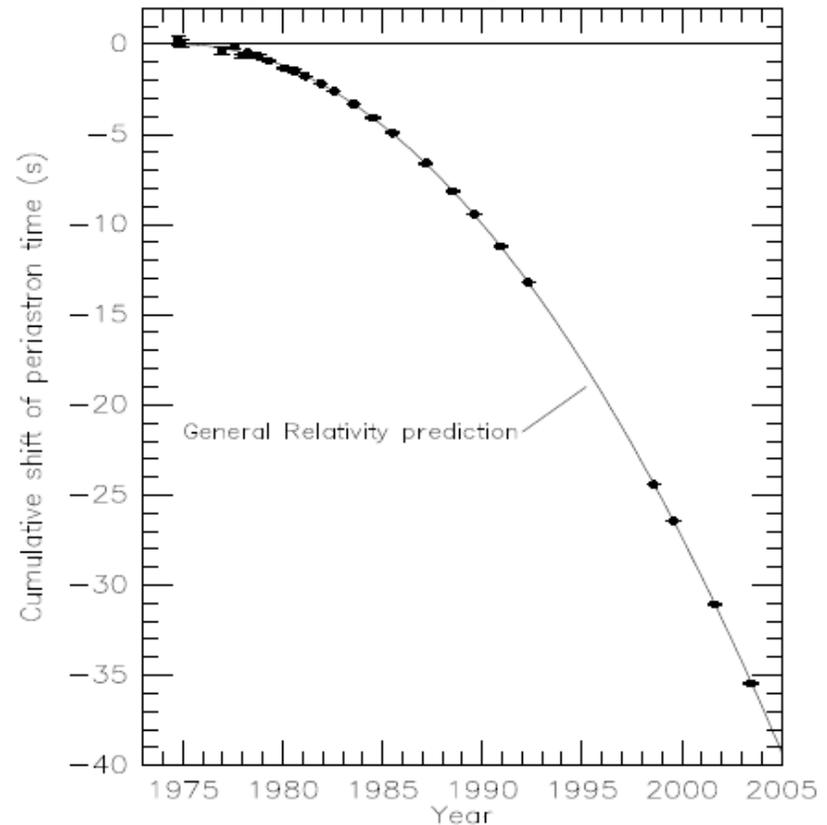


# Relativistic Binary Pulsar B1913+16



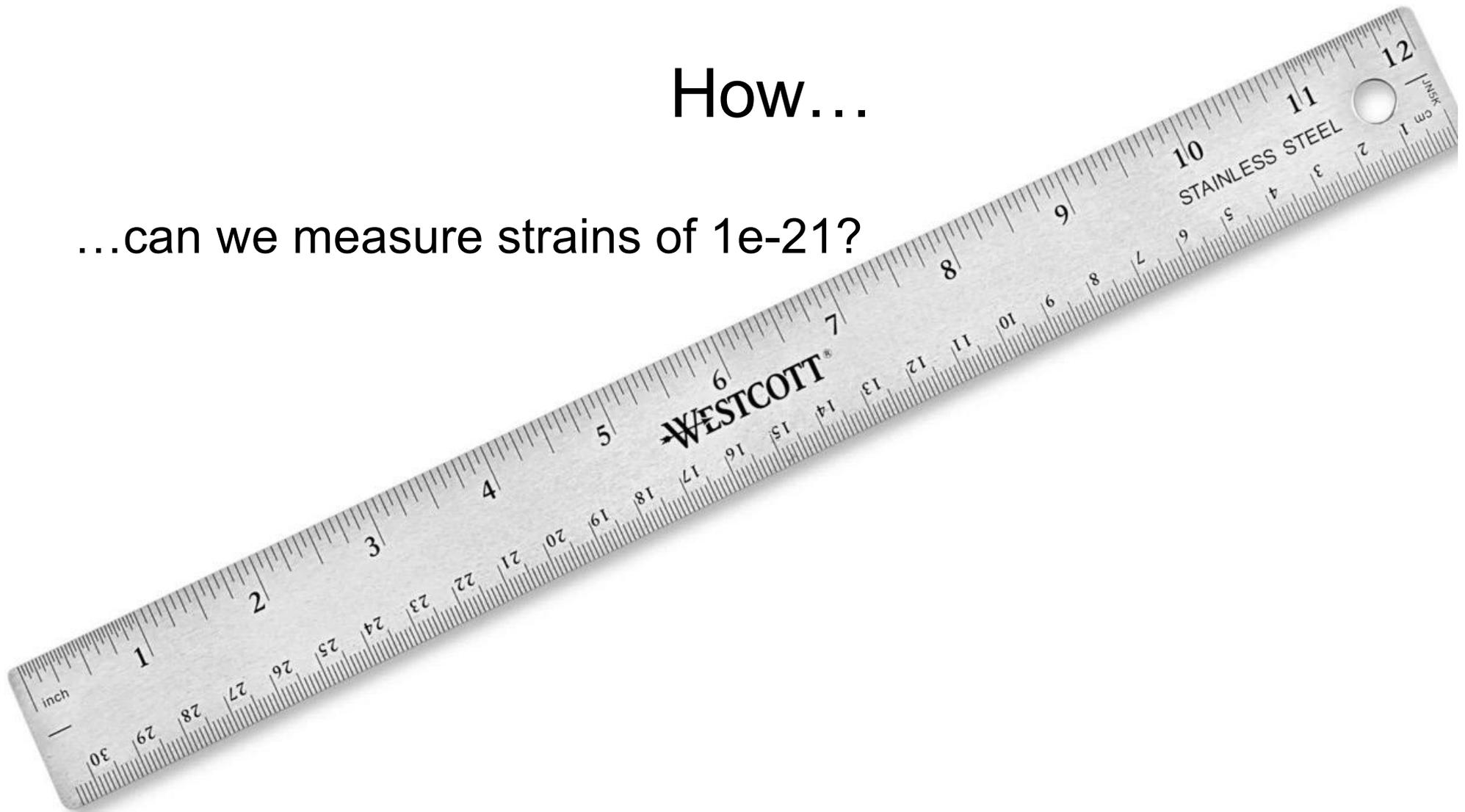
- Nobel prize in 1993
- Orbital parameters measured for 30yr!
- Energy loss agrees with GW emission
- Standard source for GW observatories
  - Merges in 300Myr

Weisberg, Taylor, arXiv:astro-ph/0407149



How...

...can we measure strains of  $1e-21$ ?





# The wave's field

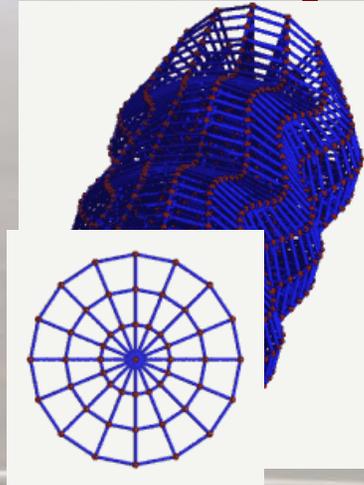


- “Ripples in Space-Time”

Amplitude:

$$dL/L = h$$

- Measureable effect:
  - Stretches/contracts distances perpendicular to propagation



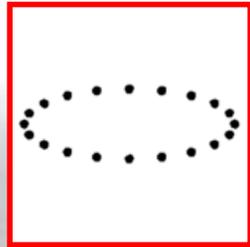
Wave propagation



# The wave's field

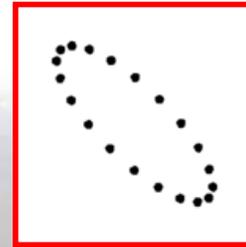


- 2 polarizations:



+ polarization

$$ds^2 = (1 + h)dx^2 + (1 - h)dy^2$$



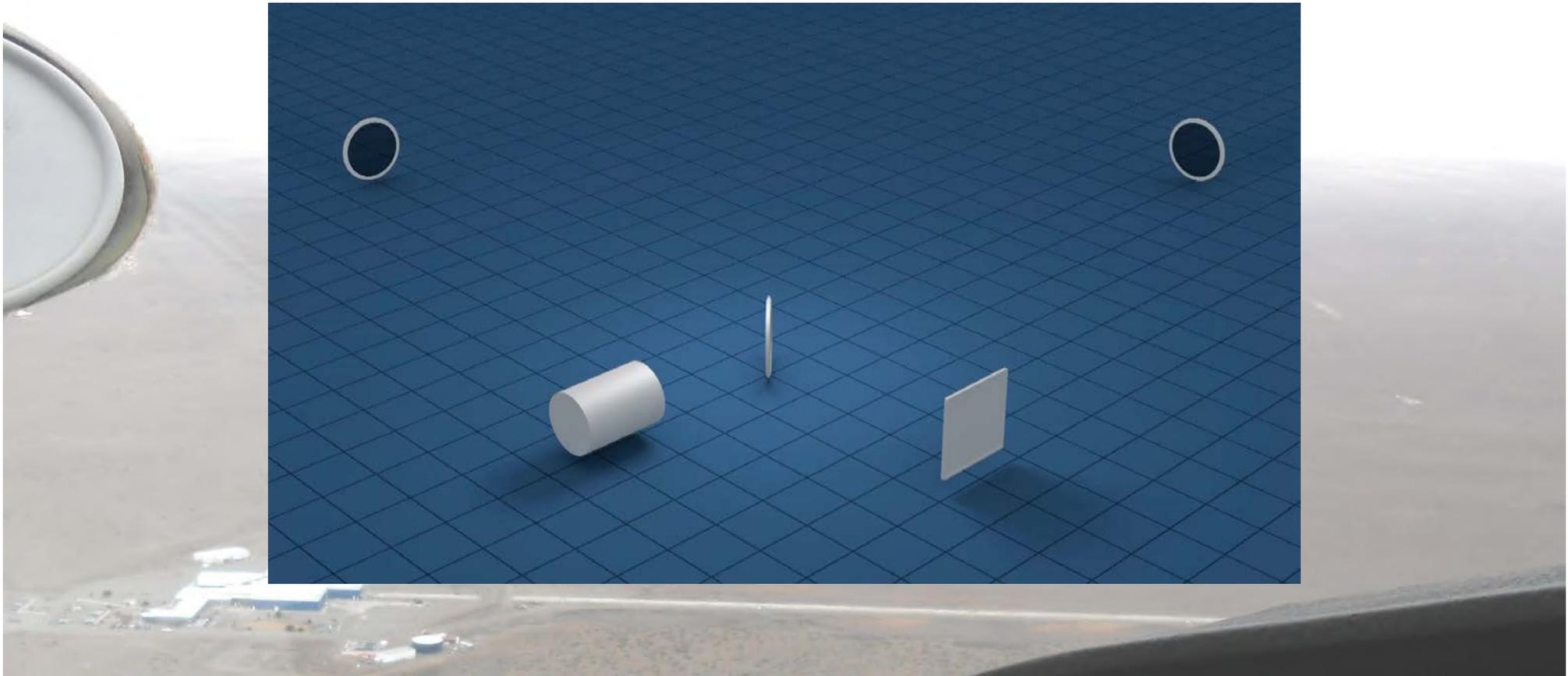
x polarization

$$ds^2 = dx^2 + dy^2 + 2hdx dy$$

- Note:  
Test particles remain at rest -  
only their separation changes!



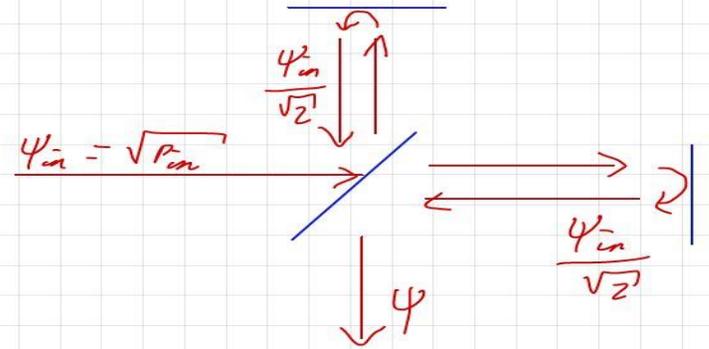
# The interferometer



## Michelson interferometer shot noise

$$\psi = \frac{\psi_{in}}{2} (e^{ik_0L} - e^{-ik_0L})$$

$$= i \psi_{in} \sin k_0L$$



$$P = |\psi|^2 = P_{in} \sin^2 k_0L = P_{in} \frac{1 - \cos 2k_0L}{2}$$

Differential Arm Length (DARM):

$$\Delta L = L_x - L_y$$

- $2k_0L = 0 \pmod{2\pi} \Rightarrow$  Dark fringe (A)
- $2k_0L = \frac{\pi}{2} \pmod{2\pi} \Rightarrow$  Half fringe (B)
- $2k_0L = \pi \pmod{2\pi} \Rightarrow$  Bright fringe (C)

Somewhere else (D)

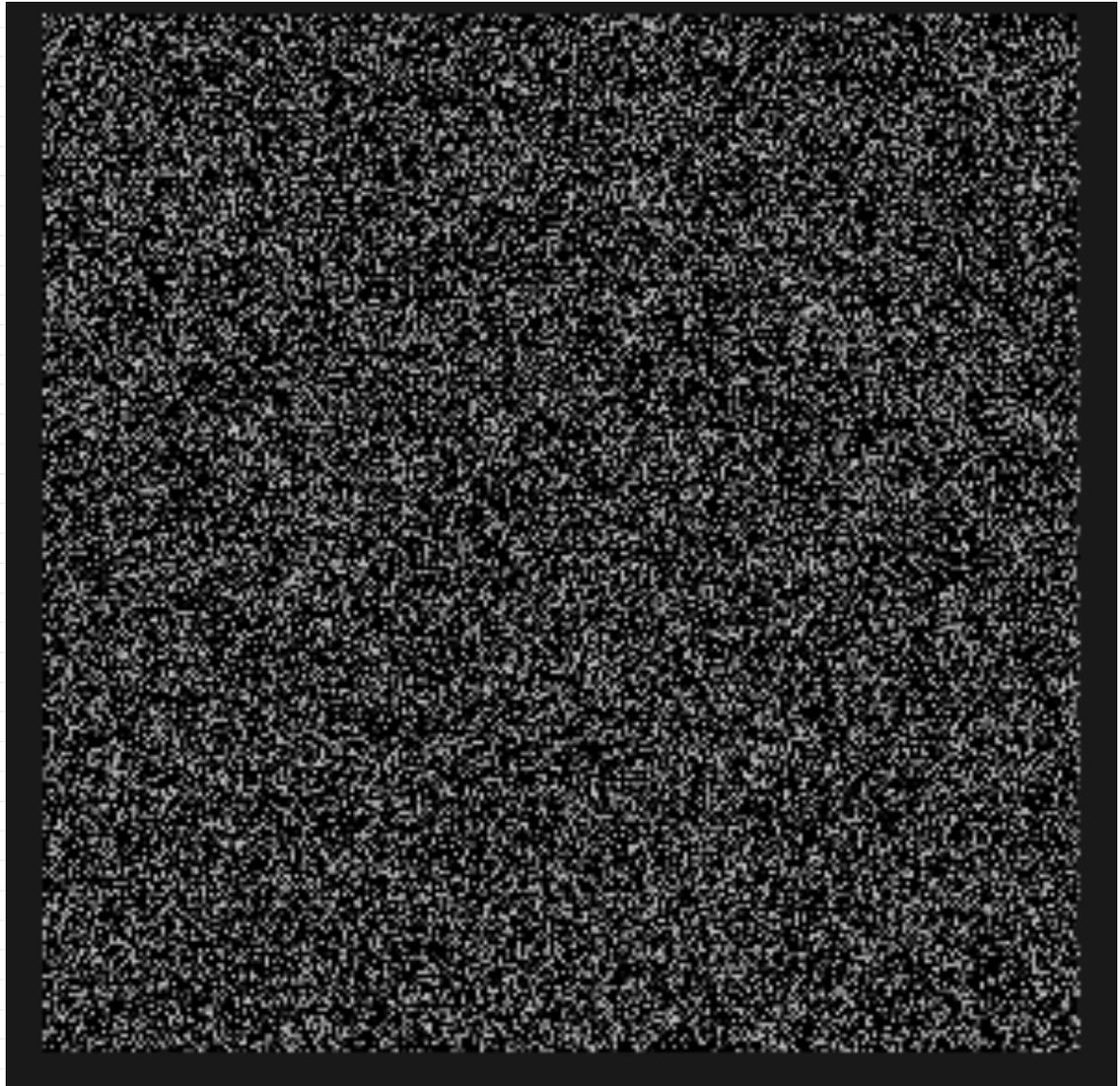
**Where should we operate?**

$$\frac{dP}{dL} = P_{in} k_0 \cdot \sin 2k_0L$$

$$= P_{in} k_0 \cdot 2 \cdot \sin k_0L \cdot \cos k_0L$$

# Measuring Power

- Interferometer translates **length fluctuations** into **laser power fluctuations**
- What is the limit on how precisely we can measure laser power?
- Light is quantized
  - Shot noise!



## Shot noise (classical)

Random photon arrival times  $t_j$  :  
Pulse train  $p(t)$ :

$$p(t) = \sum_{j=1}^N A \delta(t - t_j)$$

$N$ : Number of quanta

$A$ : Unit of quanta

$T$ : observation time

$$n = \langle p(t) \rangle = \frac{NA}{T} \quad \text{rate} \quad \left\{ \begin{array}{l} \text{Watts} \\ \text{Ampere} \\ \text{quanta/sec} \end{array} \right.$$

Note: Fourier transform of  $\delta$ -function  $\propto e^{-i2\pi f t_j}$

$t_j$  are random  $\implies$  phases are random and will average out  $\implies$  power spectrum will be white  $S_p(f) = \text{const}(in f)$

Auto-correlation function:

$$R_{pp}(\tau) = \frac{1}{T} \int_{-T/2}^{T/2} dt p(t) p(t+\tau) = \frac{1}{T} \sum_{j=1}^N \sum_{k=1}^N A^2 \delta(t_j - t_k + \tau)$$

Power spectral density is the Fourier transform of the Auto-correlation function:

$$\begin{aligned} S_{pp}^{2\text{-sided}}(f) &= \int R_{pp}(\tau) e^{-2\pi i f \tau} d\tau = \frac{A^2}{T} \sum_{j=1}^N \sum_{k=1}^N e^{-2\pi i f (t_j - t_k)} \\ &= \frac{A^2}{T} \left[ \underbrace{\sum_{j=1}^N e^0}_{N} + \sum_{j=1}^N \sum_{\substack{k=1 \\ k \neq j}}^N e^{-2\pi i f (t_j - t_k)} \right] = \frac{A^2}{T} N = n A \end{aligned}$$

$\downarrow t_j \text{ random}$   
 $0$

One-sided PSD (only positive frequencies):

$$S_{pp}^{1\text{-sided}}(f) = 2 n A$$

$\implies$

Amplitude Spectral Density:

$$S_p^{1\text{-sided}}(f) = \sqrt{2 n A}$$



Quanta shot noise:

$$S_n(f) = \sqrt{2 n I}$$

$n$ : Rate ( $\frac{\text{quanta}}{\text{sec}}$ )

Laser power shot noise:

$$S_p(f) = \sqrt{2 P R \nu}$$

$P$ : Power (Watt)

Photo current shot noise:

$$S_I(f) = \sqrt{2 I e}$$

$I$ : Current (Ampere)

## Shot noise

$$S_p(f) \sqrt{2 P R v} = \sqrt{2 P_{in} R v} \sin k a L$$

$$= S_L(f) = S_p(f) \frac{d a L}{d P} = \frac{\sqrt{2 P_{in} R v} \sin k a L}{P_{in} k \cdot \sin 2 k a L}$$

$$= \frac{\lambda}{\pi} \sqrt{\frac{2 h \nu}{P_{in}}} \cdot \frac{1}{\cos k a L}$$

$k = \frac{2\pi}{\lambda}$

Wave length is  
the meter stick

Scales with  $P_{in}^{-1/2}$

Operate close to  
the dark fringe

$$\nu \propto \frac{1}{\lambda}$$

$\Rightarrow$  Scales with  $\sqrt{\lambda}$

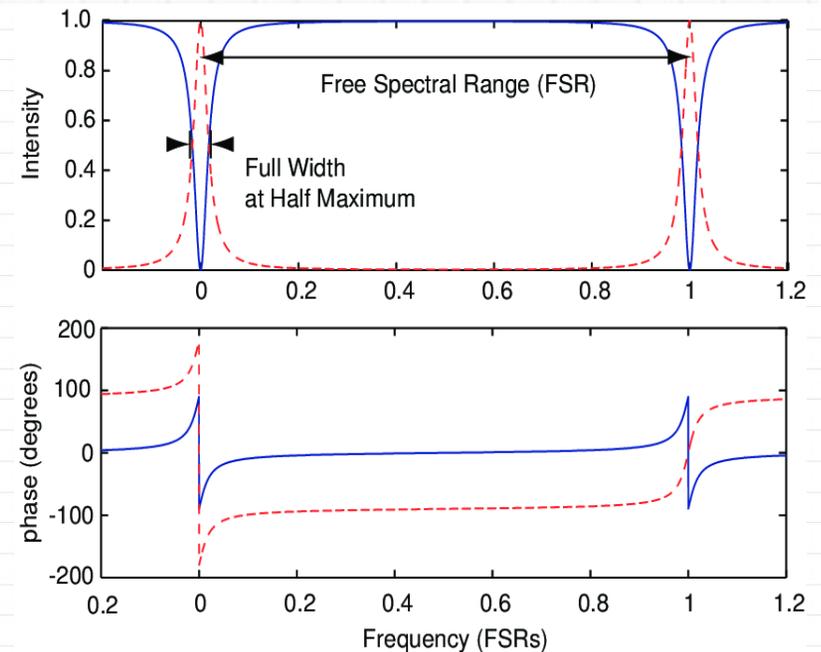
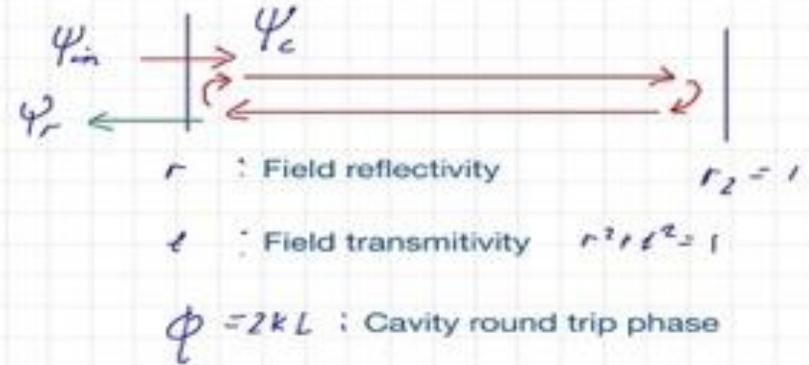
# Arm Length

- At DC:  $dx = L h$
- But  $h(t)$  changes → if  $L$  is too long, the **interrogation time** is too long, and we start averaging. Roughly at  $L = \lambda/4$
- At 100Hz:  $\lambda/4 = 750\text{km}$
- At 1kHz:  $\lambda/4 = 75\text{km}$
- No easy way to adjust effective length



# Arm Cavities

- Instead of extremely long arm we can use a **partially reflective input mirror (ITM)** in the arm  
→ Fabry-Perot cavities
- **Enhances phase sensitivity**
- **Allows for shorter arms**
- **Interrogation time set by input mirror (and signal extraction mirror...)**
- **But increases mirror thermal noise (more on that later)**



## Fabry-Perot arm cavities

$$\begin{aligned} \psi_c &= r e^{i\phi} \psi_c + t \psi_{in} \\ \psi_r &= t e^{i\phi} \psi_c - r \psi_{in} \end{aligned}$$

$$\Rightarrow \psi_c = \frac{t}{1 - r e^{i\phi}} \psi_{in}$$

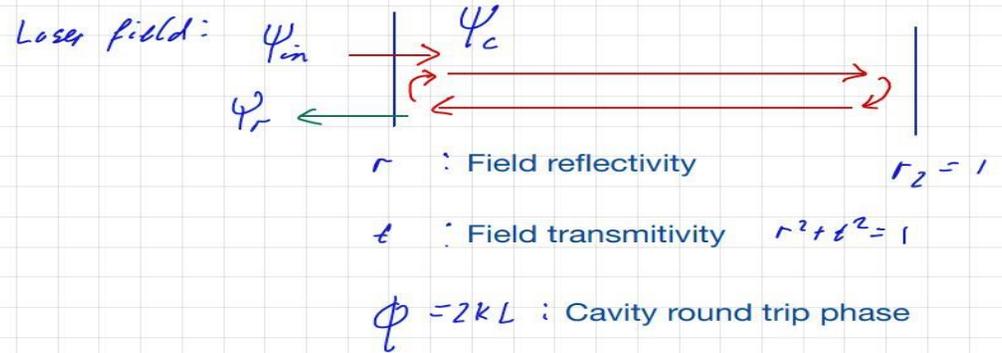
$$\phi \approx 0: \psi_r = \frac{t^2 \cdot (1 + i\phi)}{1 - r - i r \phi} \psi_{in} - r \psi_{in}$$

$$= \frac{1 - r^2}{1 - r} \frac{1 + i\phi}{1 - i \frac{r}{1-r} \phi} \psi_{in} - r \psi_{in}$$

$$\sim (1+r) \left[ 1 + i\phi \left( \frac{1}{1-r} \right) \right] \psi_{in} - r \psi_{in}$$

$$= \left( 1 + i\phi \frac{1+r}{1-r} \right) \psi_{in}$$

$$\sim e^{i \frac{1+r}{1-r} \phi} \psi_{in}$$



$\Rightarrow$  Phase enhancement by:

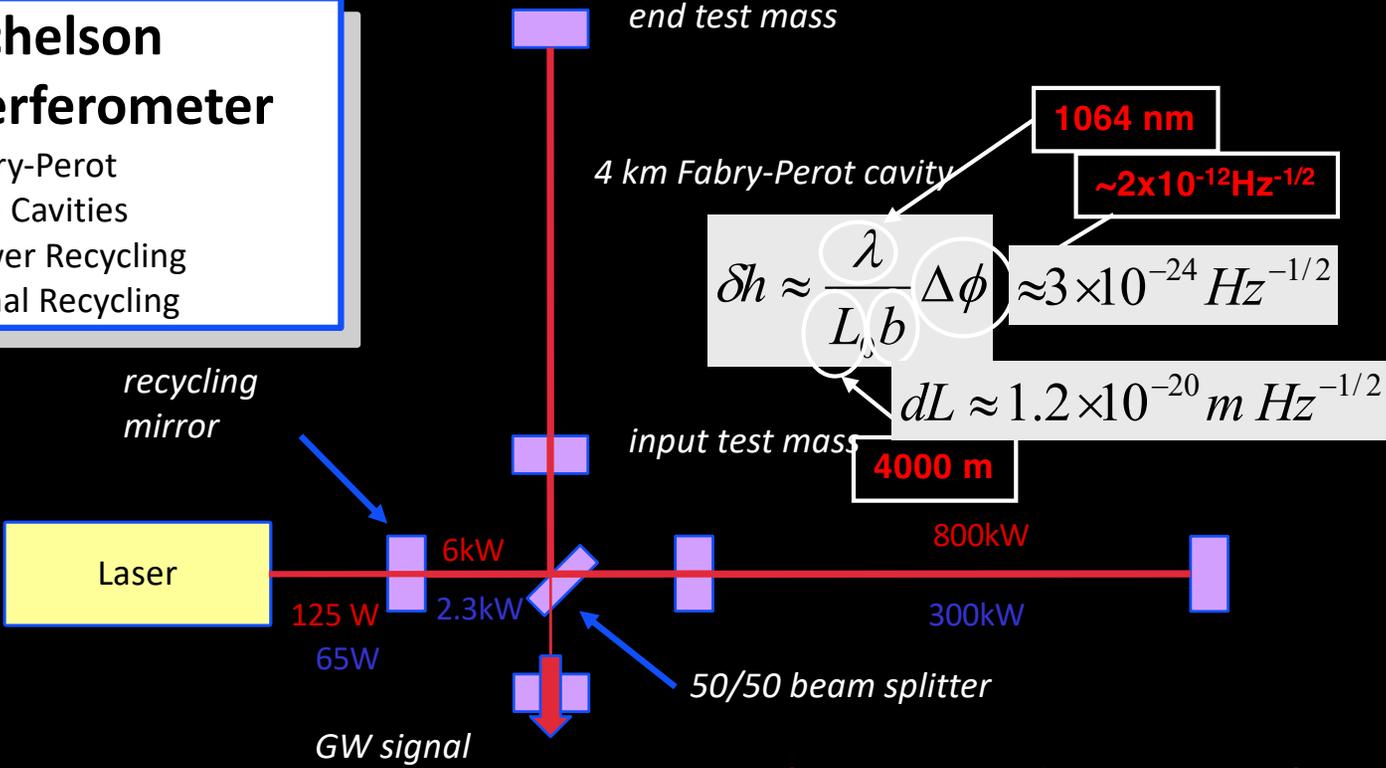
$$\Delta \left( \frac{\psi_r}{\psi_{in}} \right) = \frac{1+r}{1-r} \phi$$

$$\approx \frac{1+r}{1-r} 280 \phi$$

# Interferometer Sensitivity

**Michelson Interferometer**

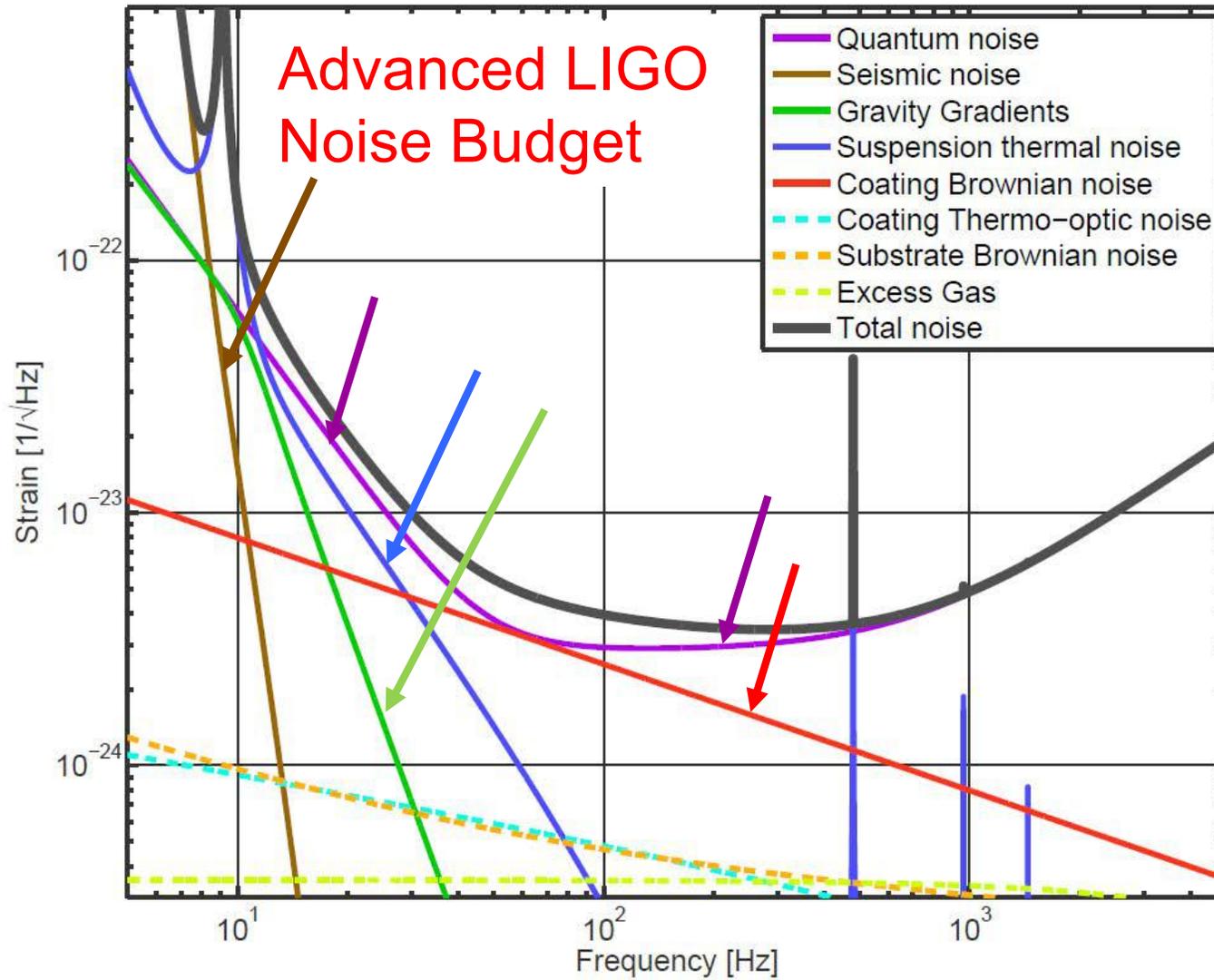
- + Fabry-Perot Arm Cavities
- + Power Recycling
- + Signal Recycling



$$\delta h \approx \frac{\lambda}{L_s b} \Delta \phi \approx 3 \times 10^{-24} \text{ Hz}^{-1/2}$$

$$dL \approx 1.2 \times 10^{-20} \text{ m Hz}^{-1/2}$$

(Numbers: Red: for aLIGO design)  
( Blue: for aLIGO 2022)

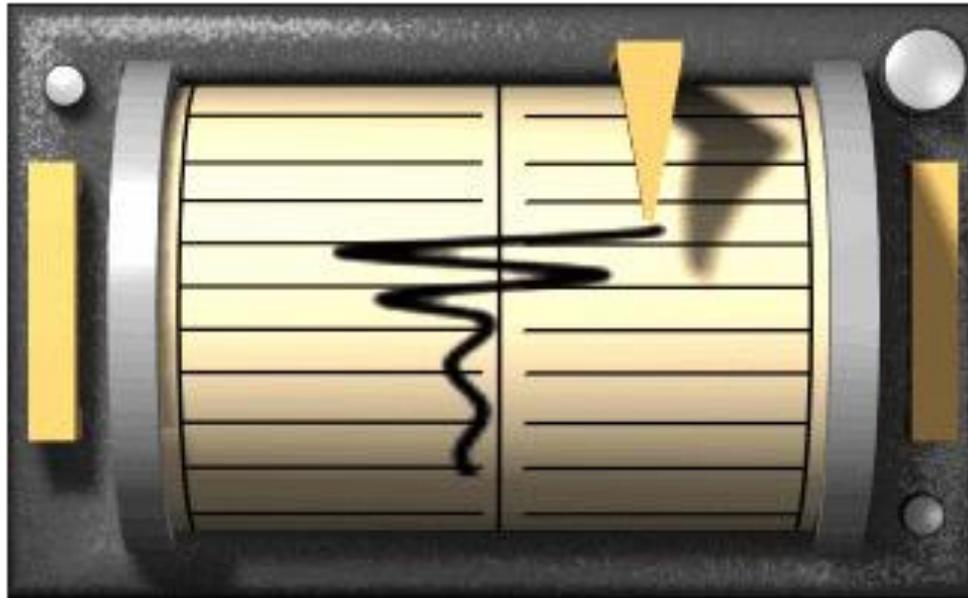




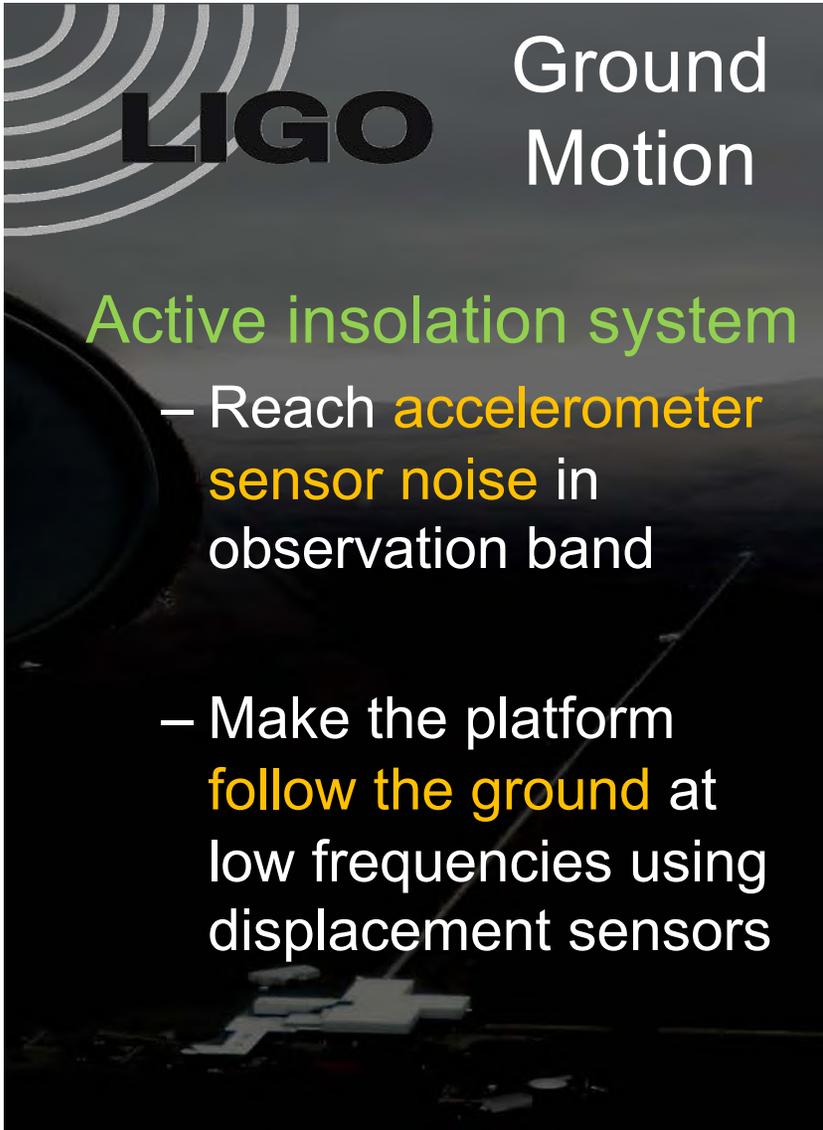
How...



...do we isolate from any other motion?



Seismic Noise

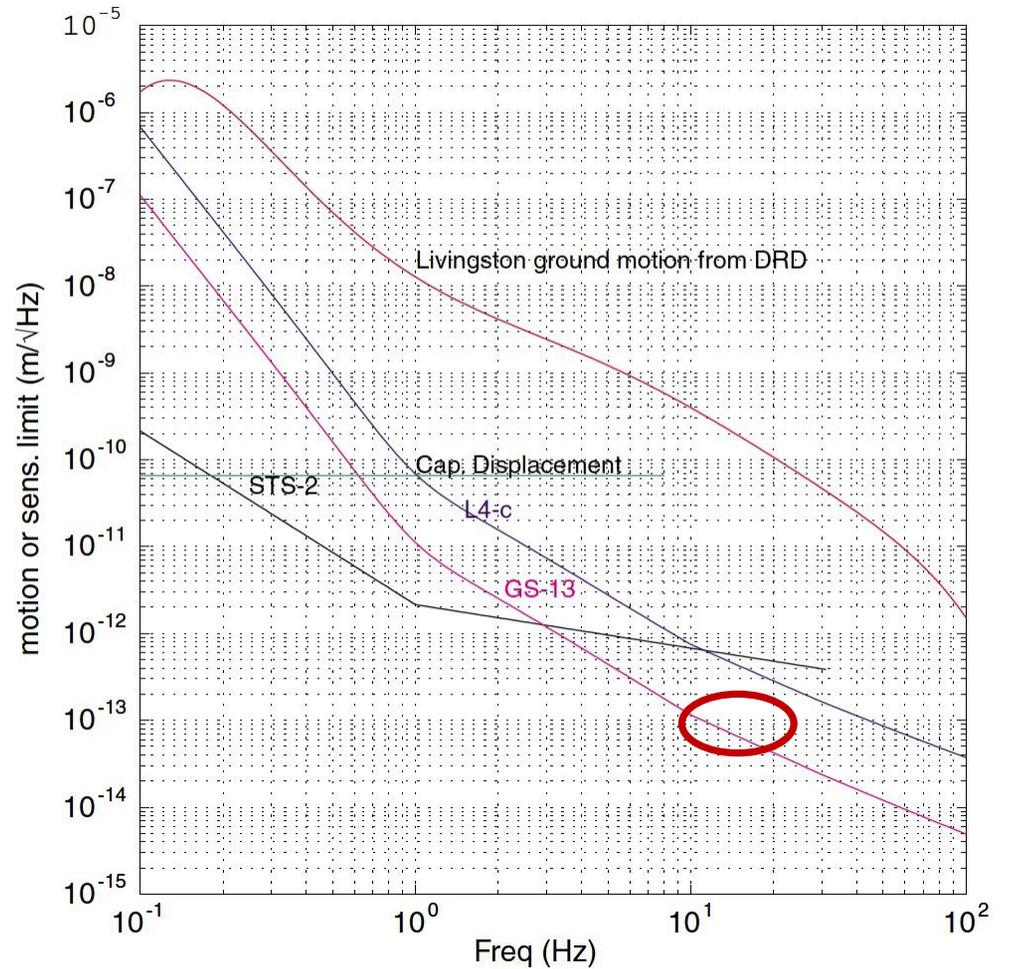


# LIGO Ground Motion

Active insulation system

- Reach **accelerometer sensor noise** in observation band
- Make the platform **follow the ground** at low frequencies using displacement sensors

## Sensor noise



## Pendulum Suspensions

Damped harmonic oscillator

$$m\ddot{x} + \gamma\dot{x} + kx = F$$

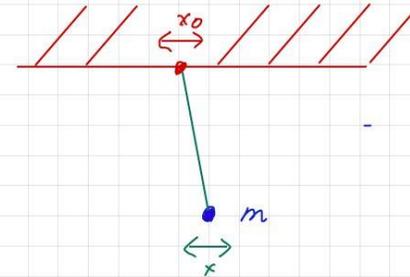
$$-\omega^2 m x + i\omega\gamma x + kx = F$$

Force  $F$  is zero, but suspension point  $x_0$  is moving:

$$\Rightarrow -\omega^2 m x + i\omega\gamma(x - x_0) + k(x - x_0) = 0$$

$$(-\omega^2 m + i\omega\gamma + k)x = (i\omega\gamma + k)x_0$$

$$\Rightarrow \frac{x}{x_0} = \frac{i\omega\gamma + k}{k - \omega^2 m + i\omega\gamma}$$



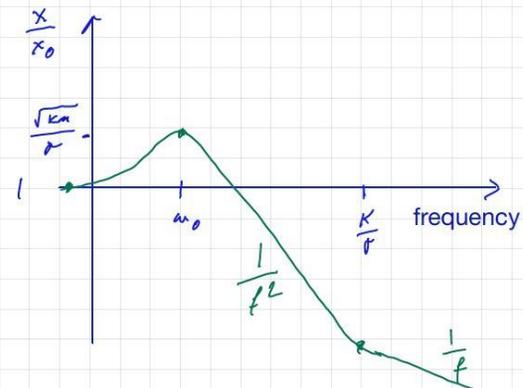
$$1 + \frac{k}{i\omega\gamma}$$

$$= 1 - i \frac{\sqrt{km}}{\gamma}$$

For  $\omega \gg \omega_0 \equiv \sqrt{\frac{k}{m}}$   $\frac{x}{x_0} \sim -\left(\frac{\omega_0}{\omega}\right)^2 \Rightarrow \frac{1}{f^2}$  suppression of external noise

But  $\omega < \frac{k}{\gamma}$

Small damping  $\gamma$  required, otherwise isolation  $\frac{1}{f}$



## Quad-Pendulum Suspensions

We can do better than  $\frac{1}{f^2}$ : Hang Pendulum from pendulum, etc (4 times for Advanced LIGO)

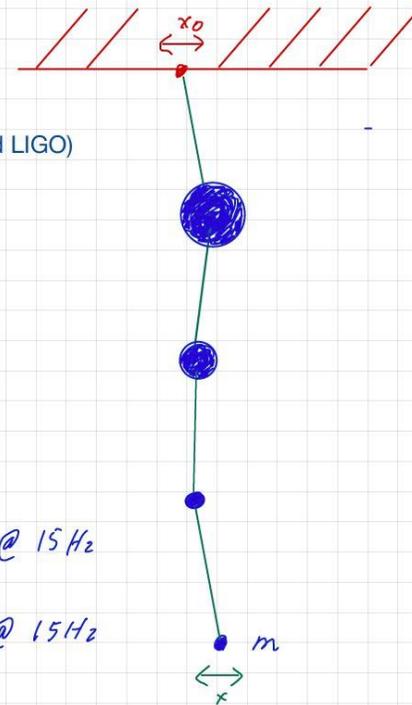
⇒ Coupled system, four resonance frequencies, choose masses wisely.

Above highest resonance ⇒ transfer function  $\frac{x}{x_0}$  drops off as  $\frac{1}{f^8}$

• Suspension platform motion (from active seismic isolation):  $\sim 2 \cdot 10^{-13} \frac{m}{\sqrt{Hz}} @ 15 Hz$

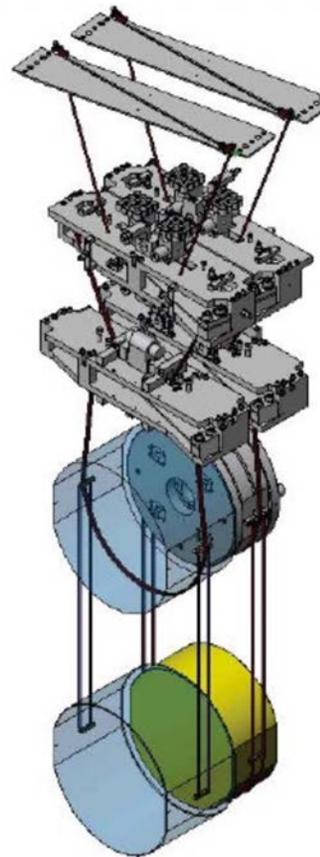
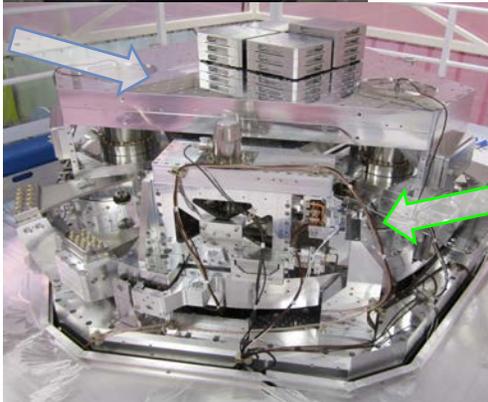
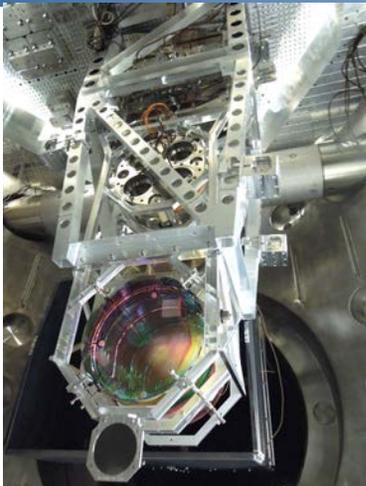
Target noise floor:  $\sim 4 \cdot 10^{-20} \frac{m}{\sqrt{Hz}} @ 15 Hz$

Highest resonance frequency: ⇒  $\sim 2.3 Hz$

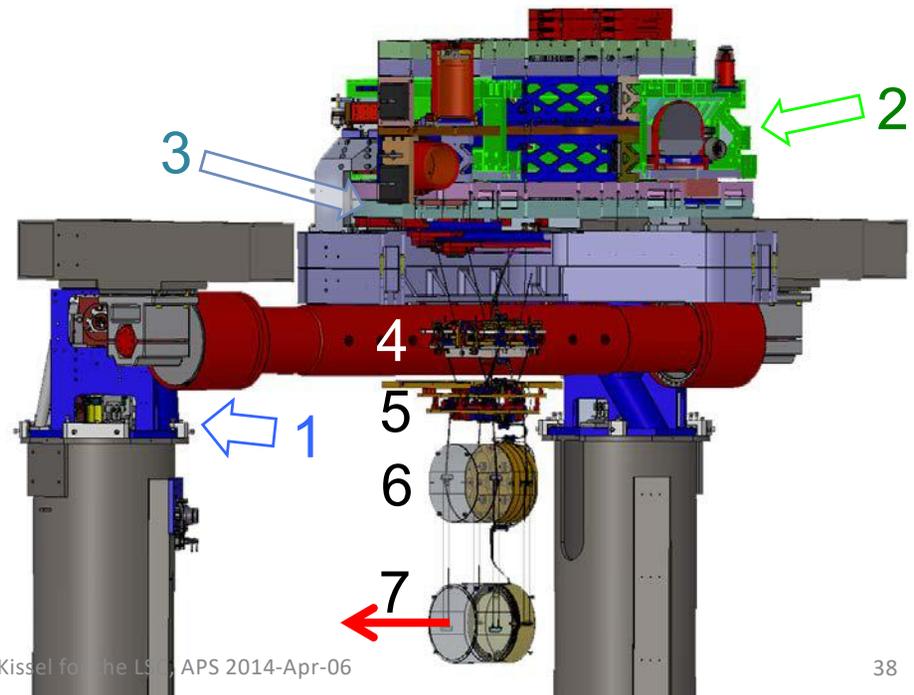


# The Advanced LIGO Detectors

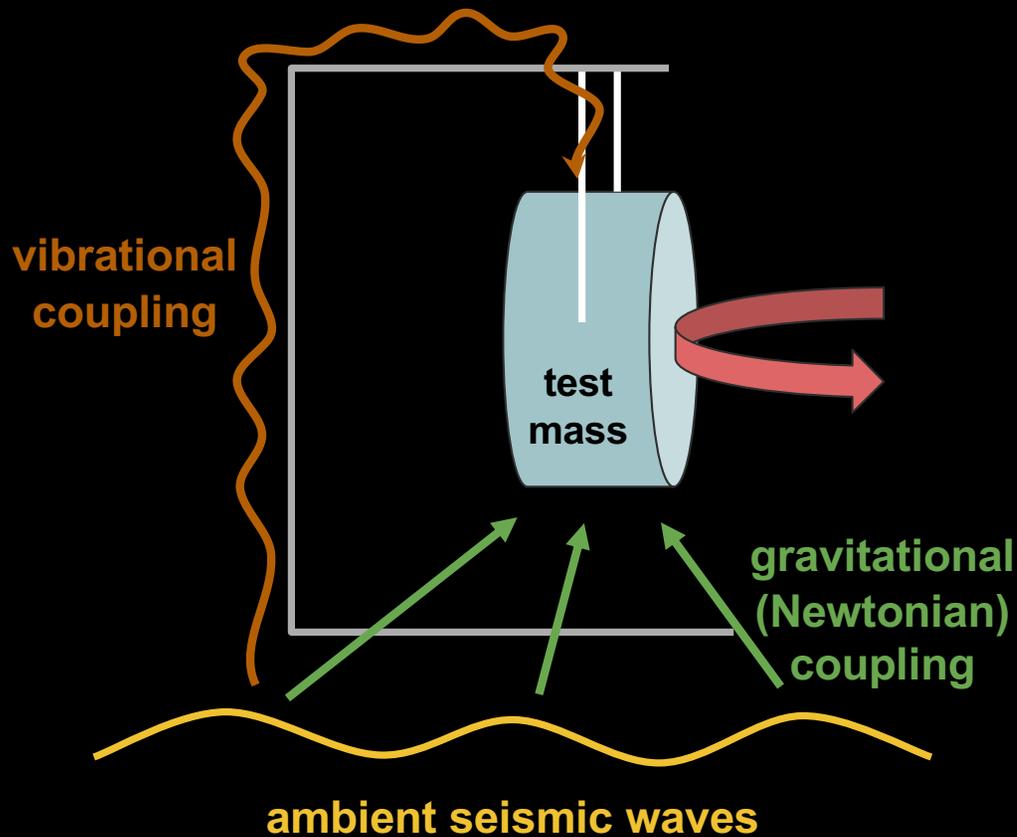
## Seismic Isolation



Internal Seismic Isolation (ISI) on top  
Quadruple Pendulum below



# Newtonian Noise: Bypassing the Isolation System



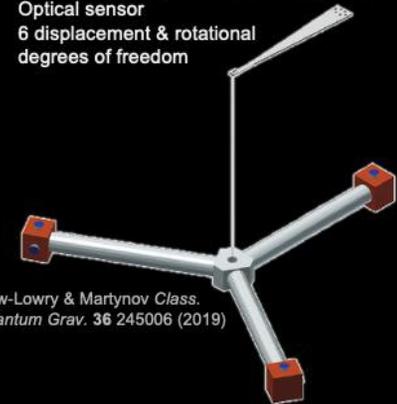
Vibrational coupling can be filtered or suppressed

Gravitational coupling cannot be shielded

- couples as  $1/f^2$
- steeper drop-off from source coherence

**Novel seismometers, e.g.:**

- Monolithic glass proof mass & suspension
- Optical sensor
- 6 displacement & rotational degrees of freedom



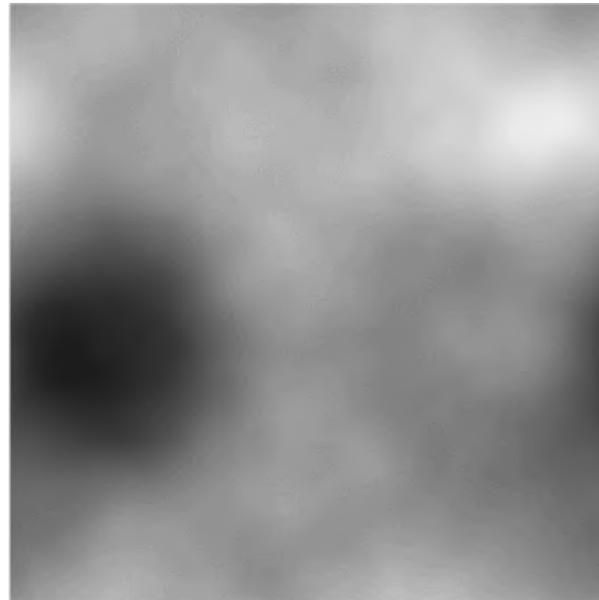
Mow-Lowry & Martynov *Class.*  
*Quantum Grav.* 36 245006 (2019)



How...



...do we isolate from any other motion?



Thermal Noise



LIGO

# Thermal Noise - Basics



- Fluctuation-dissipation theorem: It's the loss!
  - Equipartition theorem.:

$$\frac{1}{2} m \langle \dot{x}^2 \rangle = \frac{k_B T}{2}$$

vs.

$$m\ddot{x} + \gamma \dot{x} + kx = F_{\text{noise}}$$

## Thermal Noise: Fluctuation Dissipation Theorem Motivation

Damped harmonic oscillator

$$m \ddot{x} + \gamma \dot{x} + kx = F$$

Assume  $F=0 \Rightarrow x(t)$  damps out. Energy conservation?

Equipartition theorem:

$$\frac{1}{2} m \langle \dot{x}^2 \rangle = \frac{k_B T}{2} \Rightarrow \langle \dot{x}^2 \rangle = \frac{k_B T}{m}$$

Contradiction!  $F$  cannot be zero. It has to be non-zero, but random!

Express RMS velocity as integral of its power spectrum:

$$\langle \dot{x}^2 \rangle \equiv \int_0^{\infty} S_{\dot{x}\dot{x}}(f) df \quad \stackrel{!}{=} \frac{4 k_B T}{4m}$$

Can we generalize the inverse mass, and express it as an integral over frequencies???

Introduce impedance  $Z$ , via

$$Z \dot{x} = F$$

For damped harmonic oscillator:

$$Z = i\omega m + \gamma + \frac{k}{i\omega}$$

Indeed we have:

$$\frac{1}{4m} = \int_0^{\infty} \text{Re}(Z^{-1}) df = \int_0^{\infty} \frac{\gamma}{\gamma^2 + (2\alpha f m - \frac{k}{\alpha f})^2} df$$

$$\Rightarrow \int_0^{\infty} S_{\dot{x}\dot{x}}(f) df = 4k_B T \int_0^{\infty} \text{Re}(Z^{-1}) df$$



## Thermal Noise: Fluctuation Dissipation Theorem

This equation holds for the integrated at all frequencies:

$$S_{\dot{x}\dot{x}}(f) = 4k_B T \operatorname{Re}(Z^{-1})$$

Velocity Power Spectral Density (1-sided)

Real part of the inverse of the mechanical impedance

Temperature of the heat bath

- Holds for all (mechanical) systems coupled to a heat bath.
  - The physical coupling responsible for damping the motion also has to work in reverse, driving the system.
  - Can be generalized to multiple mechanical degrees of freedom, cross-power-spectra, etc.
- Note:
- $x$  and  $F$  are a pair of conjugate thermodynamic variables. Indeed the FD theorem can be generalized for any pair of conjugate TD variables: (Pressure, Volume), (Temperature, Entropy), (Chem. potential, Particle N)
  - Every pair of TD variables generates statistically independent thermal noise.



## Fluctuation Dissipation Theorem - Other Forms

Displacement Fluctuation Power Spectrum

$$S_{xx}(f) \equiv \langle x x^* \rangle = \frac{1}{-i \cdot i} \frac{1}{\omega^2} \underbrace{\langle \dot{x} \dot{x}^* \rangle}_{S_{\dot{x}\dot{x}}(f)}$$

$$S_{\dot{x}\dot{x}}(f) = 4k_B T \operatorname{Re}(Z^{-1})$$

$$\Rightarrow S_{xx}(f) = \frac{4k_B T}{\omega^2} \operatorname{Re}(Z^{-1})$$

Force Fluctuation Power Spectrum

$$\begin{aligned} S_{FF}(f) &\equiv \langle F F^* \rangle = \langle Z \dot{x} \dot{x}^* Z^* \rangle \\ &= 4k_B T \operatorname{Re}(Z^{-1}) Z^* Z \\ &= 4k_B T \cdot \frac{1}{2} (Z Z^{-1} Z^* + Z^{-1} Z^* Z) \\ &= 4k_B T \operatorname{Re}(Z) \end{aligned}$$

$$\Rightarrow S_{FF}(f) = 4k_B T \operatorname{Re}(Z)$$

$\Rightarrow S_{FF}(f)$  is white  $\Leftrightarrow \gamma = \operatorname{Re} Z$  is independent of frequency



- Fluctuation-dissipation theorem: It's the loss!
  - Equipartition theorem.:

$$\frac{1}{2} m \langle \dot{x}^2 \rangle = \frac{k_B T}{2}$$

vs.

$$m\ddot{x} + \gamma \dot{x} + kx = F_{\text{noise}}$$

- Fluctuation-dissipation theorem

$$S_{vv}(f) = 4k_B T \frac{P_{\text{diss}}(f)}{\langle F^2 \rangle}$$

- The **energy loss per cycle** (normalized by the driving force squared) is proportional to the **velocity power spectrum**

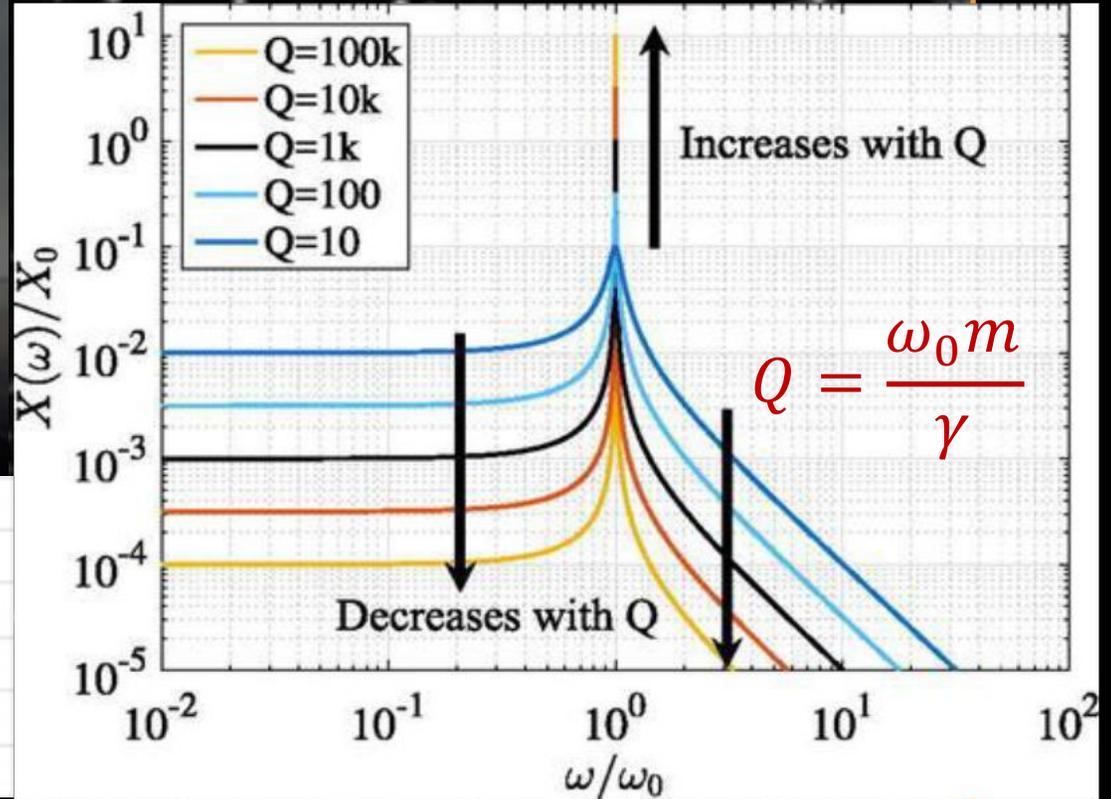
# LIGO

## Thermal Noise

$$S_{xx}(f) =$$

$$\frac{4k_B T}{\omega^2} \frac{\alpha}{\alpha^2 + \left(\omega m - \frac{k}{\omega}\right)^2}$$

Miller et al., Applied Physics Reviews 5, 041307 (2018)



Rutger Saly, YouTube, "We filmed Brownian motion, random movement of particles in water..."

## Thermal Noise: Design Implications

Damped harmonic oscillator

$$S_{xx}(f) = \frac{1}{\omega^2} S_{\dot{x}\dot{x}}(f) = \frac{4k_B T}{\omega^2} \frac{\gamma}{\omega^2 + \left(\omega_m - \frac{k}{\omega}\right)^2}$$

Off-resonance (  $\left|\omega_m - \frac{k}{\omega}\right| \gg \gamma$  )

• Above resonance frequency:  $S_{xx}(f) = \frac{4k_B T}{\omega^4 m^2} \gamma$  Example: Gas damping

• Below resonance frequency:  $S_{xx}(f) = \frac{4k_B T}{k^2} \gamma$

For structural damping:  $\gamma = 0$ , but  $k = \tilde{k}(1 + i\varphi)$   $\varphi$ : Mechanical loss angle  $\Rightarrow k \rightarrow \tilde{k}$   
 $\gamma \rightarrow \frac{k\varphi}{\omega}$

• Above resonance frequency:  $S_{xx}(f) = \frac{4k_B T}{\omega^5 m^2} \tilde{k} \varphi$  Example: suspension thermal noise

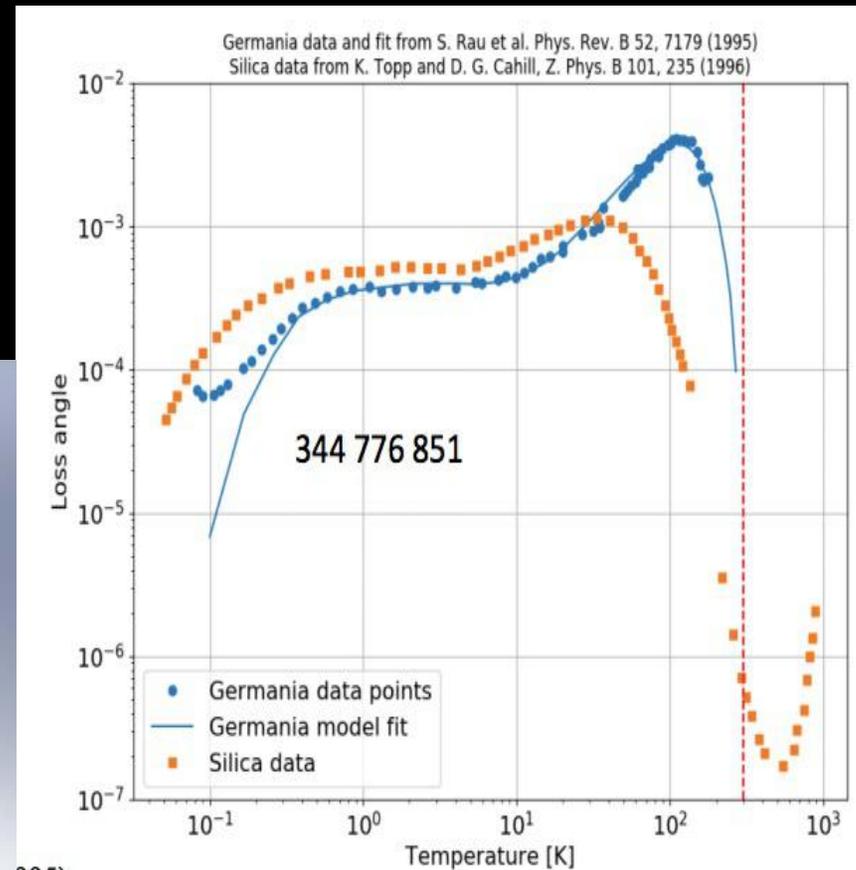
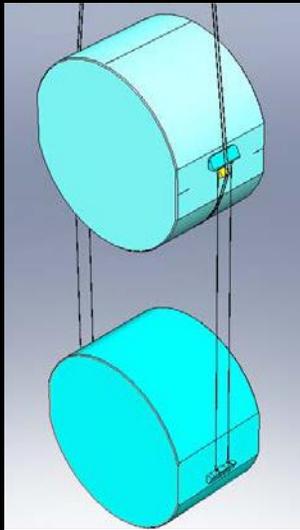
• Below resonance frequency:  $S_{xx}(f) = \frac{4k_B T}{\omega k} \varphi$  Example: coating thermal noise

**We need to minimize mechanical damping!**



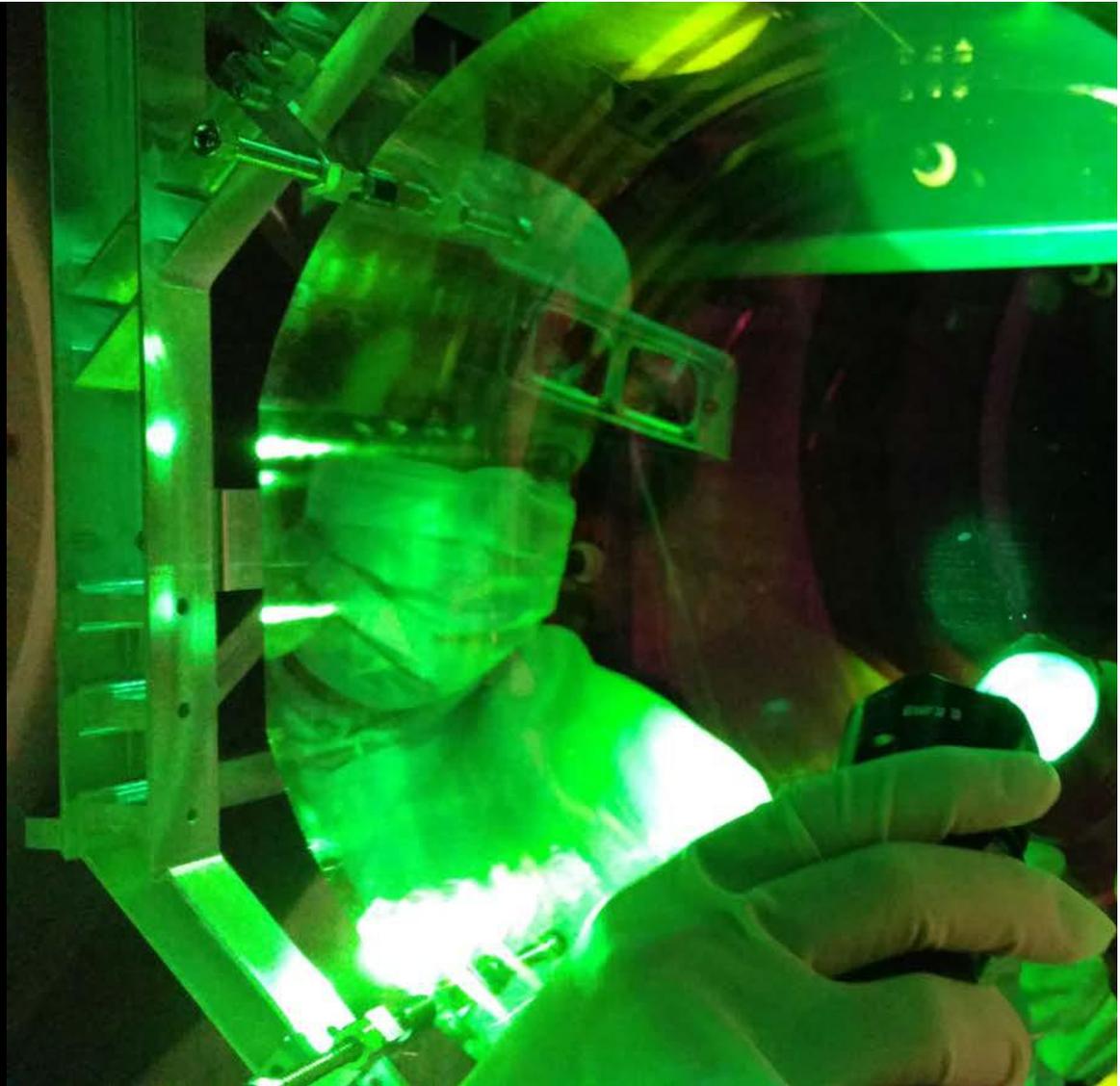
# Suspension Thermal Noise

- **Dominated** by last suspension stage
  - Thermal noise from upper stages **filtered** by remaining suspension stages
- Most potential energy stored by gravity  
→ **mechanical loss diluted**
- SiO<sub>2</sub> has **extraordinary low mechanical loss** at room temperature!  
→ **Monolithic bottom stage**



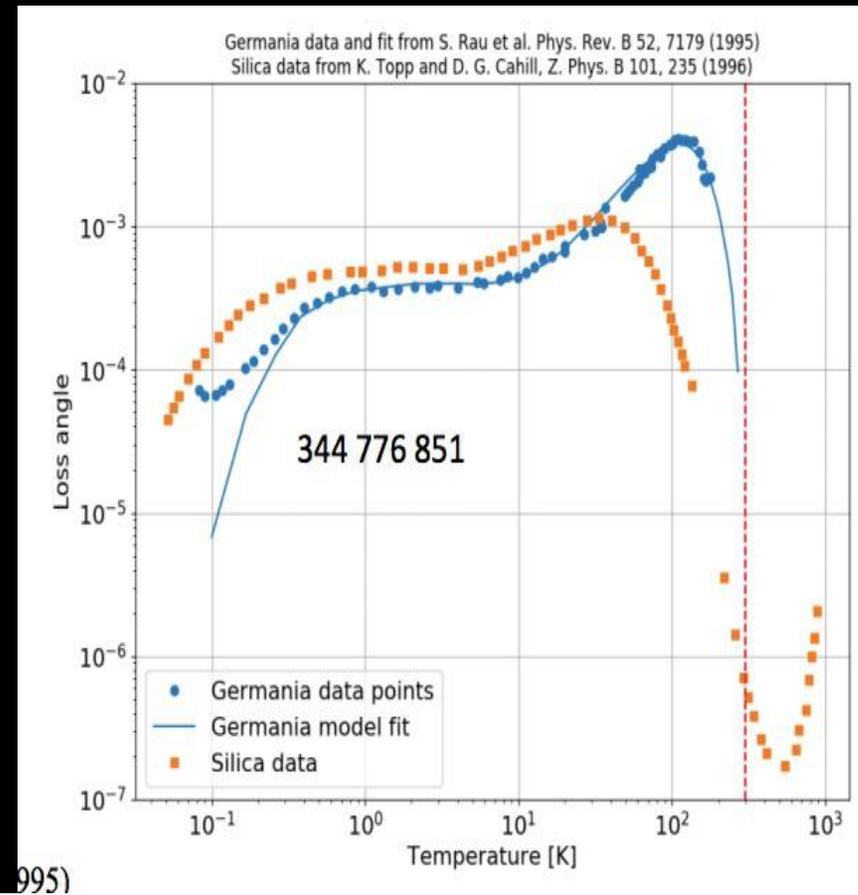
# Coating Thermal Noise

- **Dielectric Mirror Coating** dominates mechanical loss ( $\text{TiO}_2$ -doped  $\text{Ta}_2\text{O}_5$   $\text{SiO}_2$ )
- Mirror coating interacts directly with laser light, no extra filtering possible
- **Need better coating material!**



# TiO<sub>2</sub>:GeO<sub>2</sub> / SiO<sub>2</sub> coatings

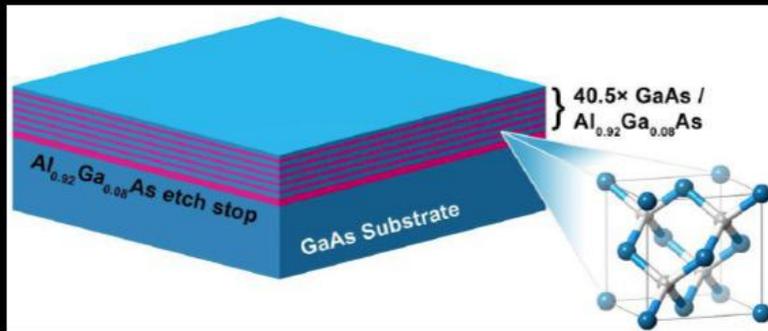
- **Germania (GeO<sub>2</sub>)** has loss angle  $\sim 4e-5$ 
  - similar to Silica (SiO<sub>2</sub>)
  - much lower than Tantalum (Ta<sub>2</sub>O<sub>5</sub>)
- But:
  - Refractive index of Germania 1.6
  - 2.1 for Tantalum
  - 1.45 for Silica
- Can achieve  **$\sim 30\%$**  thermal noise amplitude reduction
- Candidate for **A+** upgrade



# Crystalline AlGaAs coatings

- The crystal is grown via Molecular Beam Epitaxy (MBE) on a single-crystal GaAs wafer.
- Alternating the Al alloy composition forms a Bragg reflector from layers of  $\text{Al}_{0.92}\text{Ga}_{0.08}\text{As}$  ( $n=2.89$ ) and  $\text{GaAs}$  ( $n=3.30$ ).
- Limited to  $\lambda > 870\text{nm}$

G. Cole 2013

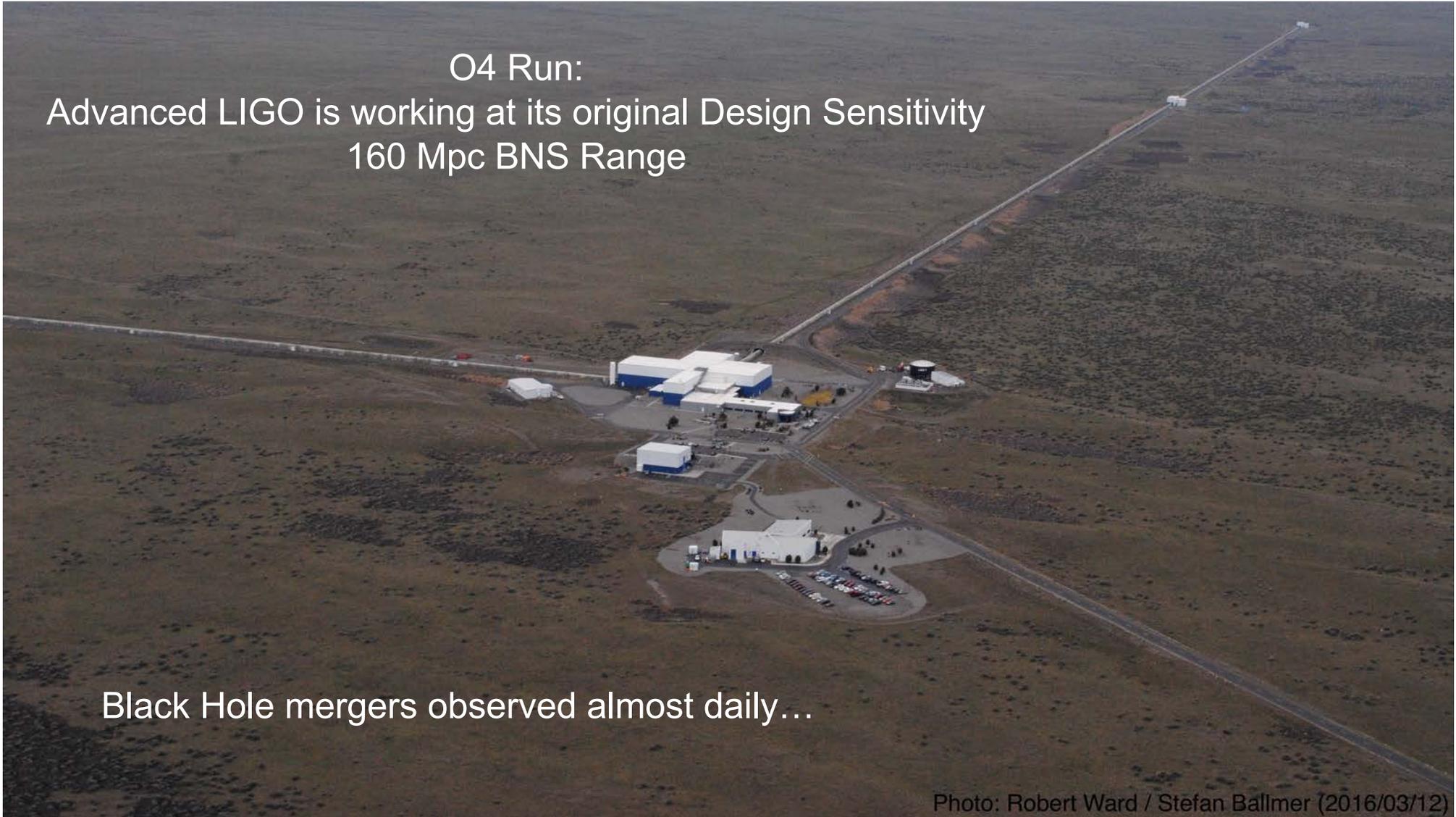


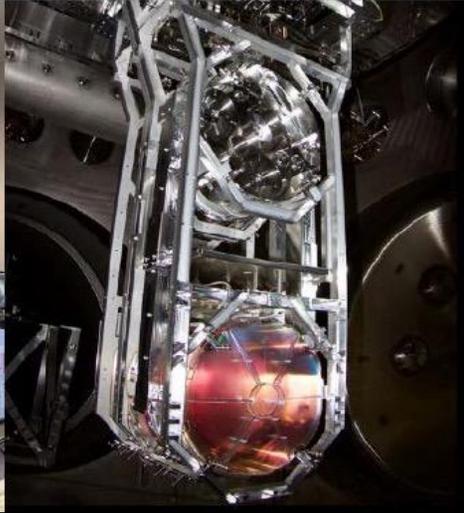
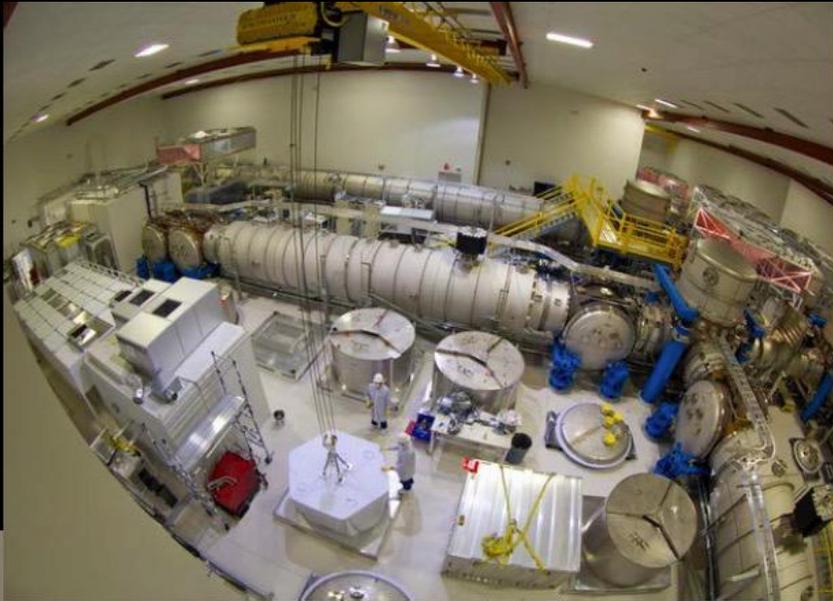
[https://www.thorlabs.com/newgrouppage9.cfm?objectgroup\\_id=14069](https://www.thorlabs.com/newgrouppage9.cfm?objectgroup_id=14069)

O4 Run:  
Advanced LIGO is working at its original Design Sensitivity  
160 Mpc BNS Range

Black Hole mergers observed almost daily...

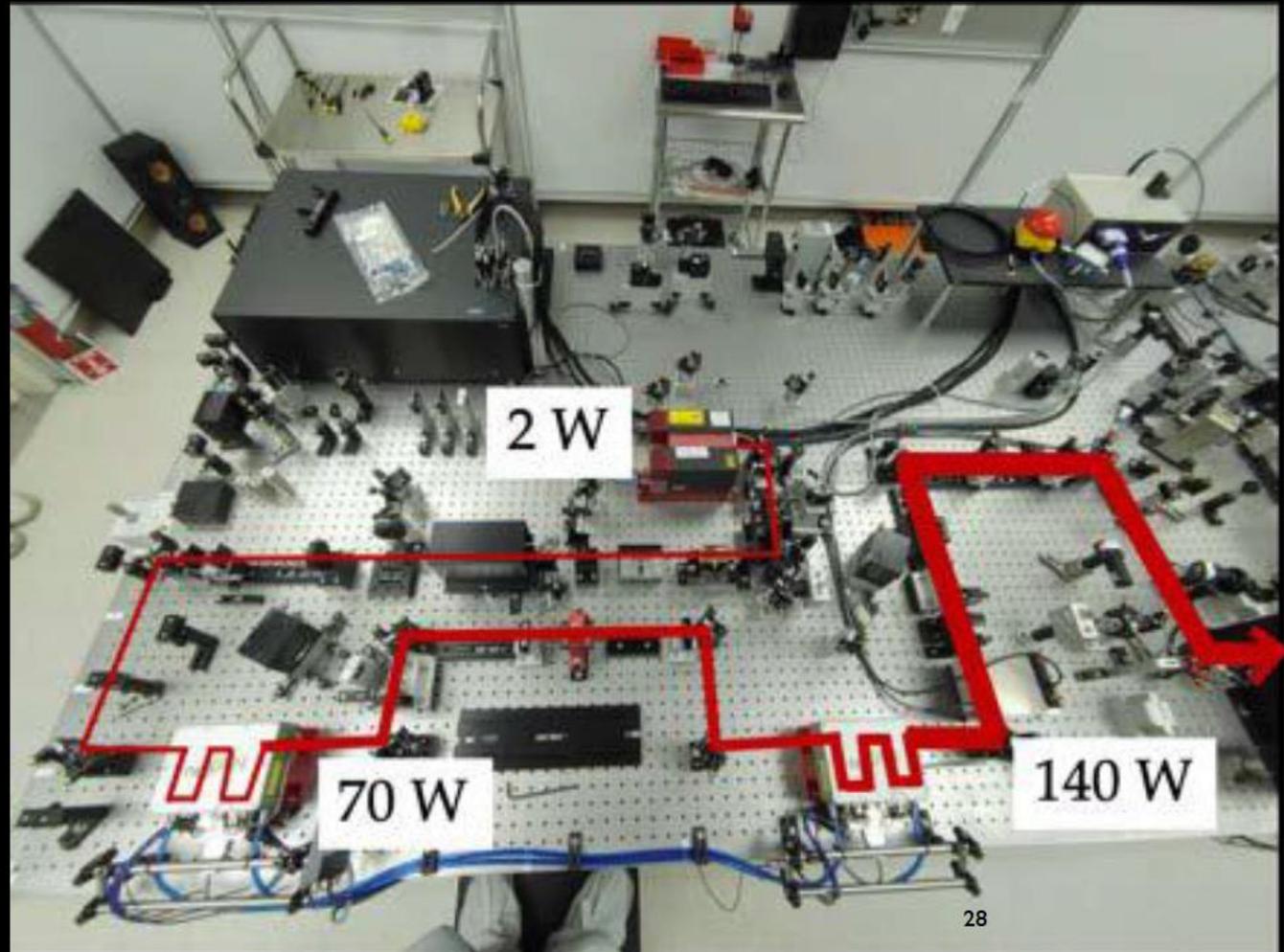
Photo: Robert Ward / Stefan Ballmer (2016/03/12)



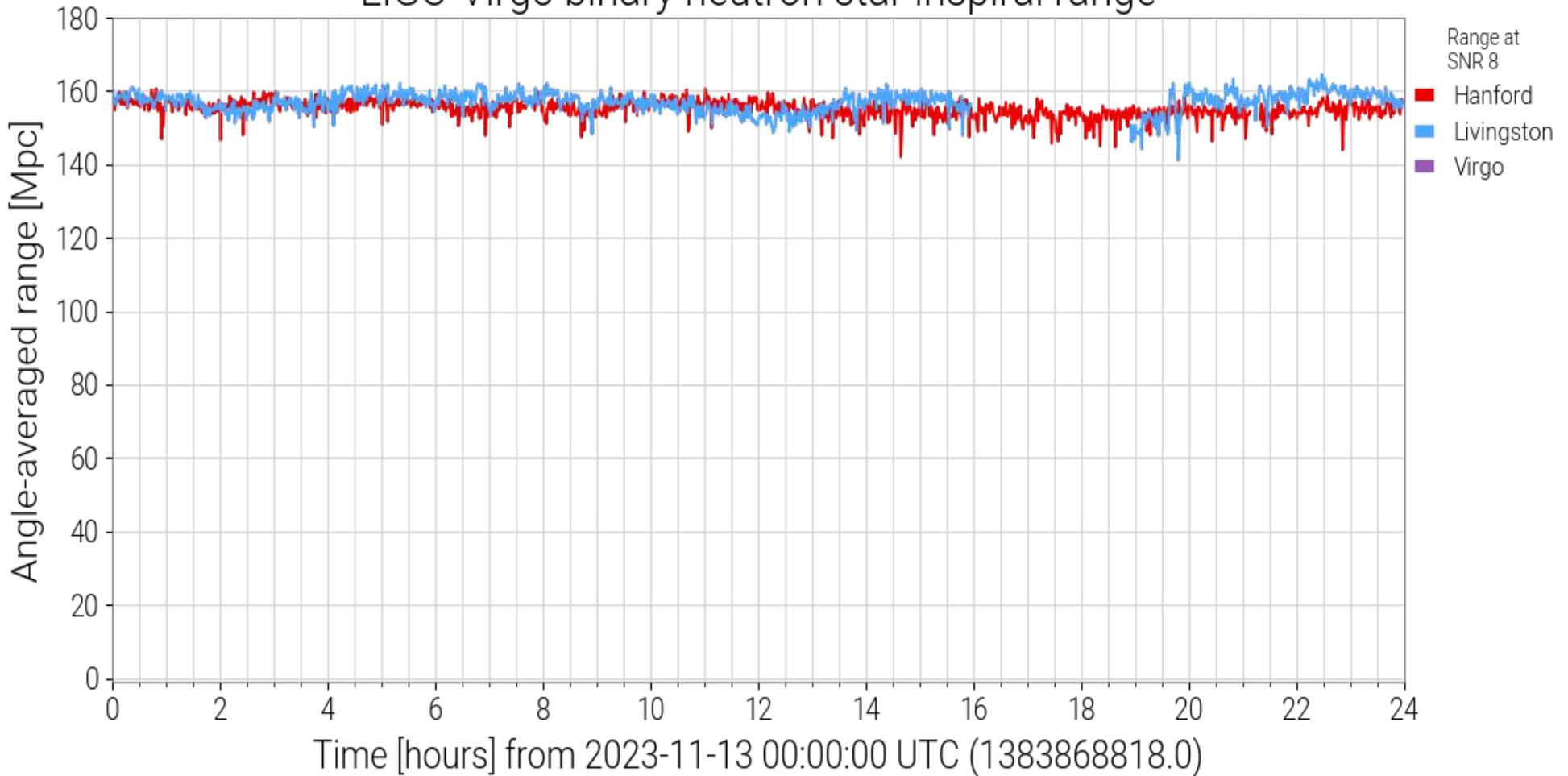


# Pre-Stabilized Laser

- 2W NPRO seed laser, 2 neoVAN-4S-HP amplification stages
- Delivers 110W to vacuum system



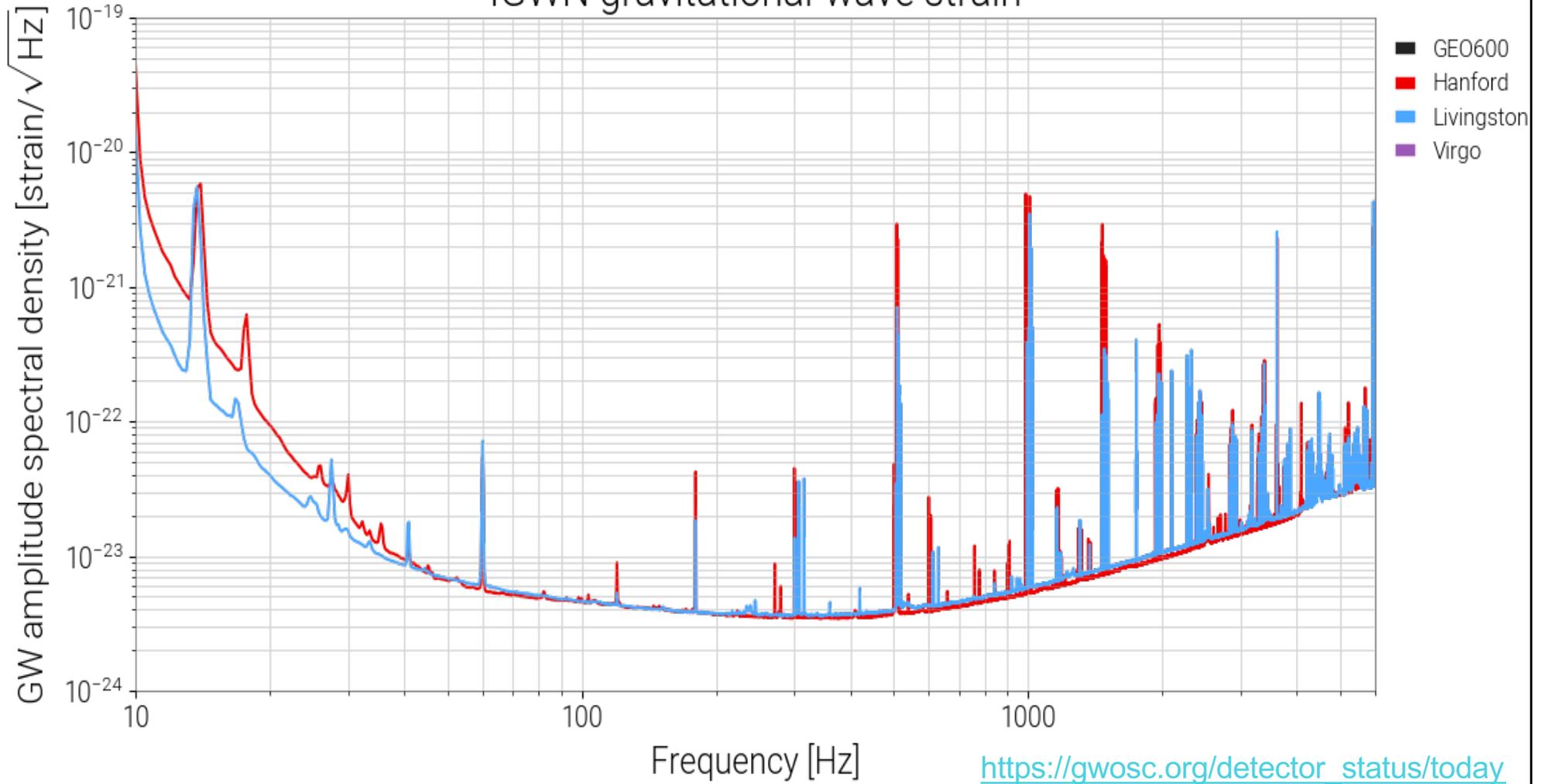
# LIGO-Virgo binary neutron star inspiral range



[https://gwosc.org/detector\\_status/today](https://gwosc.org/detector_status/today)

[1383868818-1383955218, state: Observing]

# IGWN gravitational-wave strain



# O4 Events

- <https://gracedb.ligo.org/superevents/public/O4>



Event ID	Possible Source (Probability)	UTC	GCN	Location	FAR	Comments
S231114n	BBH (>99%)	Nov. 14, 2023 04:32:11 UTC	GCN Circular Query Notices   VOE		1 per 100.04 years	
S231113bw	BBH (96%), Terrestrial (4%)	Nov. 13, 2023 20:04:17 UTC	GCN Circular Query Notices   VOE		1 per 2.3265 years	
S231113bb	BBH (96%), Terrestrial (4%)	Nov. 13, 2023 12:26:23 UTC	GCN Circular Query Notices   VOE		1.7663 per year	
S231112ag	BBH (>99%)	Nov. 12, 2023 11:02:03 UTC	GCN Circular Query Notices   VOE		1 per 2.9671e+06 years	RETRACTED
S231110g	BBH (97%), Terrestrial (3%)	Nov. 10, 2023 04:03:20 UTC	GCN Circular Query Notices   VOE		1 per 1.6429 years	
S231108u	BBH (>99%)	Nov. 8, 2023 12:51:42 UTC	GCN Circular Query Notices   VOE		1 per 100.04 years	
S231104oc	BBH (>99%)	Nov. 4, 2023 13:34:18 UTC	GCN Circular Query Notices   VOE		1 per 100.04 years	
S231102w	BBH (>99%)	Nov. 2, 2023 07:17:36 UTC	GCN Circular Query Notices   VOE		1 per 5.4261e+14 years	
S231030av	BNS (93%), NSBH (6%), Terrestrial (1%)	Oct. 30, 2023 12:51:11 UTC	GCN Circular Query Notices   VOE		1.3301 per year	RETRACTED
S231029y	BBH (>99%)	Oct. 29, 2023 11:15:08 UTC	GCN Circular Query Notices   VOE		1 per 146.45 years	
S231028bg	BBH (>99%)	Oct. 28, 2023 15:30:06 UTC	GCN Circular Query Notices   VOE		1 per 4.1513e+22 years	
S231020bw	BBH (>99%)	Oct. 20, 2023 18:05:09 UTC	GCN Circular Query Notices   VOE		1 per 91.785 years	
S231020ba	BBH (91%), NSBH (8%)	Oct. 20, 2023 14:29:47 UTC	GCN Circular Query Notices   VOE		1 per 25.01 years	
S231014r	BBH (99%)	Oct. 14, 2023 04:05:32 UTC	GCN Circular Query Notices   VOE		1 per 3.0666 years	
S231008ap	BBH (>99%)	Oct. 8, 2023 14:25:21 UTC	GCN Circular Query Notices   VOE		1 per 20.718 years	57

OBSERVING  
01  
2015 - 2016

02  
2016 - 2017

# Observations

03a+b  
2019 - 2020

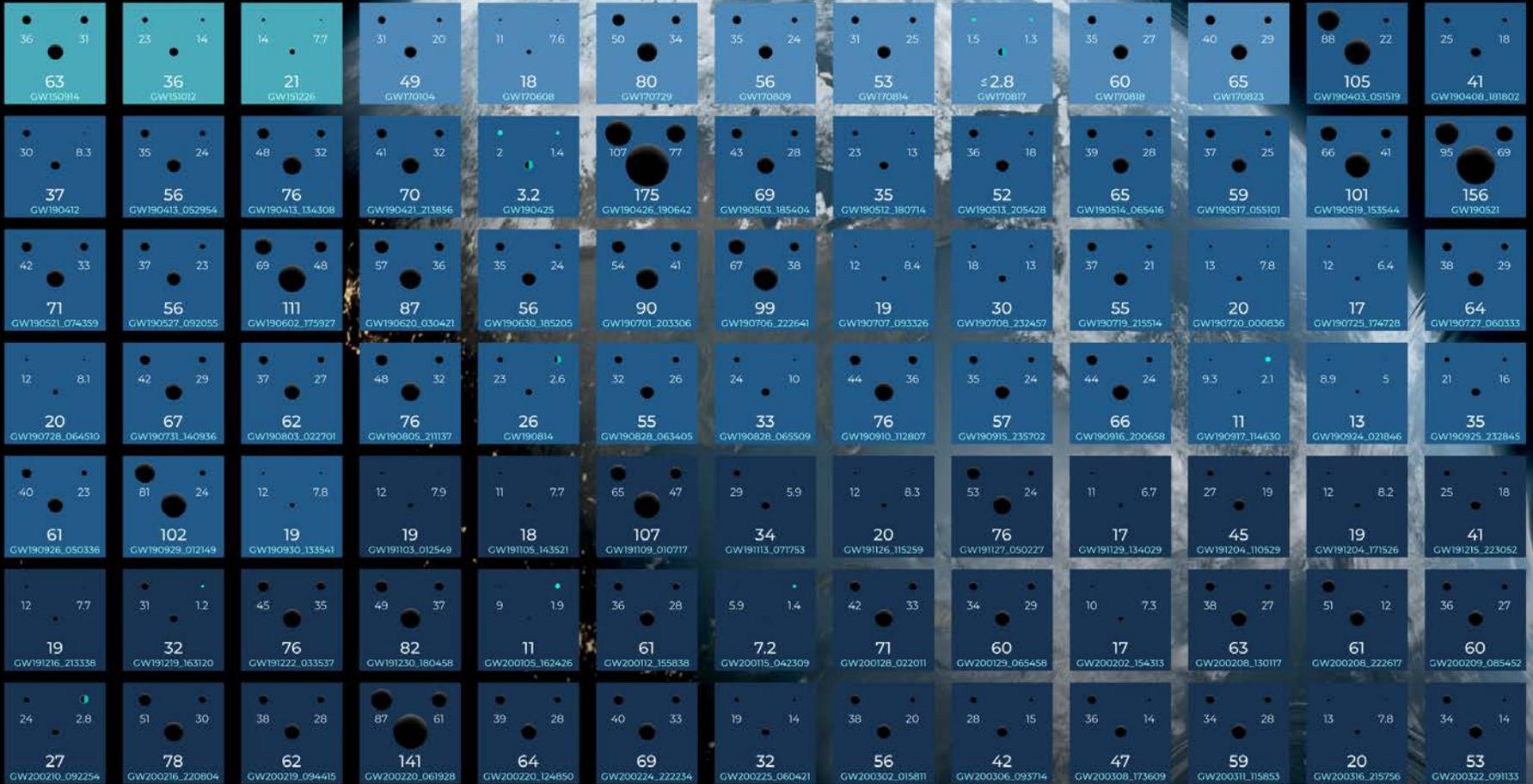
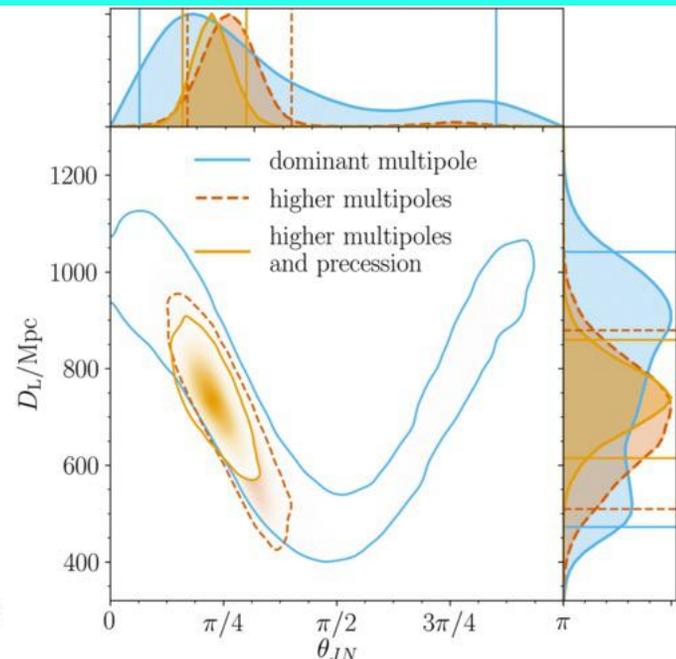
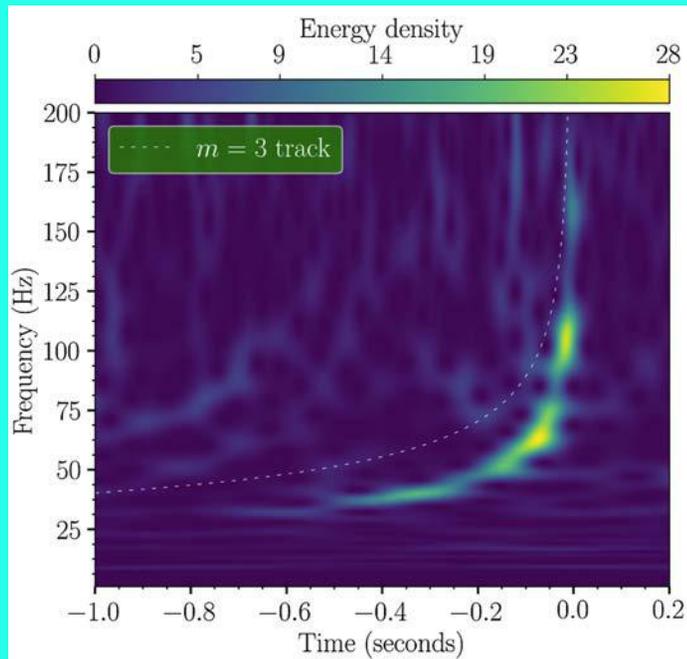


Image credit "Carl Knox (OzGrav, Swinburne University of Technology)"

Slide: S. Fairhurst



# GW190412: Unequal mass binary

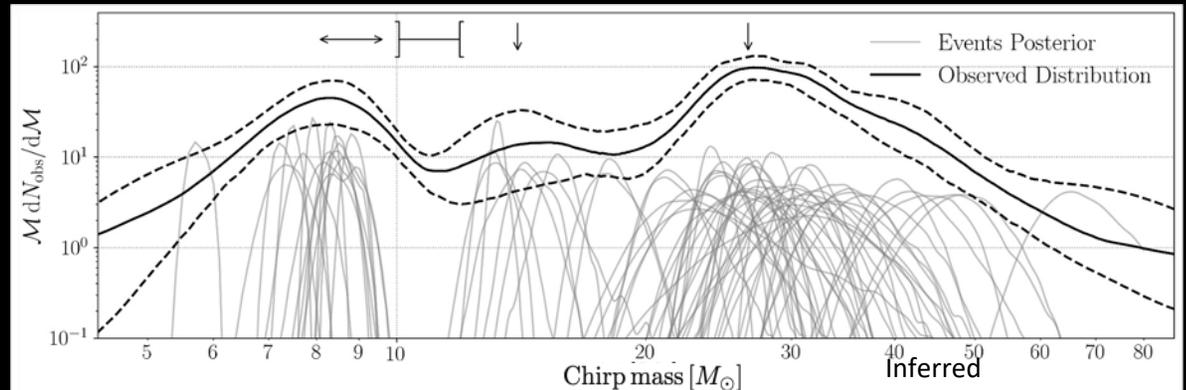


# Features in the Black Hole mass spectrum

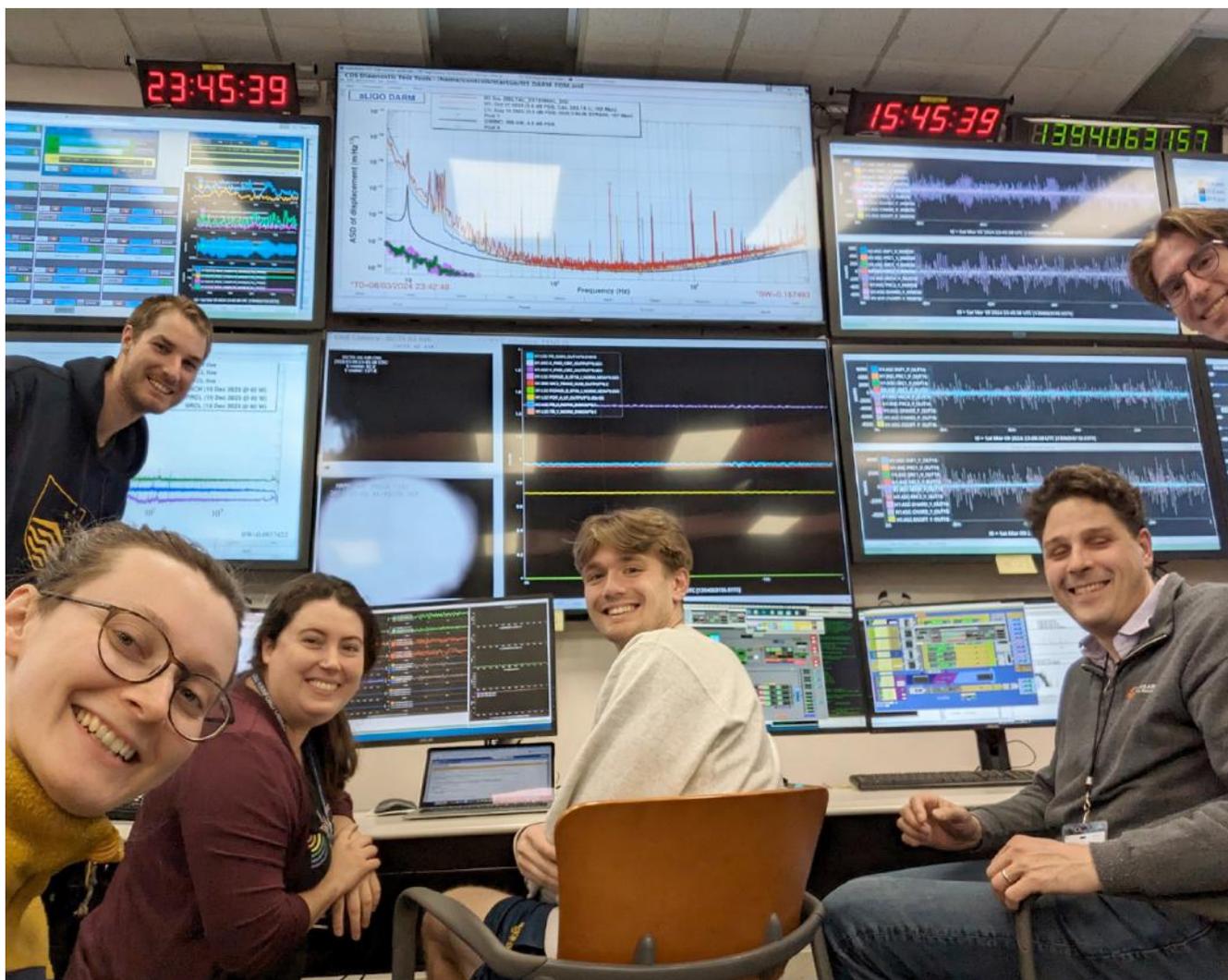
Observations clustered in chirp mass

$$\mathcal{M} = \frac{(m_1 m_2)^{3/5}}{(m_1 + m_2)^{1/5}}$$

- Chirp mass is the combination of masses which is best measured



- **Over-density** between  $8M_{\odot}$  and  $10M_{\odot}$  and around  $26M_{\odot}$ .
- A **weaker feature** present at around  $14M_{\odot}$
- **Absence** of mergers with chirp masses between  $10M_{\odot}$  and  $12M_{\odot}$ .



## 04 Commissioning Break

- LIGO Hanford Output Mode Cleaner
- LIGO Livingston End Test Mass cleaning
- Squeezer path work
- New scattered light baffles and baffle dampeners
- Resume observations Apr 3rd

Syracuse University team in the Hanford Control Room (3/9/2024)



Where do we go  
from here?

“Recently, we have waded a little out to sea,  
enough to dampen our toes or, at most, wet our  
ankles. The water seems inviting. The ocean calls.”

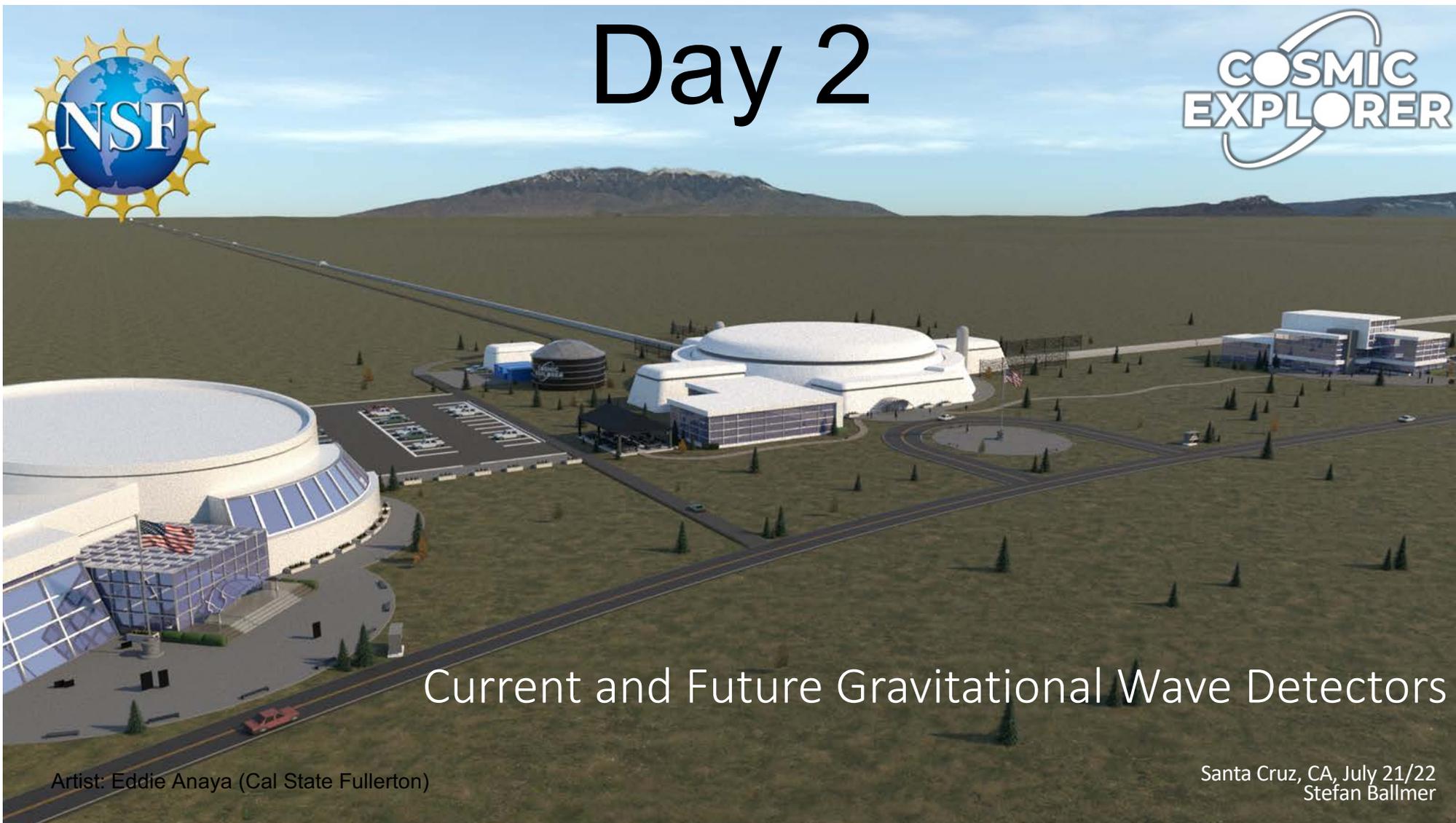
Carl Sagan



That's for tomorrow...



# Day 2



## Current and Future Gravitational Wave Detectors

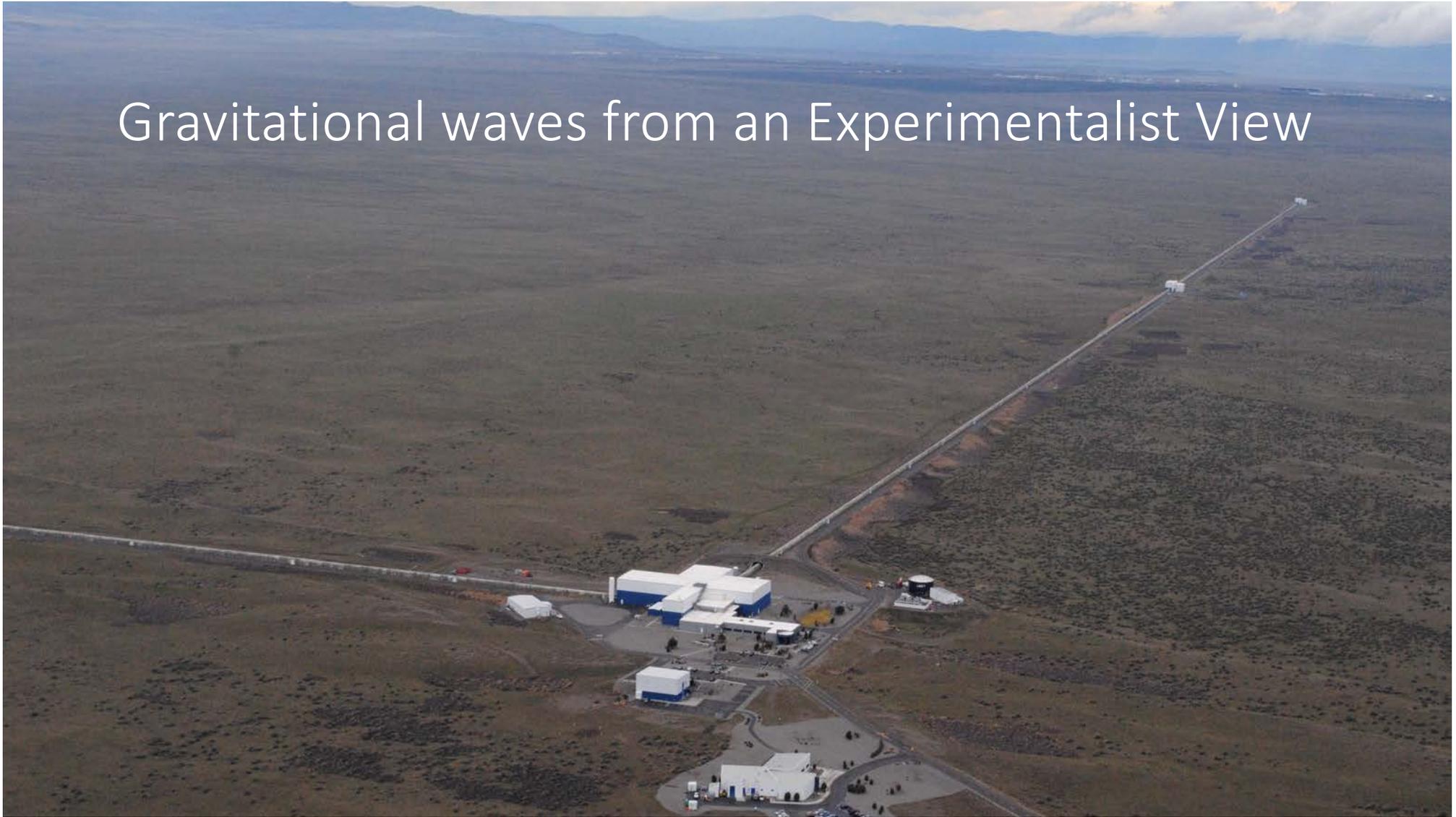
Artist: Eddie Anaya (Cal State Fullerton)

Santa Cruz, CA, July 21/22  
Stefan Ballmer

# Outline

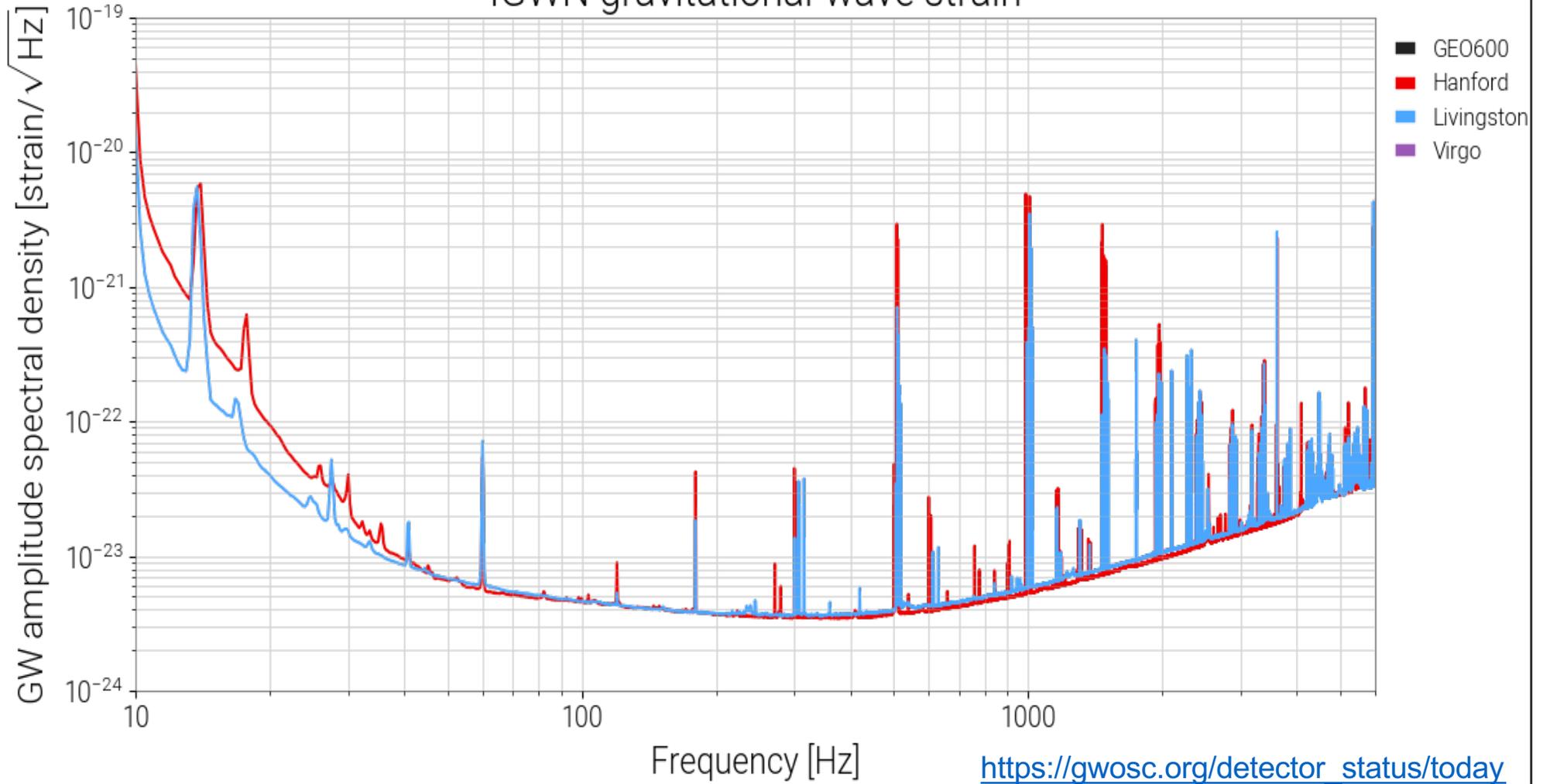
- Day 1
  - Gravitational waves from an Experimentalist View
    - History of the field
  - How can you measure them in principle?
    - Scale of effect
    - How to read out such small motions (Classical Shot Noise)
    - How to isolate all other large motion (Seismic isolation, Newtonian noise, Thermal Noise)
  - How is Advanced LIGO doing in O4?
- Day 2
  - Key Technologies for the Future
    - Beyond Quantum Noise (Quantization of EM field, squeezing)
  - Cosmic Explorer: the Next-generation of US GW detectors
- Will not talk about sources
  - See presentations from Jim Lattimer and Neil Cornish for that

# Gravitational waves from an Experimentalist View



[1383868818-1383955218, state: Observing]

# IGWN gravitational-wave strain





How...

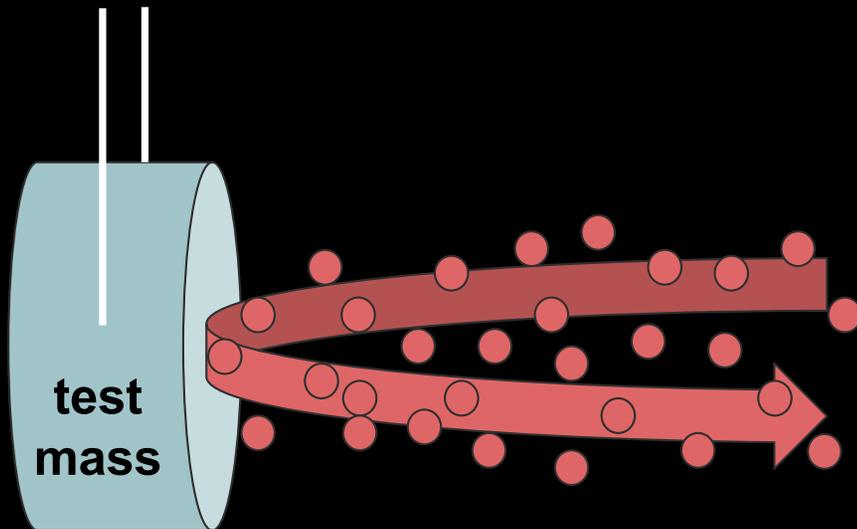
...do we surpass...

Quantum Noise

Shot Noise  
&  
Radiation Pressure Noise



# Quantum noises



Shot noise  
(photon counting on detector)  
⇒ *need high optical power*

Radiation pressure noise  
(photon momentum)  
⇒ *need heavy test masses*

# Classical:

## Classical Radiation Pressure Noise

Recall classical shot noise:

$$S_{PP}(f) = 2 P h \nu \quad ; \quad S_n = \sqrt{2 P h \nu}$$

Force on fully reflecting mirror:

$$F = \frac{2P}{c}$$

⇒ Classical radiation pressure noise:

$$S_F = \frac{2 S_P}{c} = \frac{2}{c} \sqrt{2 P h \nu}$$

But:

*usually much bigger!*

Any power fluctuations (classical and quantum) are entering from the input side

They will get enhanced in cavity (but filtered above cavity pole)

They should be common in both arms..... And cancel completely?????

## Quantization of Maxwell Equation

Maxwell equation  $c=1, \epsilon_0=1, \mu_0=1$

$$\begin{aligned} \dot{\vec{E}} &= \vec{\nabla} \times \vec{B} \\ \dot{\vec{B}} &= -\vec{\nabla} \times \vec{E} \end{aligned} \Rightarrow \text{Interpret as collection of harmonic oscillators, one at each frequency } \omega_0 \equiv k$$

For simplicity, assume plane wave,  $\vec{k} \parallel \hat{z}$ ,  $\vec{E} \parallel \hat{x}$ ,  $\vec{B} \parallel \hat{y}$

Switch to scalar amplitudes

$$\begin{aligned} \dot{E} &= -B' \\ \dot{B} &= -E' \end{aligned}$$

But for plane wave we know  $E=B$  ..... and they are in phase..... what is going on?

Two Quadratures:

$$\begin{aligned} E &= E_{10} \cos(kz - \omega t) + E_{20} \sin(kz - \omega t) \\ &= \text{Re} \left( \underbrace{(E_{10} + iE_{20})}_{X(t)} e^{i\omega t} e^{-ikz} \right) \\ &= \text{Re} \left( X(t) e^{-ikz} \right) \end{aligned}$$

Complex field amplitude  $X = X_1 + iX_2$

Note: Maxwell equation respects quadratures.

"Phasor"

Define:  $\langle f \rangle := \frac{2}{L} \int_{-L/2}^{L/2} \cos kz f(t, z) dz$

Introduce position and momentum

$$\begin{aligned}
 \dot{x} &= \langle E \rangle & \Rightarrow \dot{x} &= p \\
 \dot{p} &= \langle -B' \rangle & \dot{p} &= \langle -B' \rangle = \langle E'' \rangle = \langle -k^2 E \rangle = -k^2 x
 \end{aligned}$$

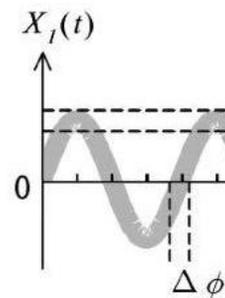
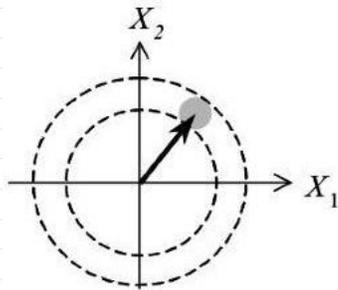
↑  
integrate by parts twice

$$\begin{aligned}
 \dot{x} &= p \\
 \dot{p} &= -k^2 x
 \end{aligned}$$

$$\delta \begin{cases} x = X_1 \\ p = -k X_2 \end{cases} \Rightarrow X \equiv X_1 + i X_2 = x - \frac{i p}{k}$$

$$\dot{X} = ikX$$

Can be quantized just like mechanical harmonic oscillator!



## Quantization of Maxwell Equation

So far we didn't pay attention to the normalization of the field  $\chi$  ;

$$\Rightarrow H = \int \omega (X^\dagger X)$$

Note: this is volume dependent...  
But we won't need the details.

$$H = \frac{1}{2} m \dot{\chi}^2 + \frac{p^2}{2m} \quad \text{with} \quad \Delta \chi \Delta \chi \geq \frac{\hbar}{2}$$

$$\Rightarrow \Delta X_1, \Delta X_2 \geq \frac{1}{4}$$

## Normalization for Experimentalists

Compare to classical shot noise! (unsqueezed,  $\Delta\psi_1 = \Delta\psi_2$ )

$$P = |\psi|^2 = |\psi_0 + \delta\psi_1 + i\delta\psi_2|^2 = |\psi_0|^2 + 2\psi_0 \delta\psi_1$$

$$= P + 2\sqrt{P} \delta\psi_1$$

$$S_{PP}^{2\text{-sided}} \equiv \langle PP^+ \rangle = 4P \langle \delta\psi_1^2 \rangle = 4P \Delta\psi_1^2 \stackrel{!}{=} P \hbar\omega \Rightarrow \text{we need to}$$

recover shot noise!

$$\begin{array}{l} \downarrow \\ \text{2-sided} \\ \Delta\psi_1^2 = \frac{1}{4} \hbar\omega \left[ \frac{\text{Watt}}{\text{Hz}} \right] \\ \Rightarrow \Delta\psi_1 \cdot \Delta\psi_2 \geq \frac{1}{4} \hbar\omega \end{array}$$

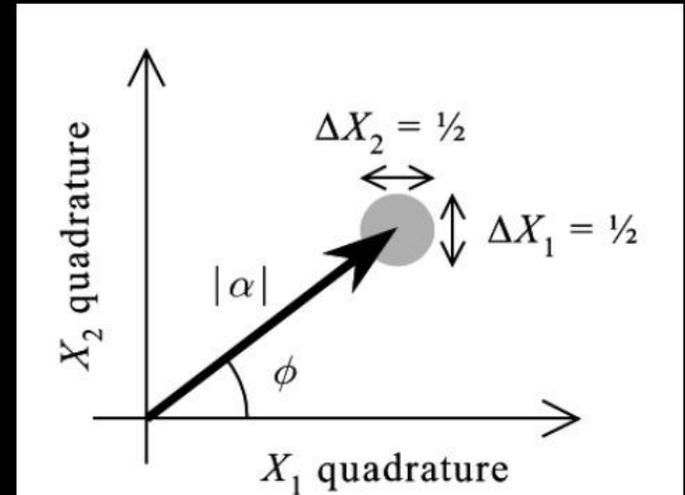
but only  $\delta\psi_1$  matters!

$$S_{PP}^{1\text{-sided}} \equiv \langle PP^+ \rangle = 4P \langle \delta\psi_1^2 \rangle = 4P \Delta\psi_1^2 \stackrel{!}{=} 2P \hbar\omega$$

$$\begin{array}{l} \downarrow \\ \text{1-sided} \\ \Delta\psi_1^2 = \frac{1}{2} \hbar\omega \left[ \frac{\text{Watt}}{\text{Hz}} \right] \end{array}$$

## Coherent State I (Fox 7.5)

- Quantum mechanical equivalent to classical monochromatic EM wave is coherent state  $|\alpha\rangle$
- For linearly polarized mode in cavity volume  $V$ ,  $\alpha = X_1 + iX_2$
- Can separate into amplitude and phase  $\alpha = |\alpha| e^{i\phi}$  with  $|\alpha| = \sqrt{X_1^2 + X_2^2}$  and  $X_1 = |\alpha| \cos \phi$  and  $X_2 = |\alpha| \sin \phi$ ,  $\alpha$  can be represented with phasor length  $|\alpha|$ , angle  $\phi$
- Coherent state is a minimum uncertainty state so  $\Delta X_1 = \Delta X_2 = \frac{1}{2}$  (shaded circle)
- Relating with  $E_{\text{classical}} = \bar{n}\hbar\omega$ , find  $|\alpha| = \sqrt{n}$



**Fig. 7.5** Phasor diagram for the coherent state  $|\alpha\rangle$ . The length of the phasor is equal to  $|\alpha|$ , and the angle from the  $X_1$ -axis is the optical phase  $\phi$ . The quantum uncertainty is shown by a circle of diameter  $1/2$  at the end of the phasor.

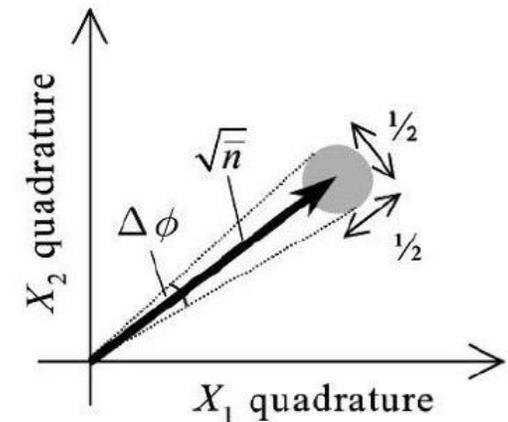
Mark Fox, Quantum Optics

## Shot Noise (Fox 7.6)

- Average phasor length  $\alpha$ , circle diameter is  $1/2$ , length of phasor uncertain between  $(\alpha + 1/4)$  and  $(\alpha - 1/4)$
- $\Delta n = (|\alpha| + 1/4)^2 - (|\alpha| - 1/4)^2 = |\alpha| = \sqrt{\bar{n}}$ 
  - coherent states have Poissonian photon statistics and shot noise (from light's quantum uncertainty)

- For large  $|\alpha|$ , phase uncertainty is  $\Delta\phi = \frac{1/2}{\sqrt{\bar{n}}}$

- These give number-phase uncertainty of light,  $\Delta n \Delta\phi \geq \frac{1}{2}$



**Fig. 7.6** The uncertainty circle of a coherent state  $|\alpha\rangle$  introduces both photon number and phase uncertainty. Note that the phase uncertainty  $\Delta\phi$  is only well-defined when  $|\alpha| = \sqrt{\bar{n}} \gg 1$ .

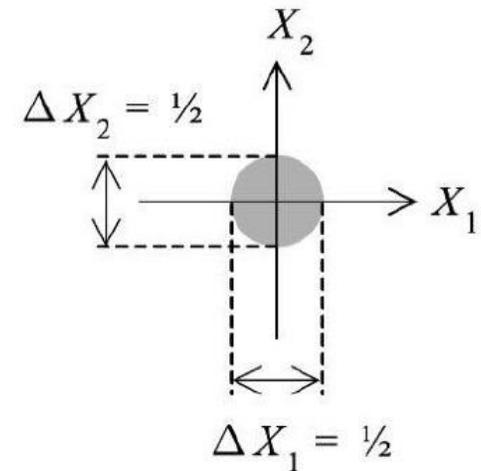
Mark Fox, Quantum Optics

## Vacuum Field I (Fox 7.4)

- Zero-point energy of QHO is  $(1/2)\hbar\omega$
- Quantum optics: this energy from randomly fluctuating field called vacuum field (present everywhere)
- Equating zero-point energy of QHO to time-averaged

energy of E and B fields gives, 
$$E_{\text{vac}} = \sqrt{\frac{\hbar\omega}{2\epsilon_0 V}}$$

- Uncertainties in the two quadratures equal the minimum allowed, **minimum uncertainty state**  $\Delta X_1^{\text{vac}} = \Delta X_2^{\text{vac}} = \frac{1}{2}$



**Fig. 7.4** Phasor diagram for the vacuum state. The uncertainties in the two field quadratures are identical, with  $\Delta X_1 = \Delta X_2 = 1/2$ . Note that this figure is essentially the same as Fig. 7.3(a) except that the uncertainty circle is displaced to the origin to account for the zero classical field of the vacuum.

Mark Fox, Quantum Optics

# Squeezed States (Fox 7.7)

- Can squeeze the uncertainty circle of vacuum or coherent state into ellipse of same area: quadrature-squeezed state
- Phase squeezed light allows interferometric measurements with greater precision
- Amplitude squeezed light allows lower amplitude noise
  - has sub-Poissonian statistics
- Could squeeze along any angle
- Could also make photon number state where  $\Delta n = 0$  and phase is completely undefined!

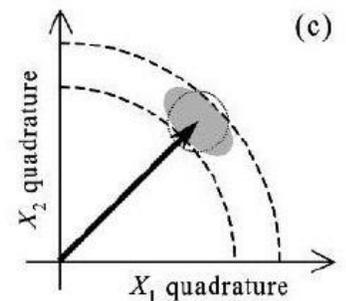
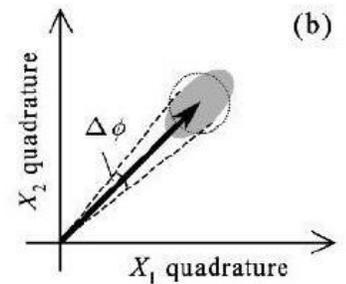
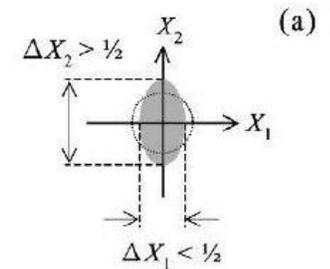
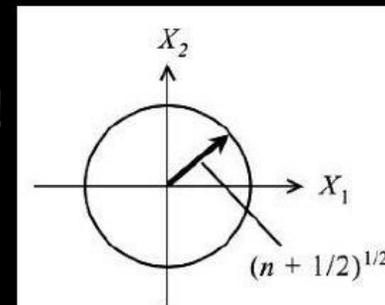


Fig. 7.8 Quadrature squeezed state (a) Squeezed vacuum. (b) Phase squeezed light. (c) Amplitude-squeezed light. The dotted circle in each of the diagrams shows the quadrature uncertainty of the vacuum/coherent state.

# Michelson interferometer quantum noise

## Shot Noise

$$\psi = \frac{\psi_{in}}{2} \left( e^{ikaL} - e^{-ikaL} \right) + \frac{\phi_{in}}{2} \left( e^{ikaL} + e^{-ikaL} \right)$$

$$= i \psi_{in} \sin kaL + \phi_{in} \cos kaL$$

near fringe:  $\psi = \phi_{in} + ikaL \psi_{in}$

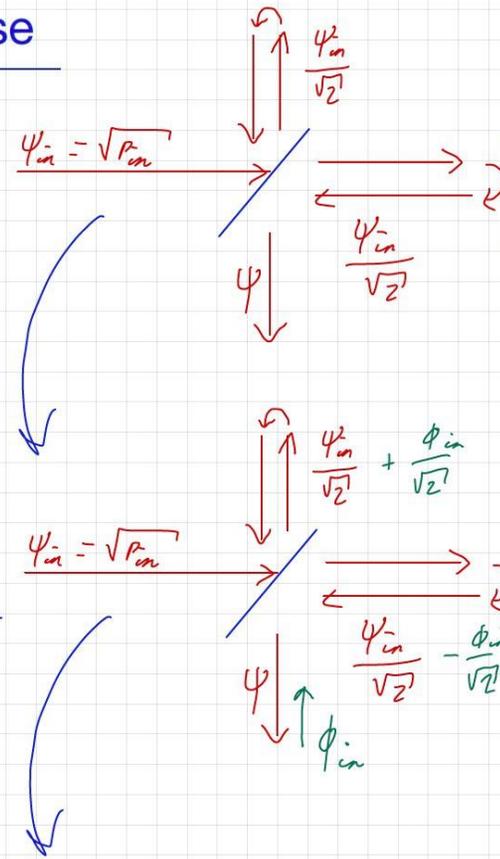
$$P = |\psi|^2 = (kaL)^2 \psi_{in}^2 - 2 \Im (kaL \phi_{in} \psi_{in}^*) + |\phi_{in}|^2$$

$$\delta P = 2k^2 aL \delta L - 2kaL \Im (\phi_{in} \psi_{in}^*)$$

$$= 2kaL \left( k \delta L - \Im (\phi_{in} \psi_{in}^*) \right)$$

$$\Im (\phi_{in} \psi_{in}^*)$$

Is shot noise quadrature



## Radiation Pressure Noise

$$F = \frac{2(P_x - P_y)}{c}$$

$$P_x - P_y = \left| \frac{\psi_{in}}{\sqrt{2}} + \frac{\phi_{in}}{\sqrt{2}} \right|^2 = \frac{1}{2} P_{in} + \underset{(-)}{\text{Re}(\psi_{in}^* \phi_{in})}$$

$$F = \frac{4 \text{Re}(\psi_{in}^* \phi_{in})}{c}$$

$$\text{Re}(\phi_{in} \psi_{in}^*)$$

Is radiation pressure  
noise quadrature

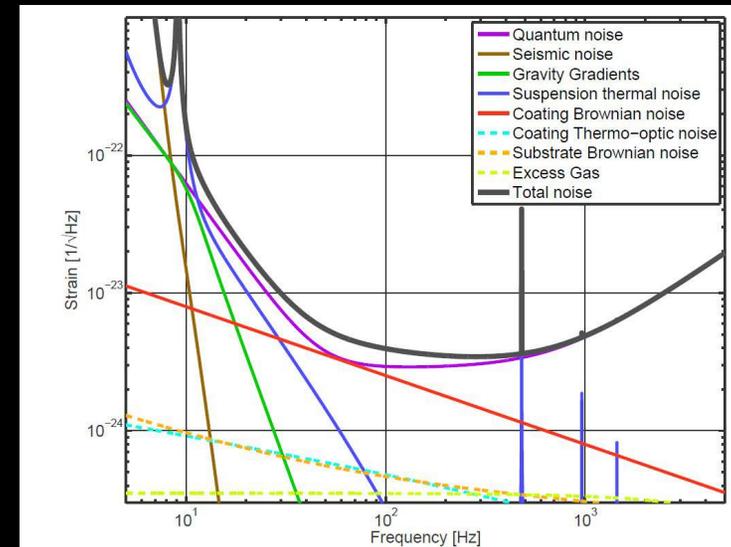
# How to calculate quantum noise in any interferometer

- Calculate optical input-output relations for all ports of the interferometer (dark port, bright port)
- Send in normal vacuum state at every port:

$$\frac{1}{2} \hbar \omega$$

in each quadrature

- Propagate to the output.

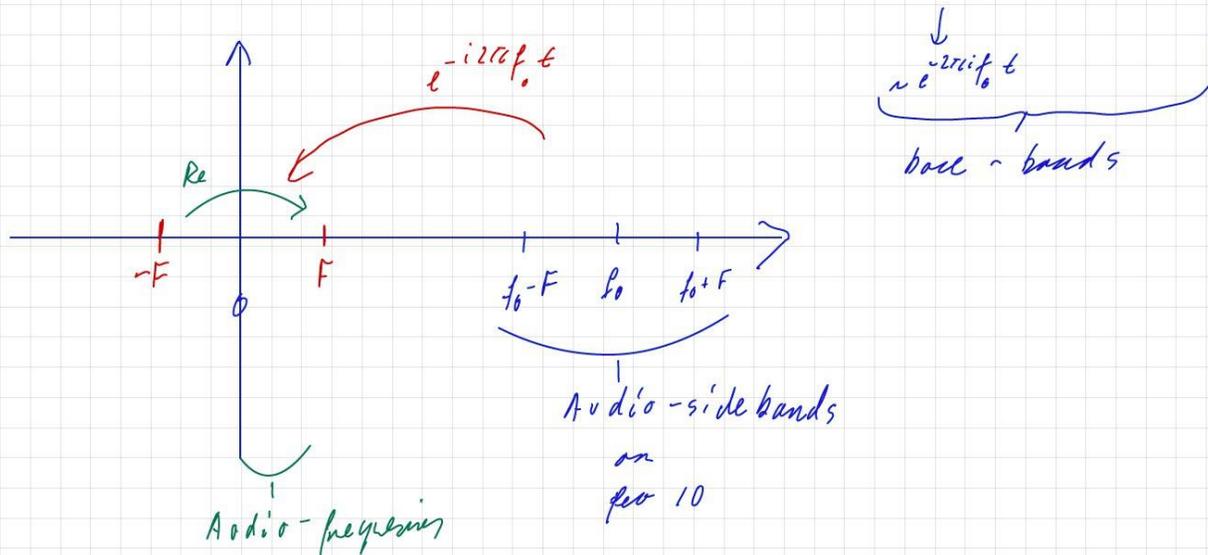


## Quantum Power Spectral Density and Two-photon Squeezing

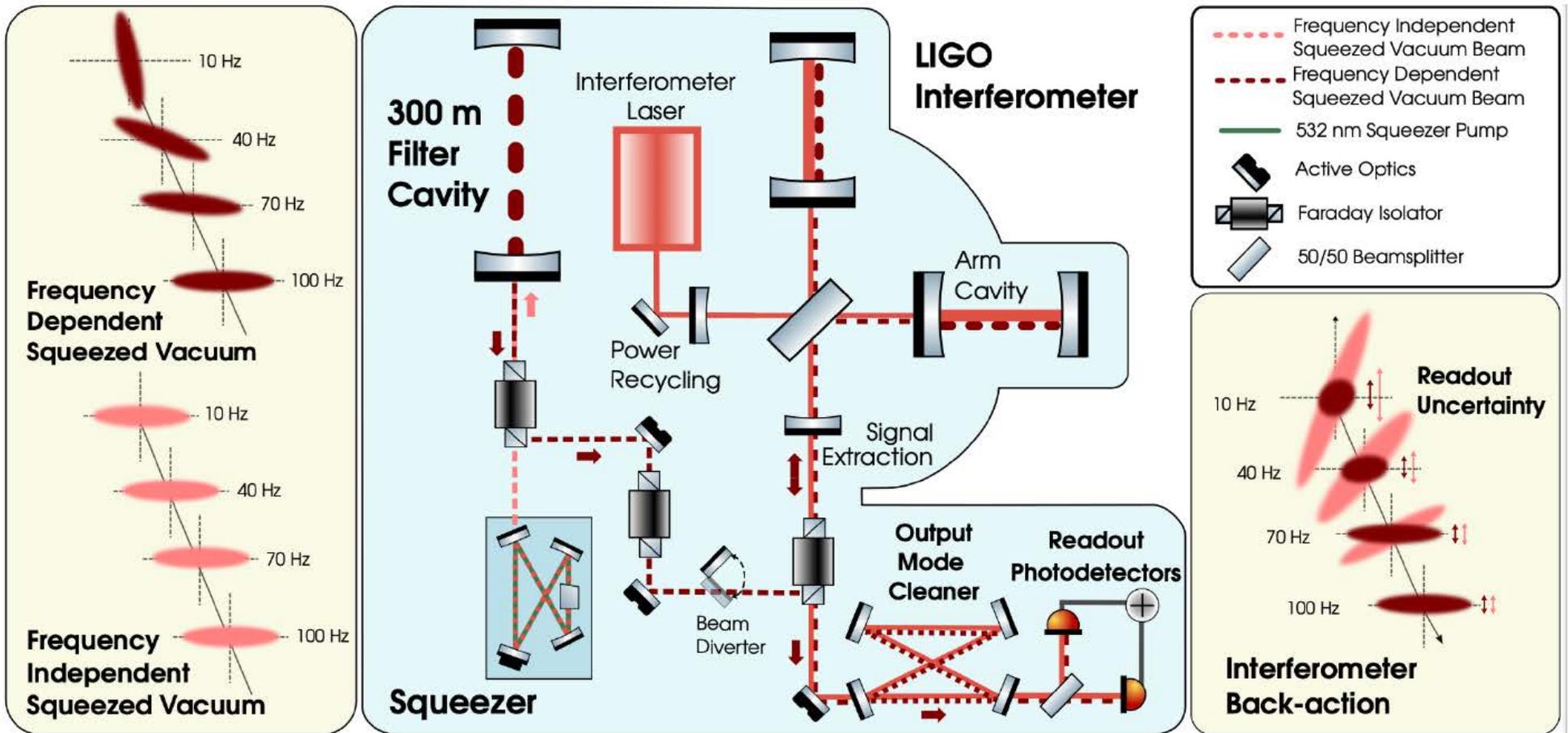
$$\psi = \psi_0 + \delta\psi_1 + i\delta\psi_2$$

Amplitude quadrature  $\downarrow$  Phase quadrature  
 $\uparrow$  carrier  $\nwarrow$  fluctuations at all frequencies

$$P = |\psi|^2 = |\psi_0|^2 + 2\text{Re}(\psi_0^* \delta\psi_1) = |\psi_0|^2 + 2\text{Re}\psi_0^* \int df \delta\psi_1(f)$$



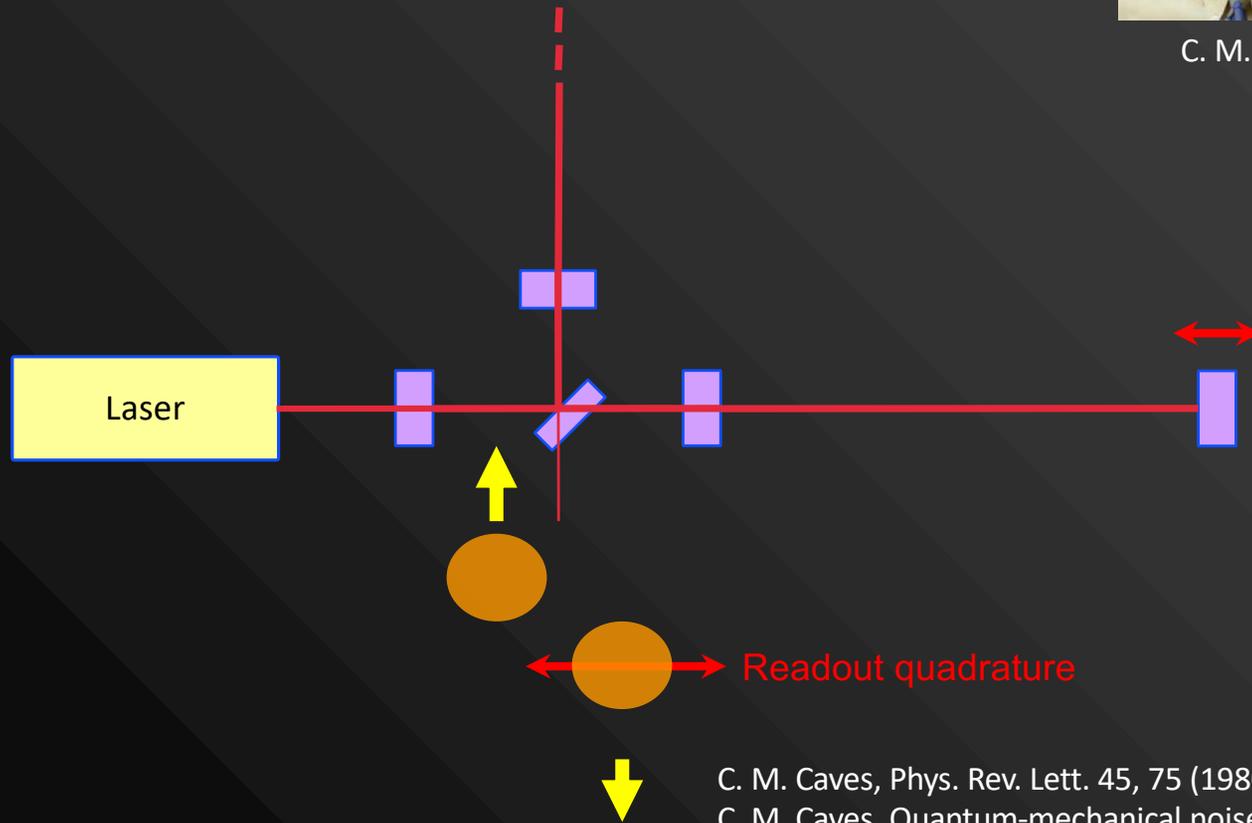
# Frequency Dependent Squeezing



# Beyond Quantum Noise



C. M. Caves

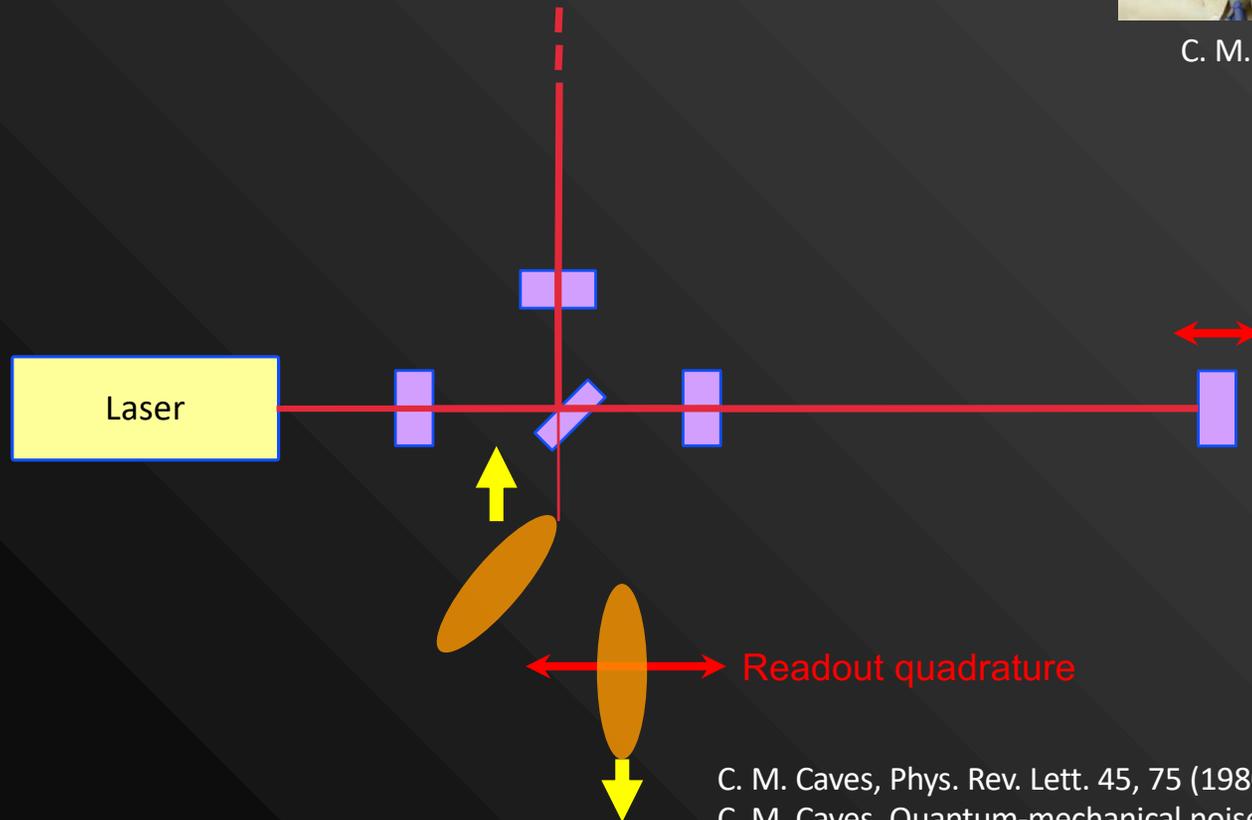


C. M. Caves, Phys. Rev. Lett. 45, 75 (1980).  
C. M. Caves, Quantum-mechanical noise in an  
interferometer. Phys. Rev. D 23, p. 1693 (1981).

# Beyond Quantum Noise



C. M. Caves



C. M. Caves, Phys. Rev. Lett. 45, 75 (1980).  
C. M. Caves, Quantum-mechanical noise in an  
interferometer. Phys. Rev. D 23, p. 1693 (1981).

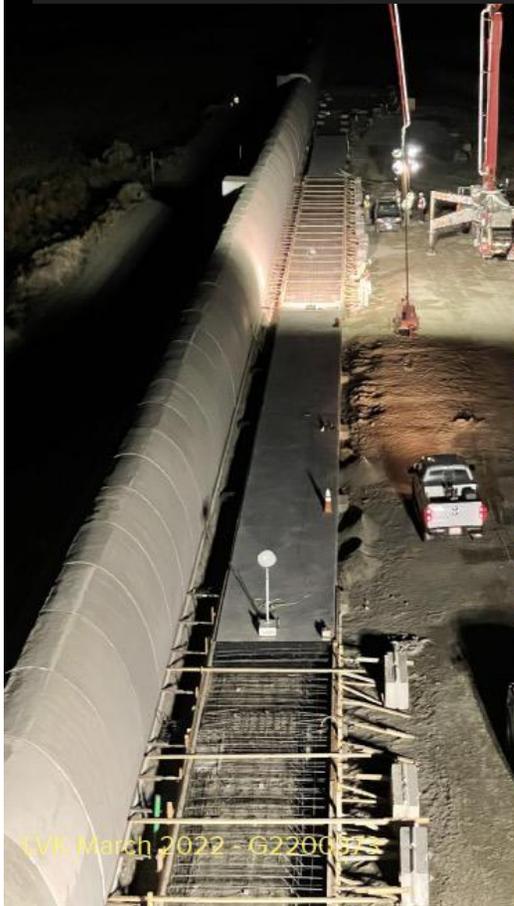
October 2021

December 2021

p/c Bubba Gately, LHO

February 2022

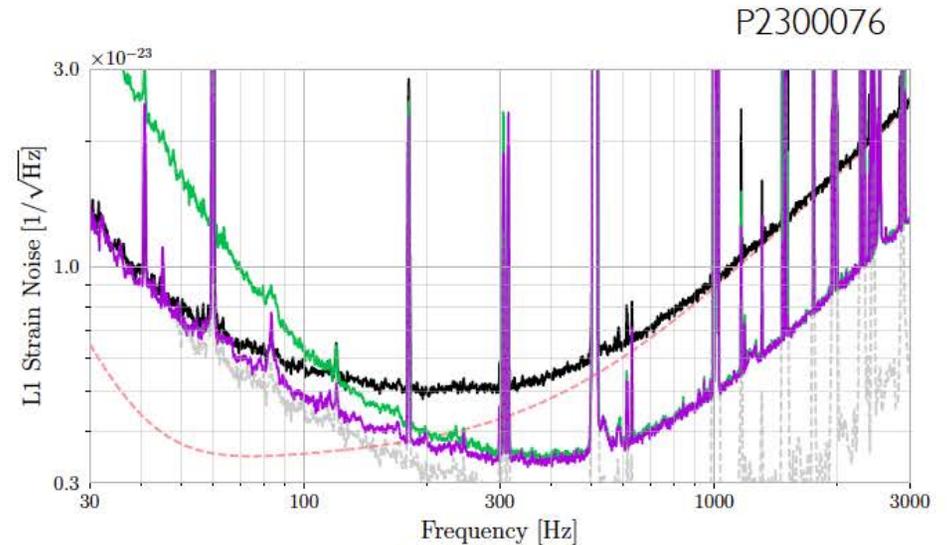
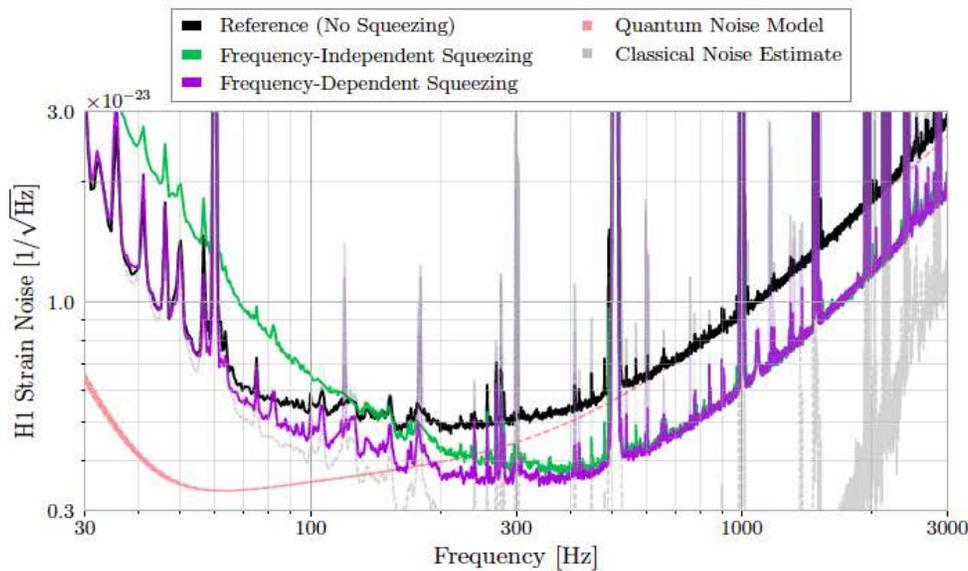
# Key Pieces of LIGO A+ done: Freq. Dep. Squeezing in O4!



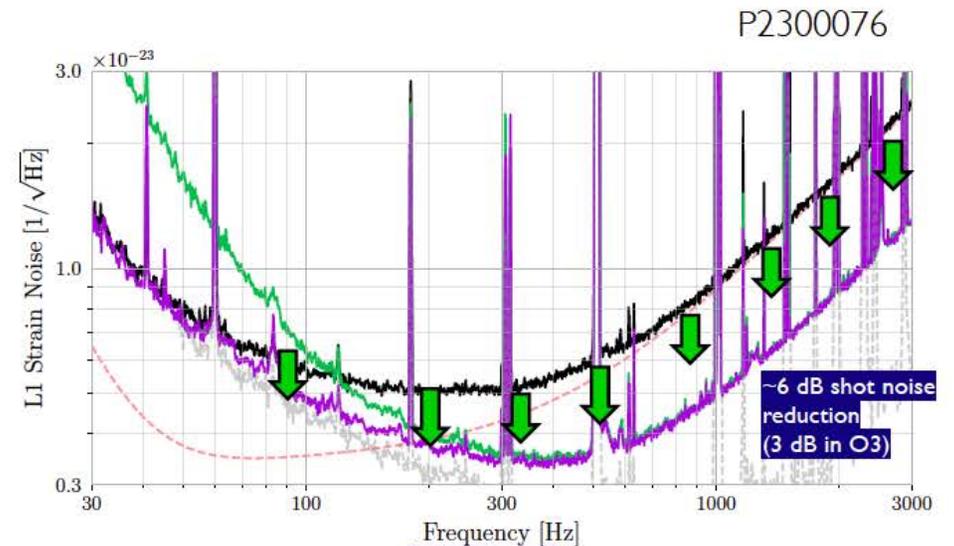
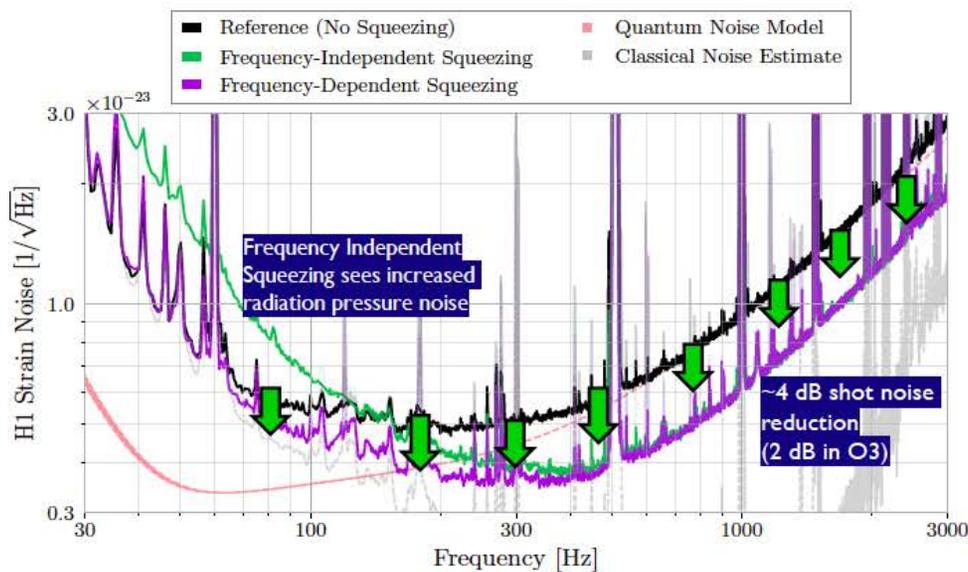
LVK March 2022 - G2200373

Slide from Vicky Xu : DCC-G2200373

# Frequency Dependent Squeezing in O4



# Frequency Dependent Squeezing in O4





Where do we  
go from here?

“Recently, we have waded a little out to sea,  
enough to dampen our toes or, at most, wet our  
ankles. The water seems inviting. The ocean calls.”

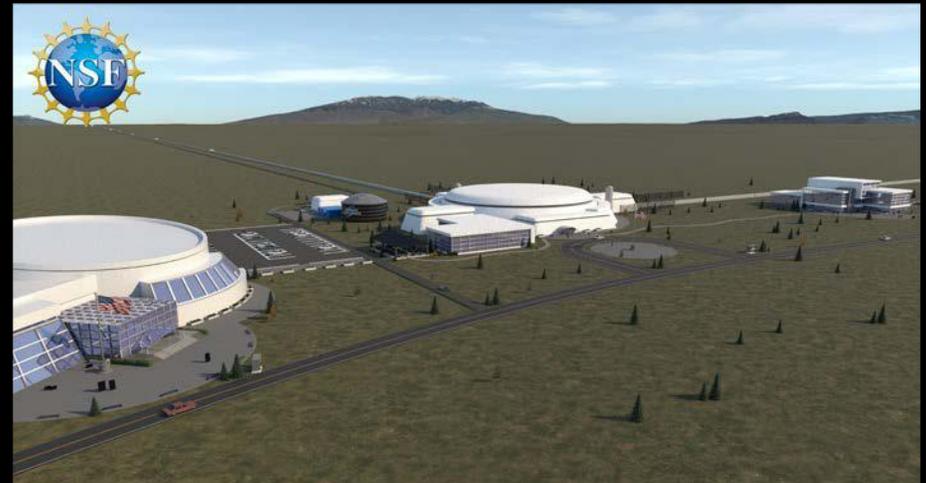
Carl Sagan

# Cosmic Explorer

Stefan Ballmer

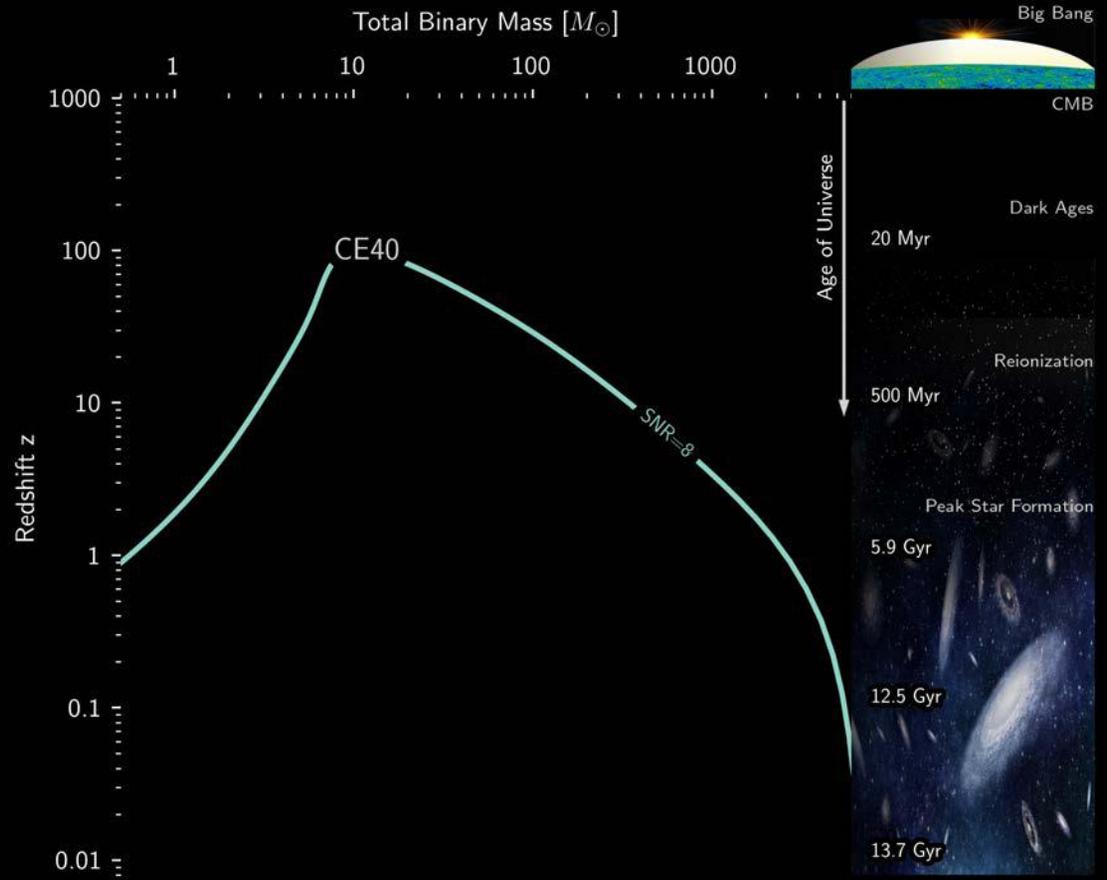
The US Vision for Gravitational-Wave Astrophysics

- Next-Generation Gravitational-Wave Observatory
  - 40 km and 20 km L-shaped surface observatories
  - 10x sensitivity of today's observatories
  - Global network together with European Einstein Telescope
- Enables access to
  - Stellar to intermediate mass mergers throughout Cosmic Time
  - Dynamics of Dense Matter
  - Extreme Gravity



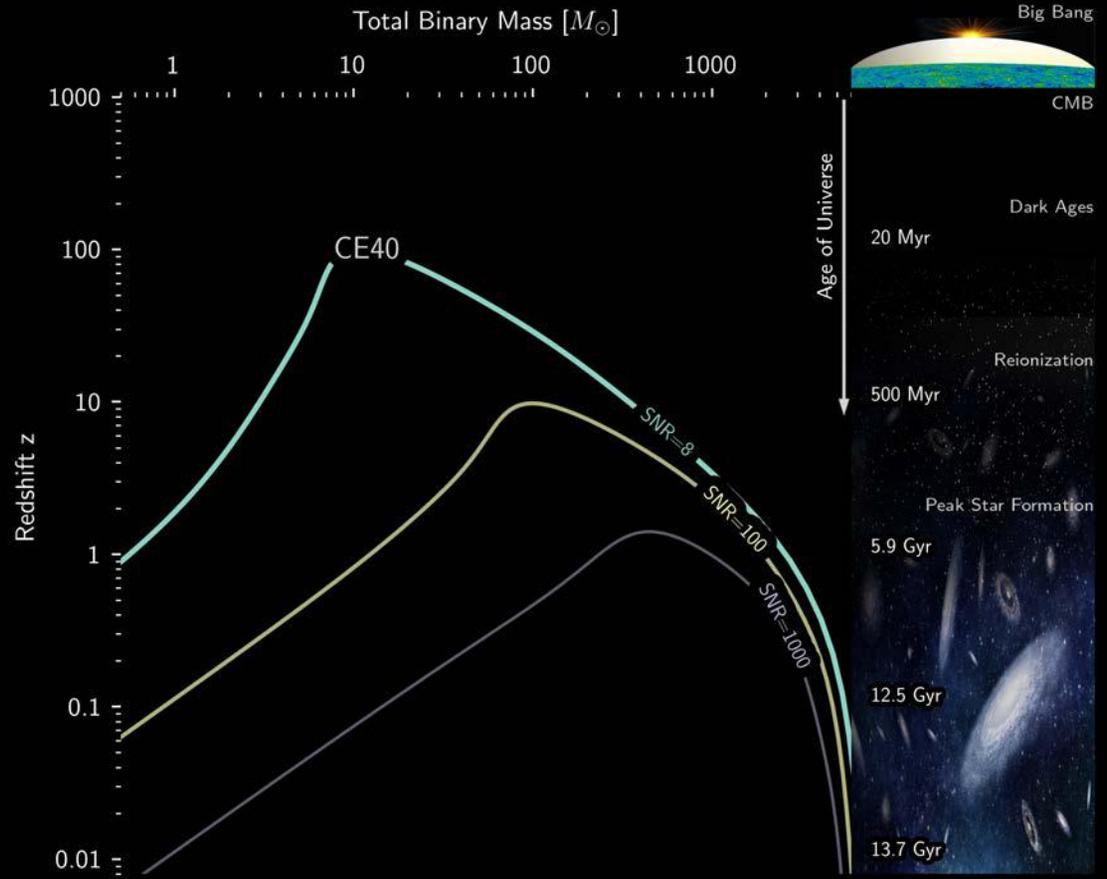


Reaching the Far Shores of the Cosmic Ocean



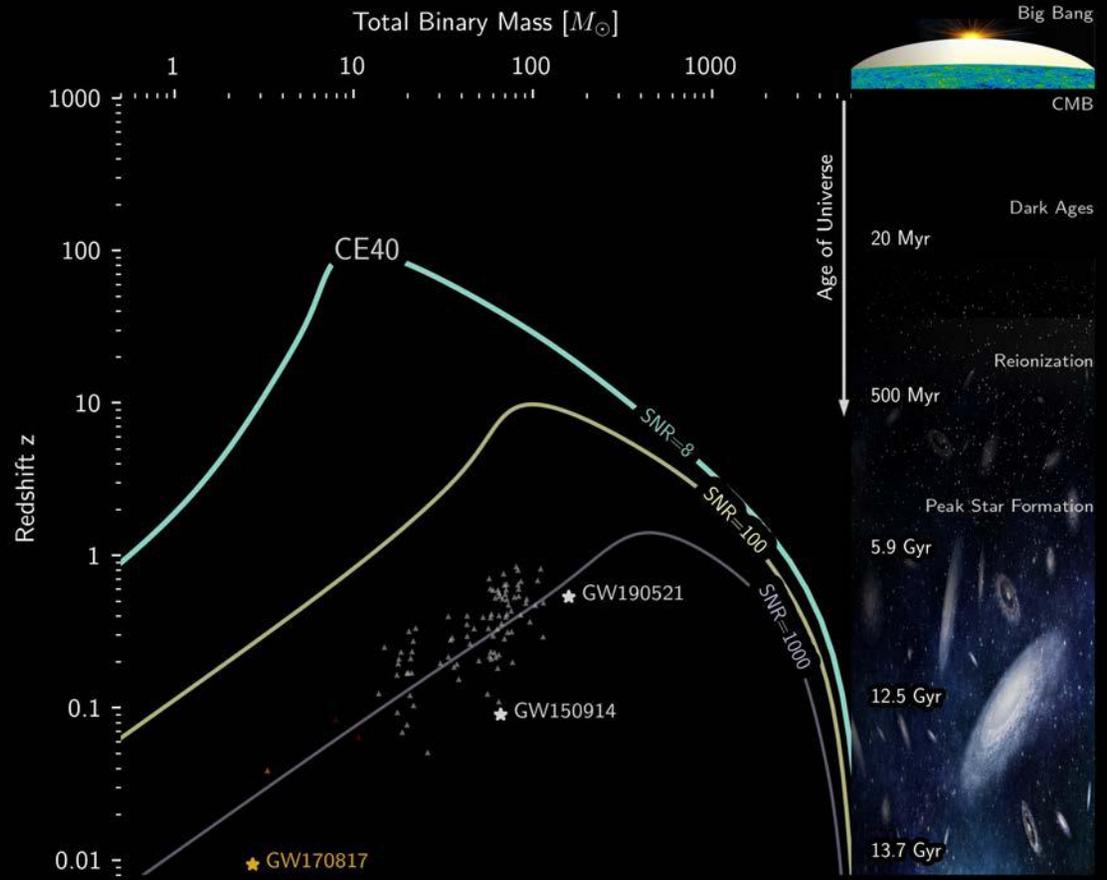


Reaching the Far Shores of the Cosmic Ocean



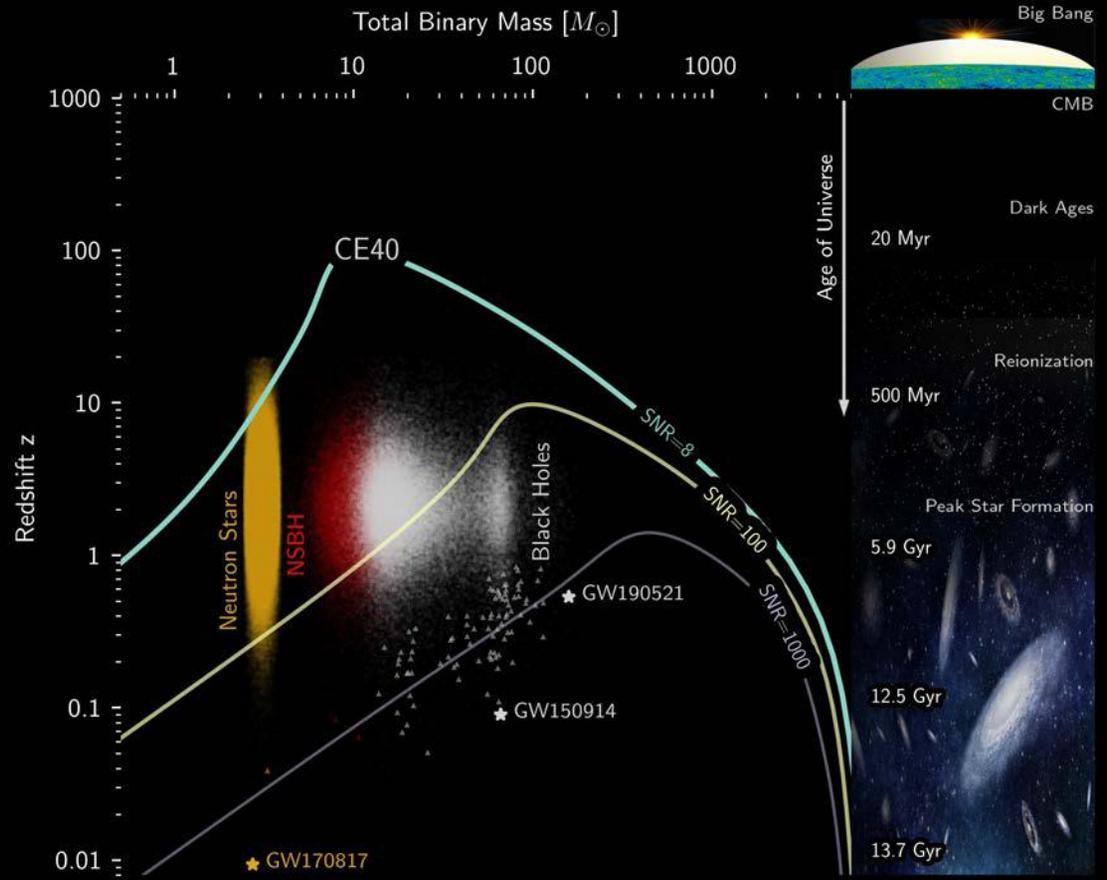


Reaching the Far Shores of the Cosmic Ocean



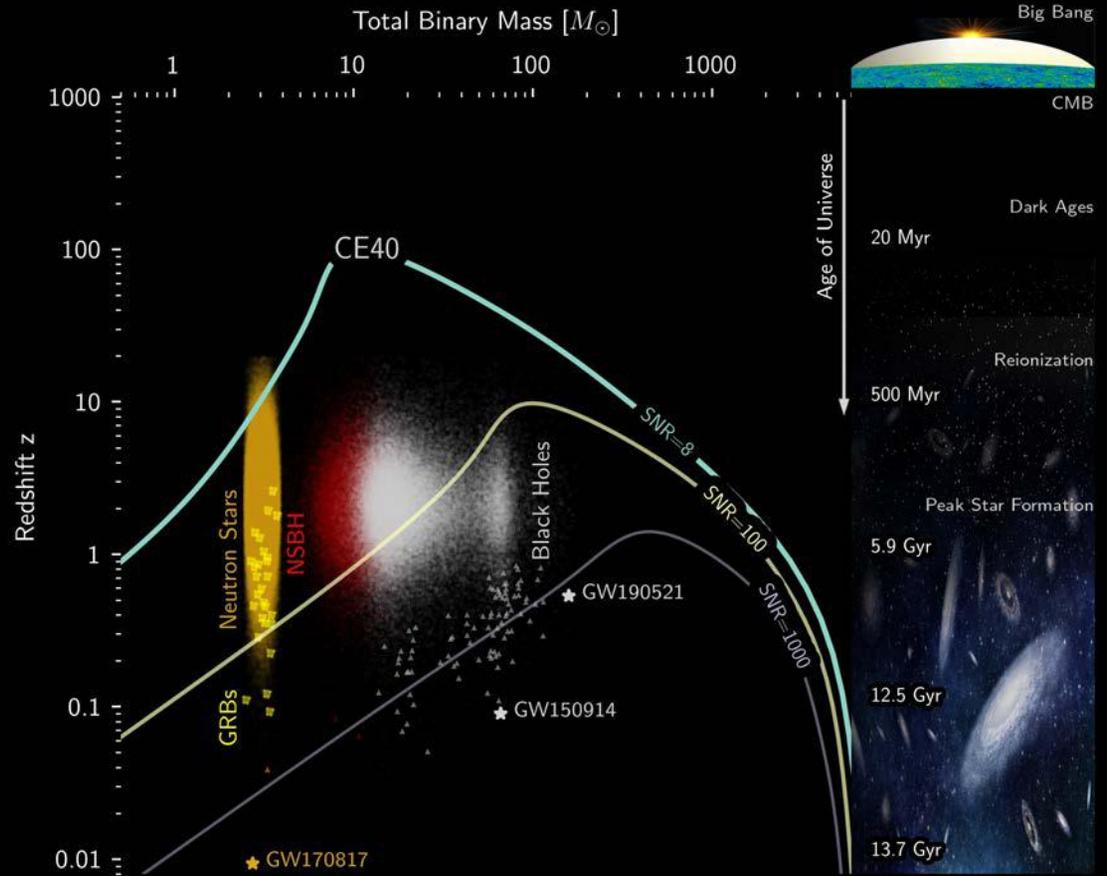


Reaching the Far Shores of the Cosmic Ocean



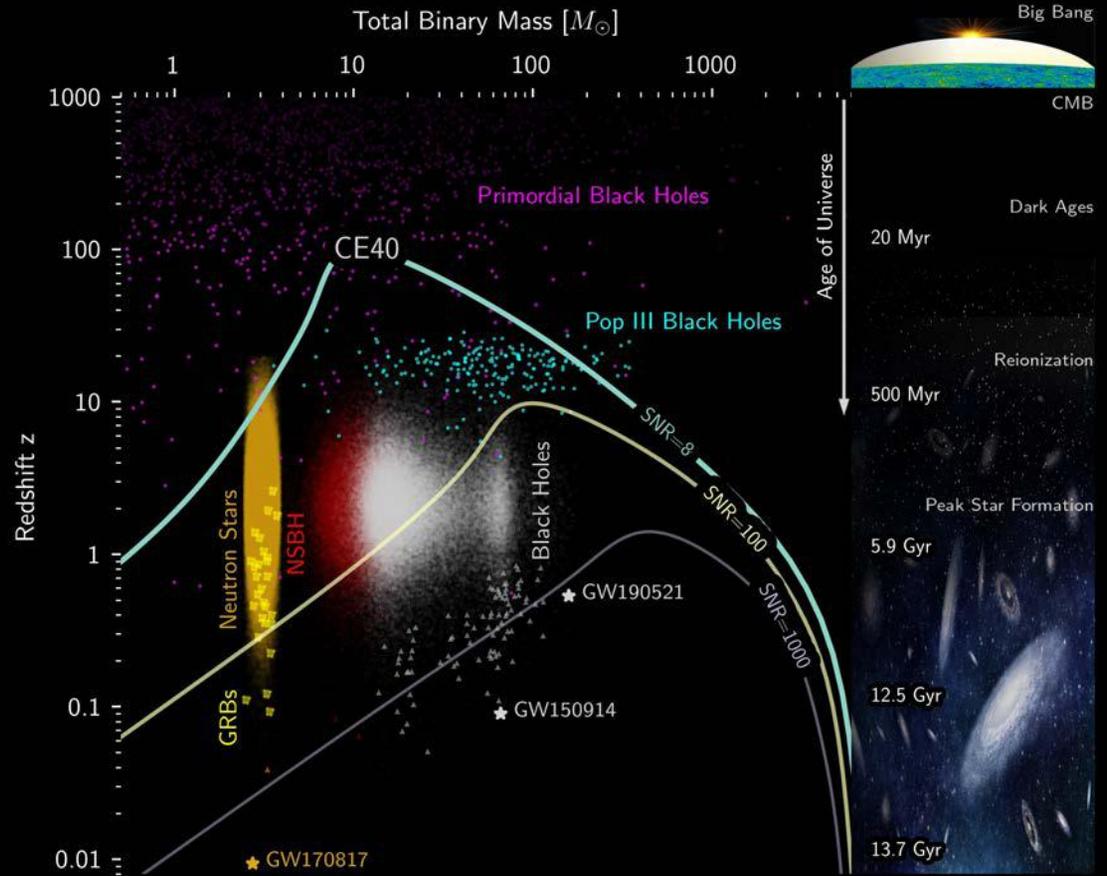


Reaching the Far Shores of the Cosmic Ocean





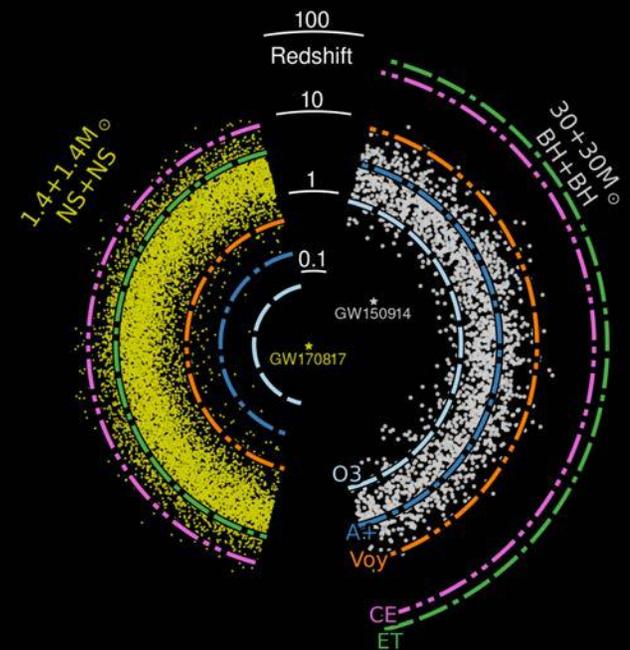
Reaching the Far Shores of the Cosmic Ocean





# Cosmology with Cosmic Explorer

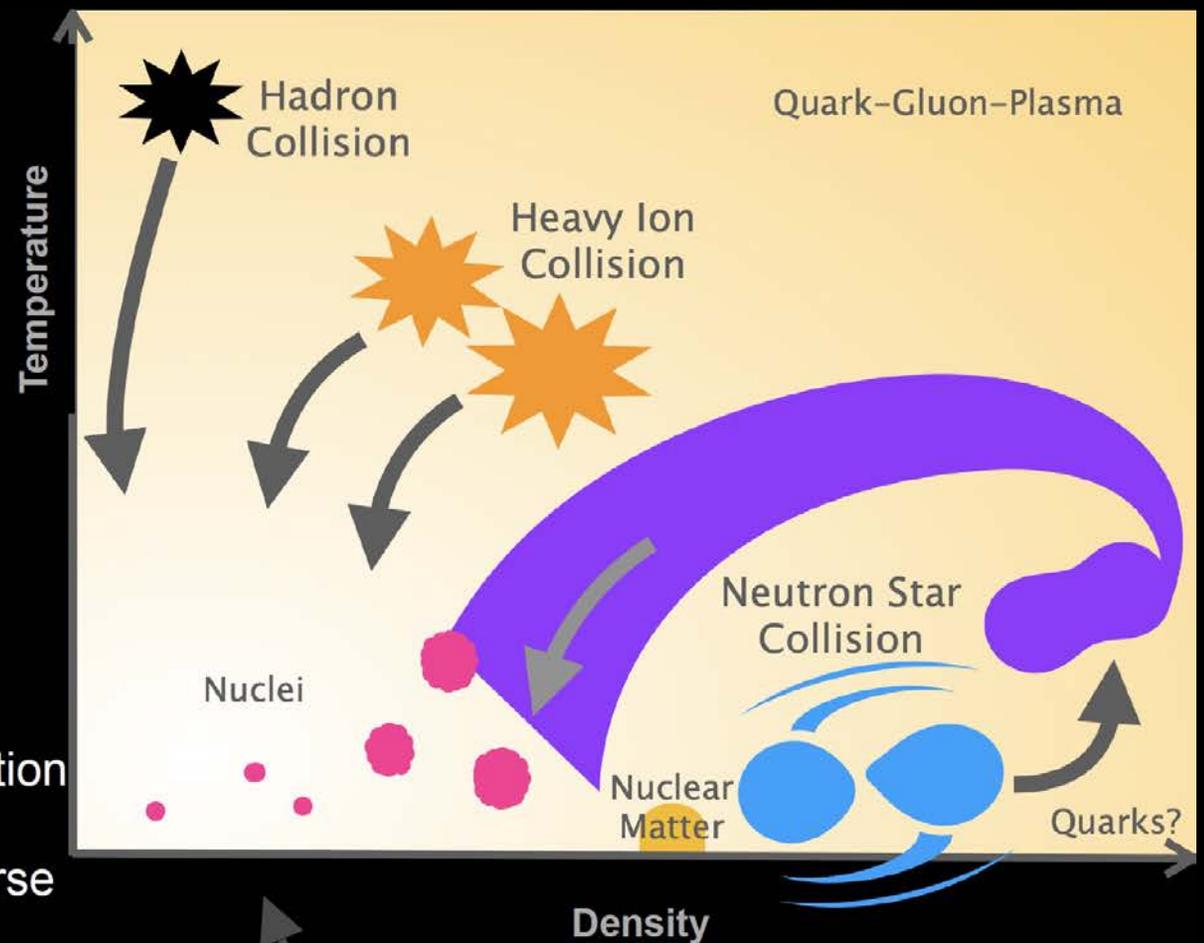
- Expected event rate
  - $O(1e5)$  BHBH merger annually
  - $O(1e6)$  NSNS mergers annually
- Across redshifts up to  $O(30)$ 
  - Sky localization from detector network
- The full Cosmic Explorer data set is a treasure trove for structure formation studies



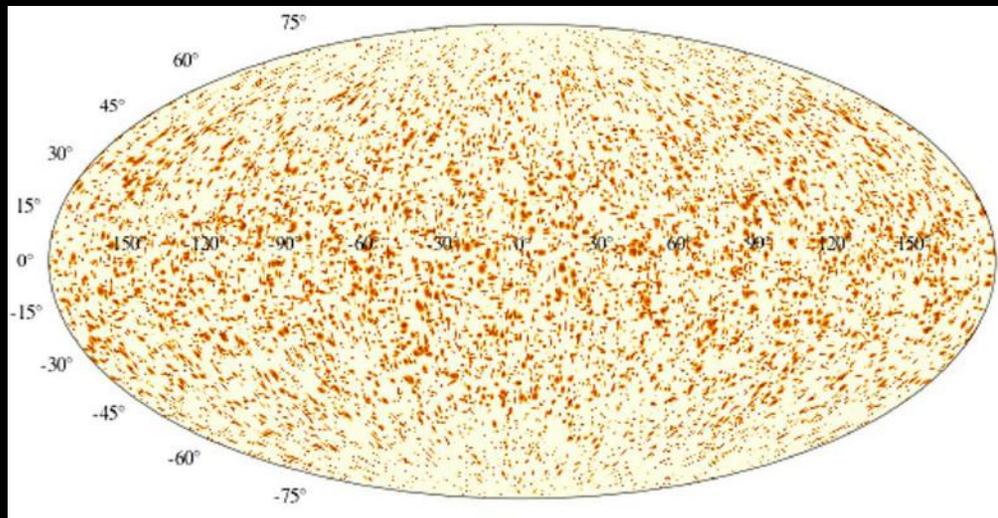
# Dynamics of dense matter

*How does matter behave under the most extreme conditions in the universe?*

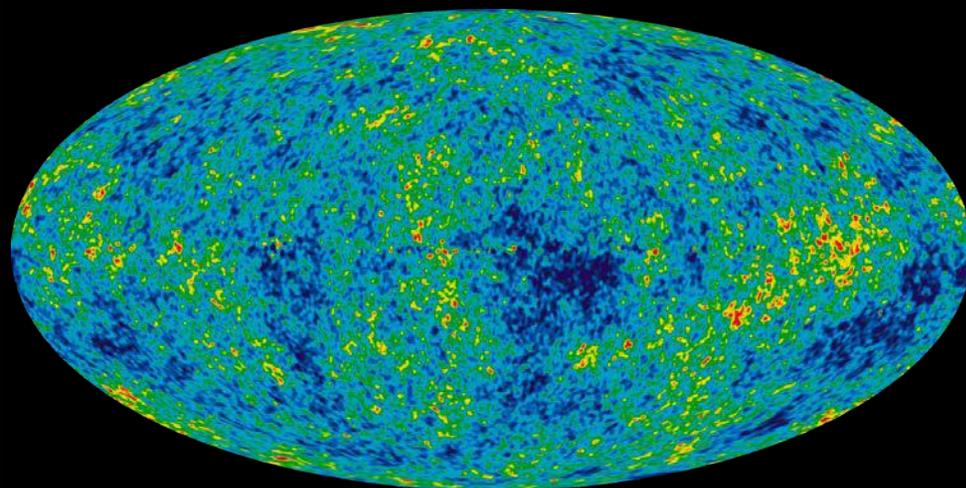
- Neutron star structure, composition
- New phases of dense matter
- Chemical evolution of the universe
- Gamma-ray bursts and jets



# Detecting Baryon Acoustic Oscillations



Combined posterior field 1 year 3G detector network

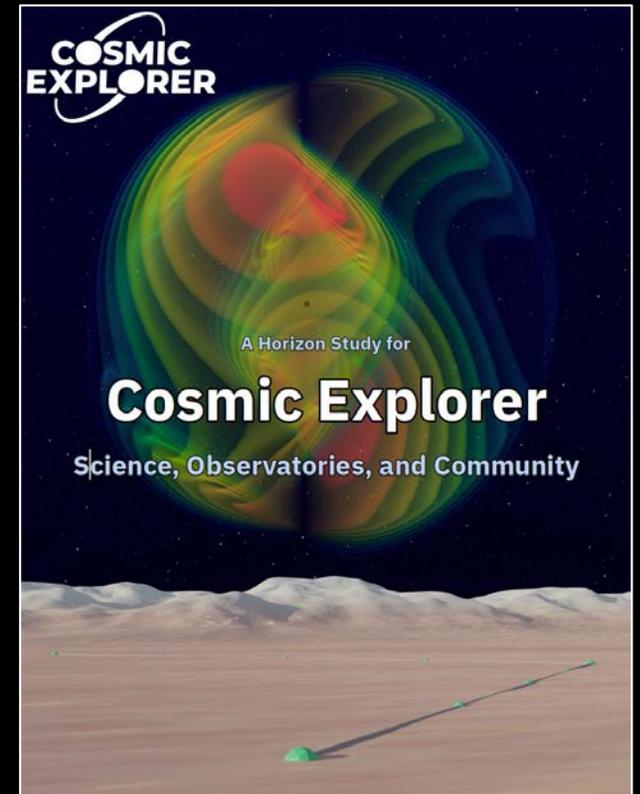


CMB - WMAP

$$\theta \sim \frac{r_s}{(1+z)D_A(z)}$$

# Cosmic Explorer Updates

- Horizon Study for more information available at:
  - <https://arxiv.org/abs/2109.09882>
  - <https://cosmicexplorer.org>
- CE is as envisioned an **NSF-funded Project**
  - **Initial design funding** for 3 years at ~ **USD 9M...**
  - Institutions involved (alphabetically):  
Caltech, CSU Fullerton, **MIT (lead)**, Syracuse University,  
University of Arizona, University of California Riverside,  
University of Florida, University of Minnesota, University of  
Oregon





# Design and Hardware for Cosmic Explorer

# Overview of CE Design and Research Activities

- **Funded NSF awards:**
  - “Launching the Cosmic Explorer Conceptual Design”
  - “Collaborative Research: Identifying and Evaluating Sites for Cosmic Explorer”
  - “Cosmic Explorer Optical Design”
  - “Enabling Megawatt Optical Power in Cosmic Explorer”
  - “Local Gravity Disturbances and Next-Generation Gravitational-Wave Astrophysics.”
  - “Cosmic Explorer: Research and Conceptual Designs for Scattered-Light Mitigation.”
- **Other related funded awards partly supporting Cosmic Explorer:**
  - Observational Science (consortium driven)
  - Vacuum system research
  - Center for Coatings Research
  - Suspension design (A#)



# CE Retreat, Minnowbrook, NY, Oct 15-19, 2023

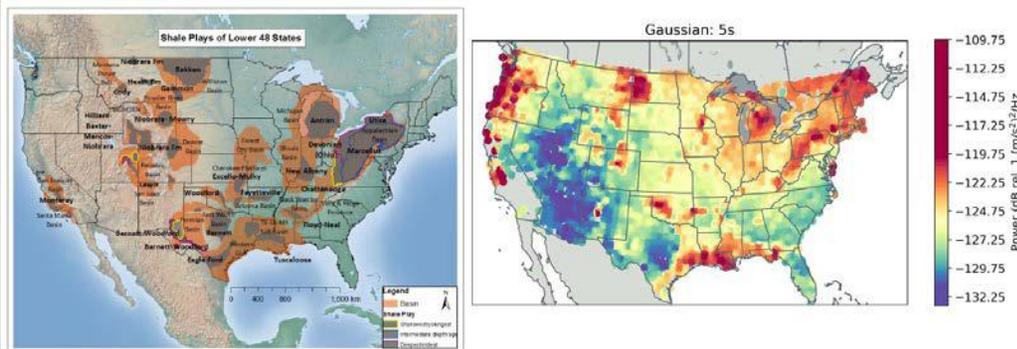
- Workshop to kick off design work for Cosmic Explorer
  - Site search for Cosmic Explorer
  - Optical and Thermal design
  - Project management and international collaborations



# Identifying and Evaluating Sites for Cosmic Explorer

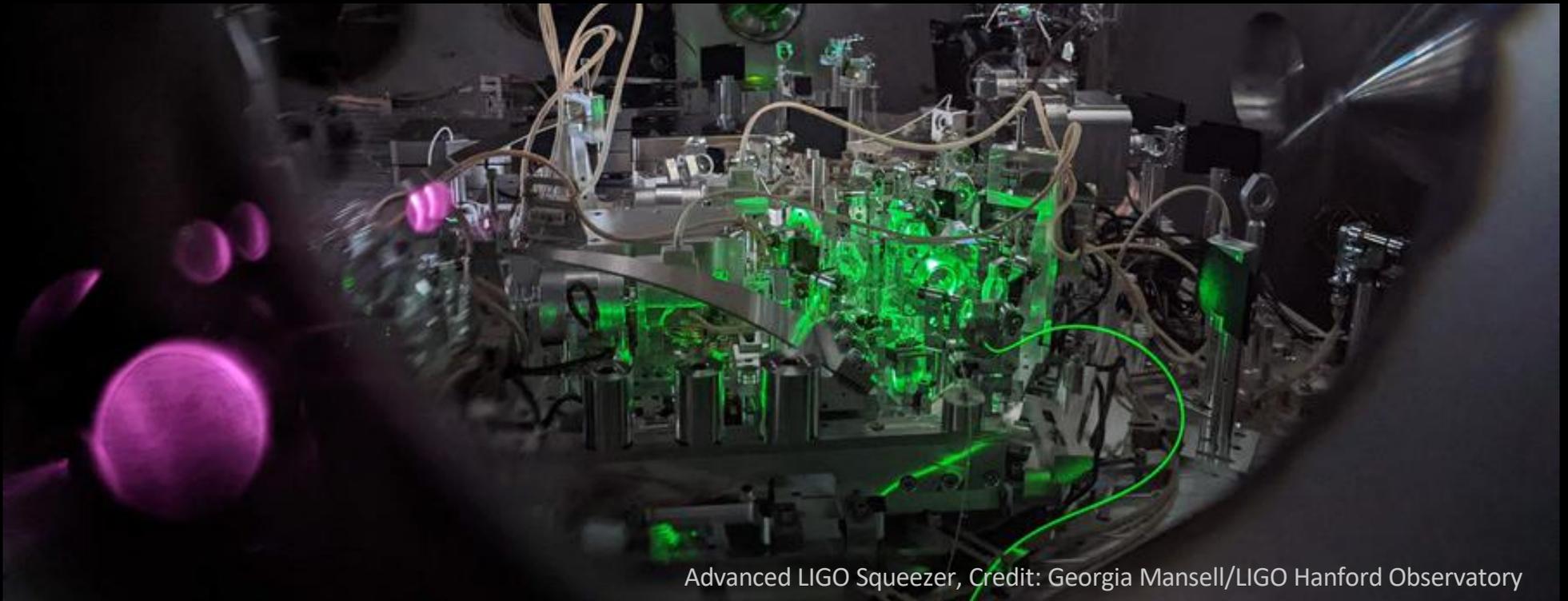
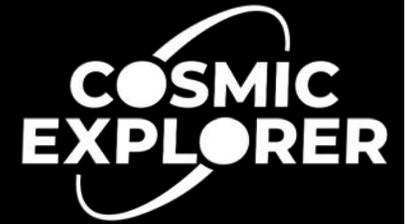
- Identification and evaluation of the most promising locations for CE observatories while developing protocols
- Many considerations:
  - Site Topography
  - Seismicity
  - Land ownership and Indigenous People Partnership
  - Long-term suitability and Economic Impact
- Initial candidate site selection in progress

0.2 Hz energy compared to basin locations



Sedimentary Basin Seismic Response  
Joshua Russell, Syracuse University

# Cosmic Explorer Optical Design



Advanced LIGO Squeezer, Credit: Georgia Mansell/LIGO Hanford Observatory

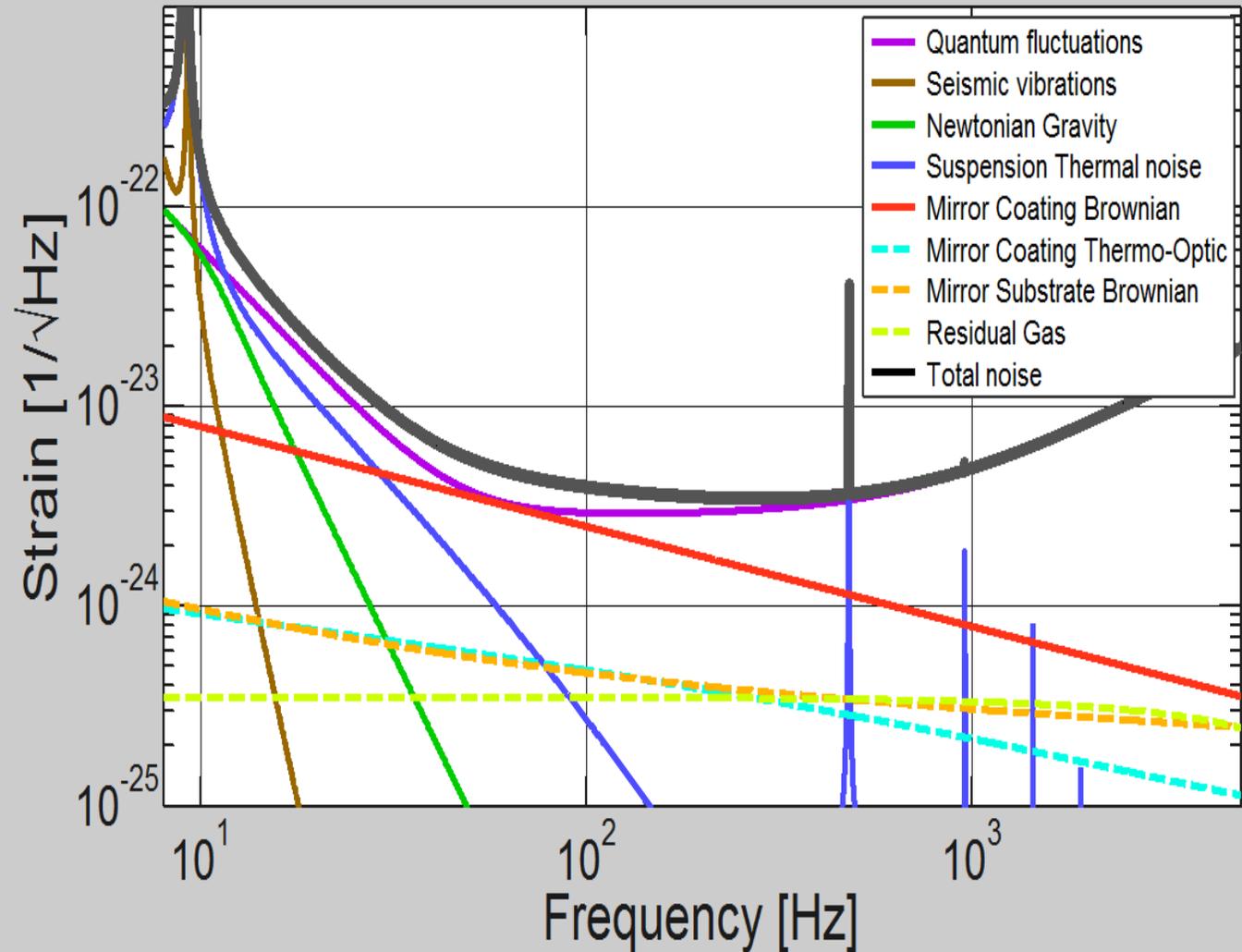
# GWADW 2013

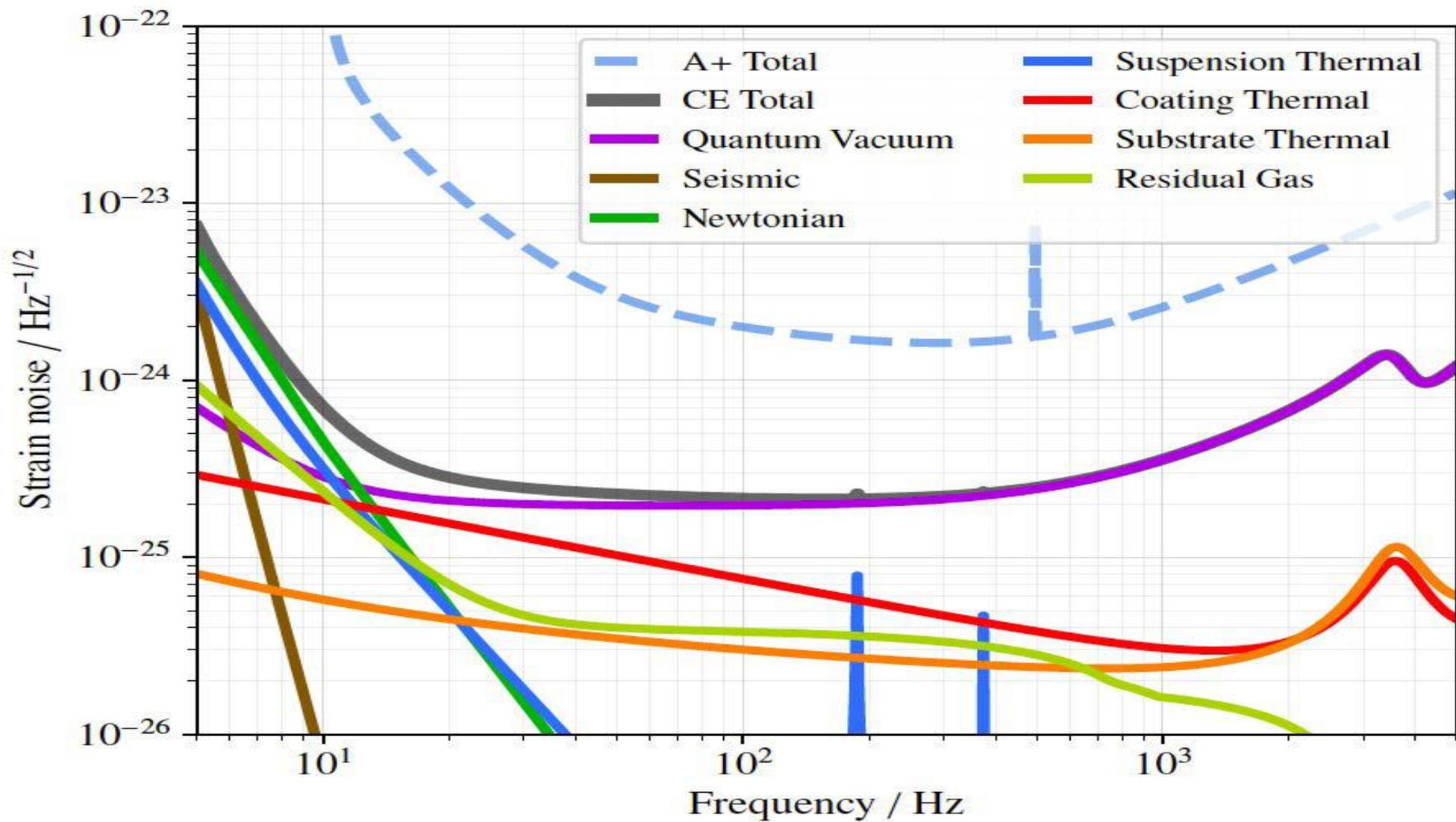
Talk on final day  
May 24, 2013

Advanced LIGO  
noise budget

Scaled to longer  
arm length

Range: 190Mpc; L: 4 km (aLIGO: 178 Mpc)





## Large Test masses

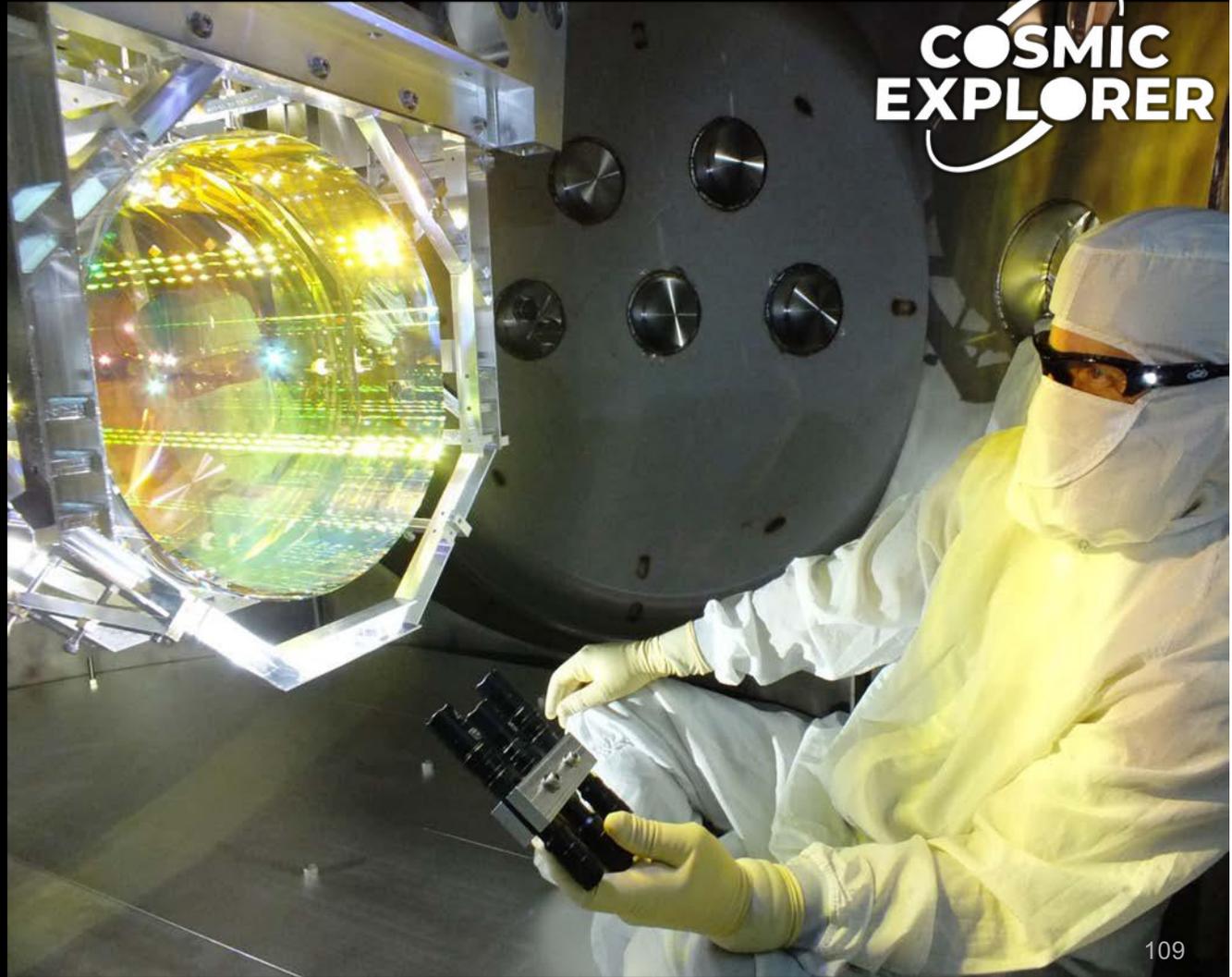
### **320 kg ultra-pure glass:**

Reduce thermodynamic fluctuations and heat-induced deformation

Research into fabrication techniques & metrology

### **Metal-oxide thin-film coatings:**

Turn test mass into a mirror with reflectivity  $>99.995\%$



# Configuration changes compared to Advanced LIGO

- Longer arm cavities (4km→40km)
- Larger test masses ( $m=40\text{kg}$ ,  $\varnothing=34\text{cm}$  →  $m=320\text{kg}$ ,  $\varnothing=70\text{cm}$  )
- 2<sup>nd</sup> input mode cleaner for frequency stabilization (arXiv:2107.14349)
- Scaled filter cavity (compared to A+)
- Homodyne readout (same as A+)
- Larger vacuum system (cost-critical)

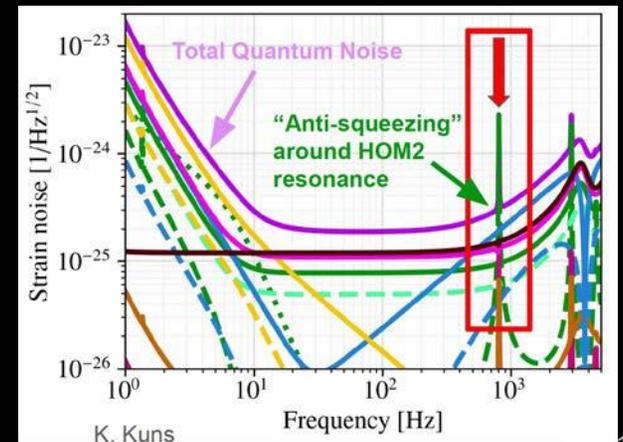
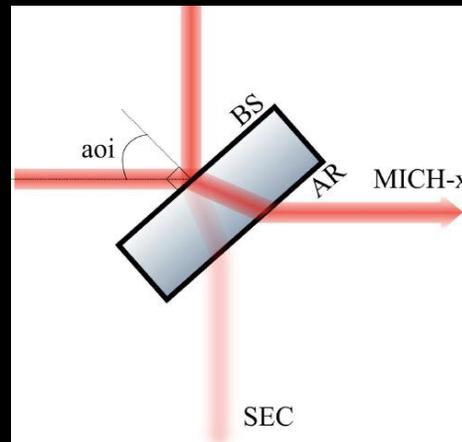
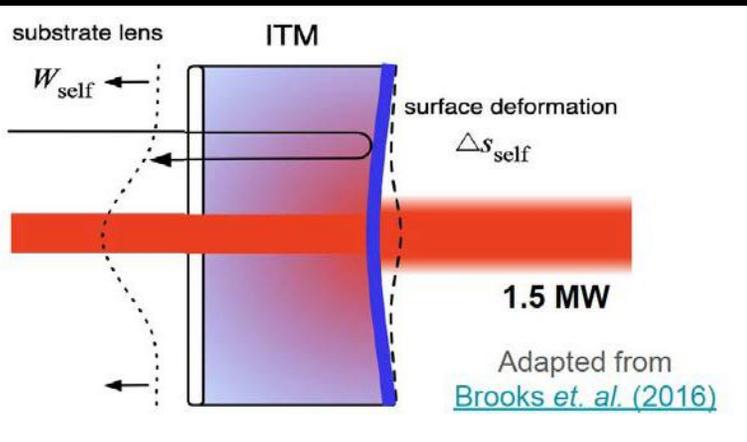


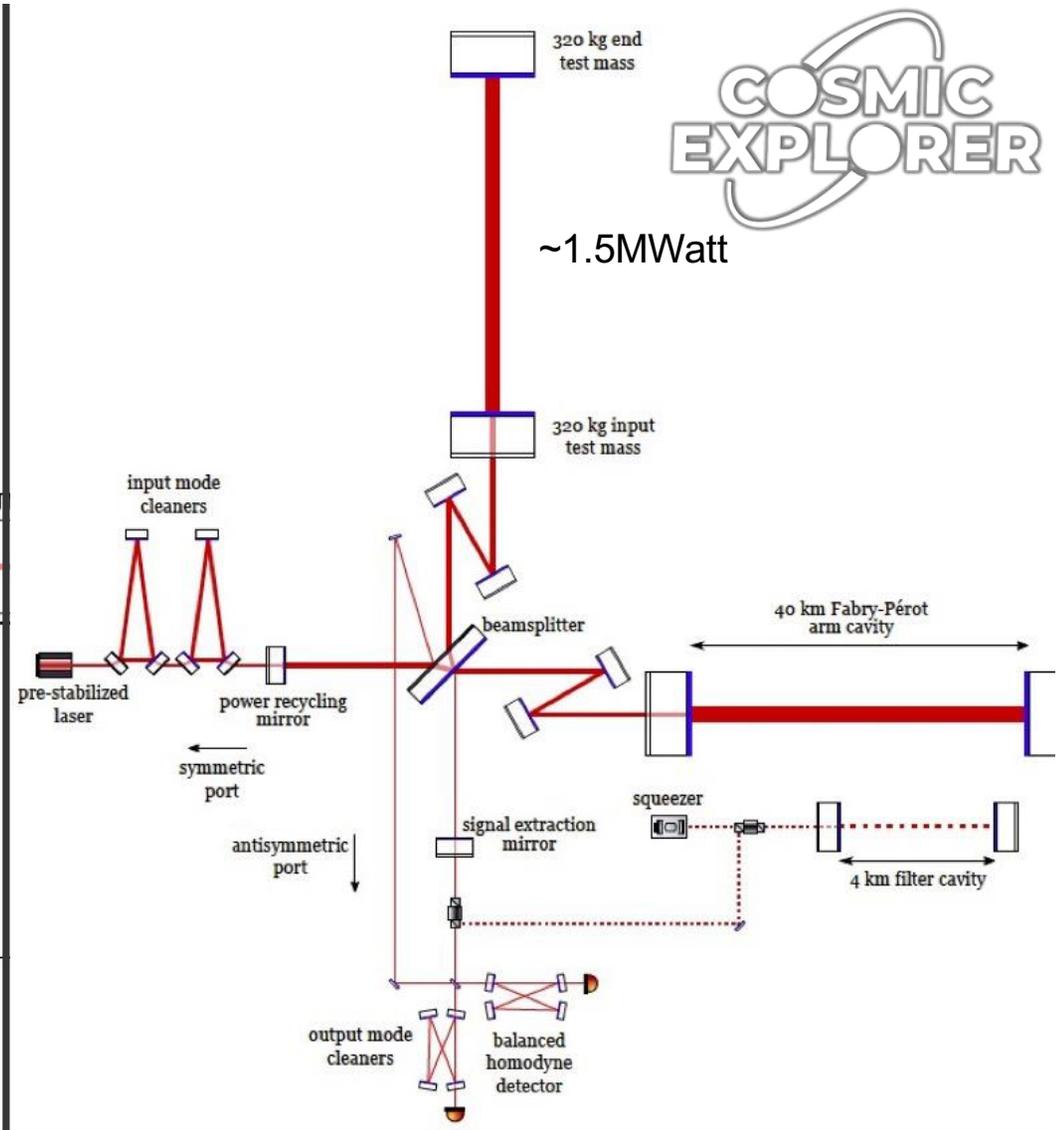
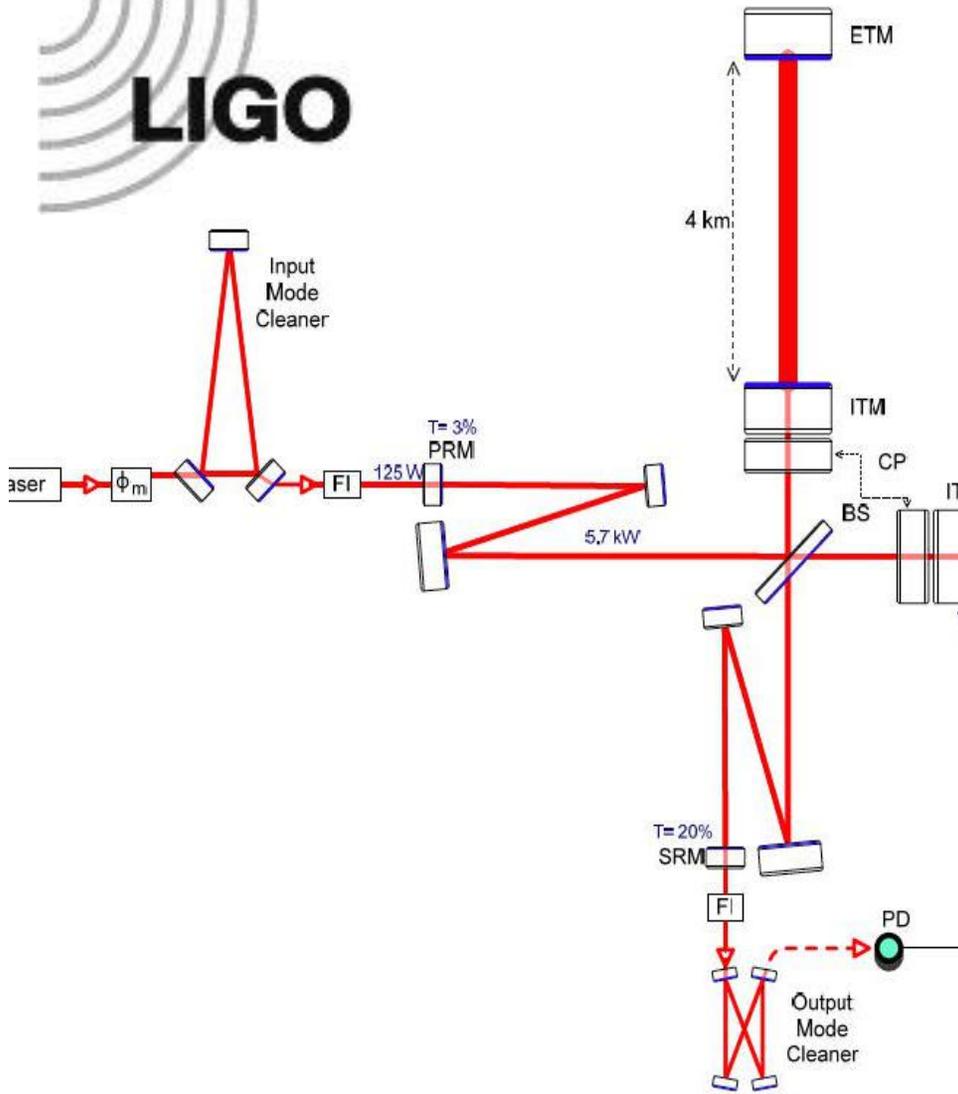
## Cosmic Explorer: Why Not Just Scale up LIGO Design?

- Unique challenges arise from a 10x longer arm length (CE-G2300033)
  - Minimum beam size for 40 km arms is  $\sim 12$  cm. For  $< 1$  ppm clipping loss on ITMs, require  $\sim 70$  cm ITMs. Beamsplitter should be  $\sqrt{2}$  bigger\* (at  $45^\circ$  AOI). 1 m diameter unfeasible?
    - ➔ Consider alternate layouts with a different beamsplitter location
- Signal Extraction Cavity (SEC) resonance approaches detection band with 40 km or 20 km arms
  - ➔ SEC length must be  $< 200$  m (40 km arms) or  $< 90$  m (20 km arms)
- FSR of 40 km arms is 3.75 kHz. With same arm finesse, DARM pole is 10x lower
  - ➔ Need 10x higher SEC finesse to recover same bandwidth

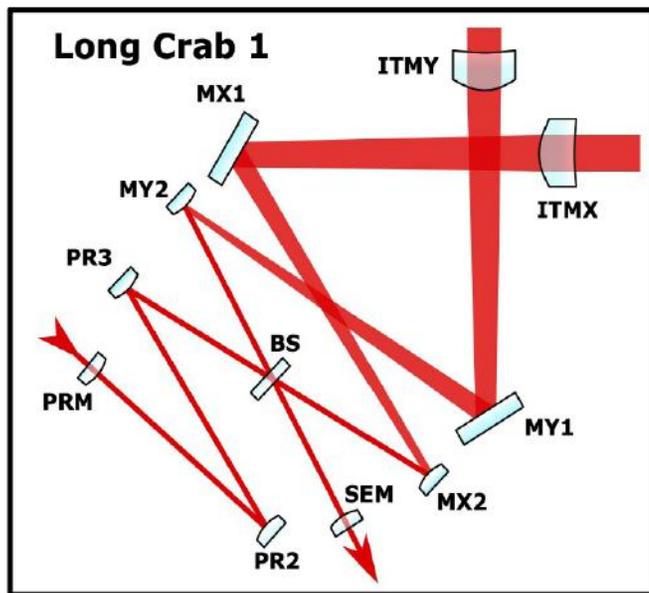
# Cosmic Explorer: Why Not Just Scale up LIGO Design?

- With a 10x lower arm cavity FSR, nearly all higher-order mode (HOM) resonances will lie in the observation band
  - ➔ Precision mode-matching is critical to suppress noise couplings, squeezing loss, and squeezing angle mis-rotation around the frequencies of these resonances

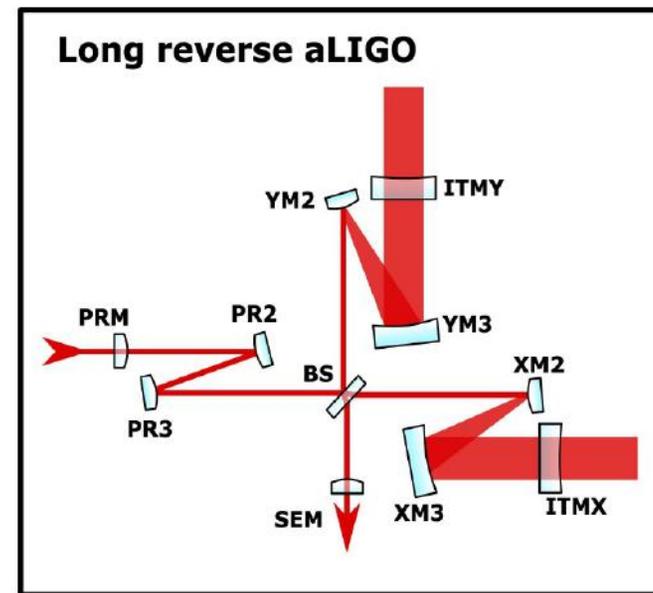




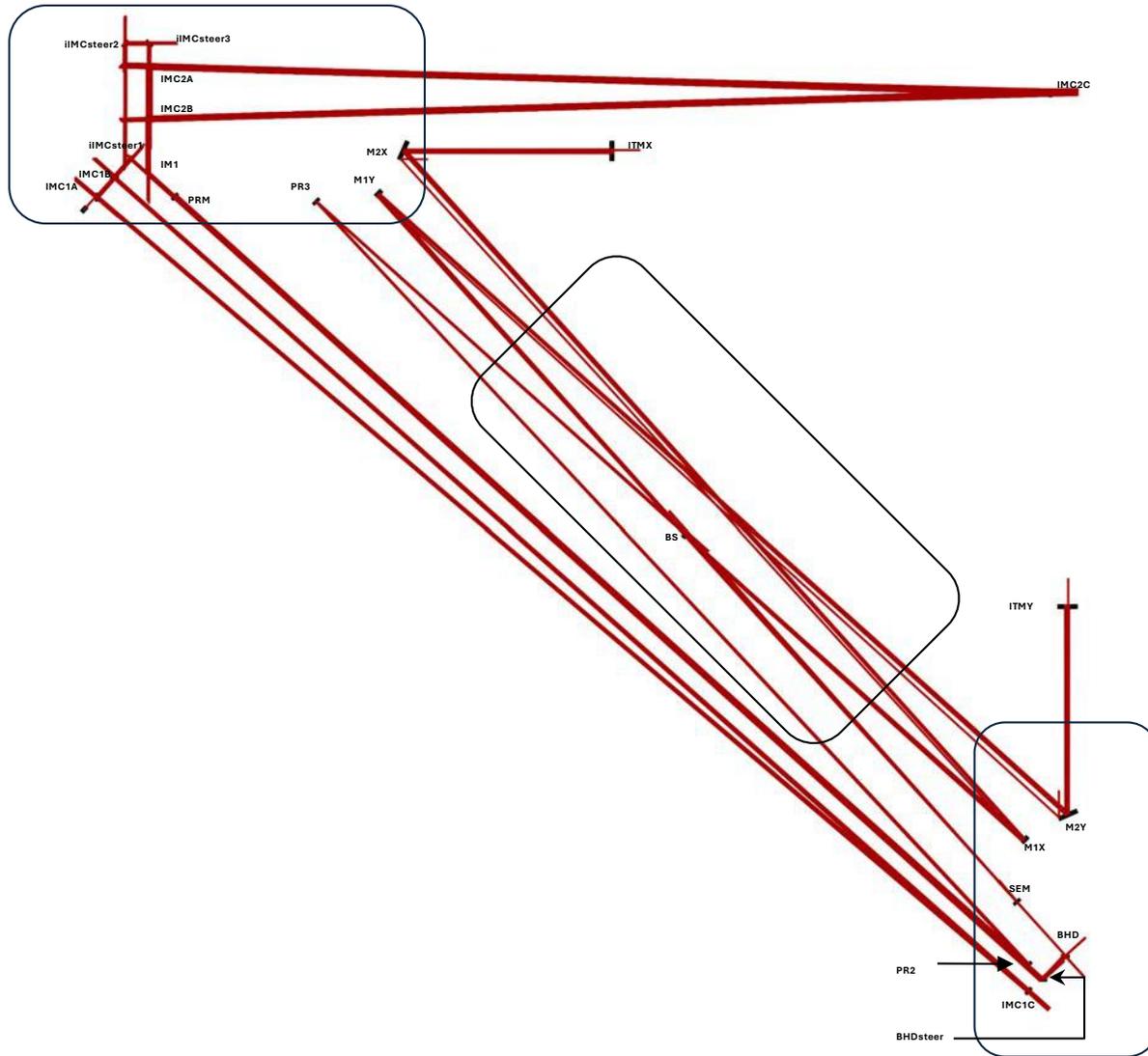
# “Leading” CE Interferometer Topologies (Preliminary)



- $\sim 1^\circ$  beamsplitter AOI
- Static lens polished onto ITM AR surface

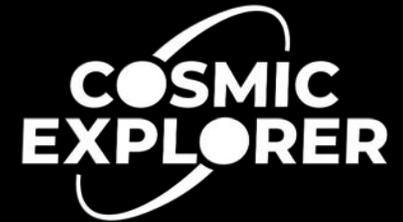


- $45^\circ$  beamsplitter AOI
- Lower-risk option, *if* beamsplitter thermal lensing is manageable



More to scale

# Cosmic Explorer Technology Challenges



- Large Optics
- Coatings (Thermal noise, Absorption)
- Squeezing (application)
- **Suspensions and seismic isolation systems**
- Vacuum system



# The Road Ahead



# Next-Generation Gravitational Wave Observatory Subcommittee (NextGenGW SC)



- Established by the **NSF**
- Committee home page with membership: <https://www.nsf.gov/mps/phy/nggw.jsp>
- Charge:
  - “... Based on this survey, a **recommended list of GW detection network configurations** that will **deliver a detector with sensitivity an order of magnitude greater** than the LIGO A+ design...”
  - [https://www.nsf.gov/mps/advisory/subcommittee\\_charges/mpsac-nggw-charge\\_signed.pdf](https://www.nsf.gov/mps/advisory/subcommittee_charges/mpsac-nggw-charge_signed.pdf)
- Call for White Papers:
  - Addressing “... science motivation and **key science objectives**, **technical description** of the proposed concept(s) and **how different aspects are associated with key science**, current and new technologies needed, risks, timelines, and approximate cost assessment, any synergies or dependencies on other multi-messenger facilities. ...”
  - <https://www.nsf.gov/mps/phy/nggw/WhitePaperCall2.pdf>
- Cosmic Explorer White Paper submitted: <https://arxiv.org/abs/2306.13745>
- **Report is now published**

Report available on home page:  
<https://www.nsf.gov/mps/phy/nggw.jsp>



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### Next-Generation Gravitational Wave Observatory Subcommittee (NextGenGW SC)

The Assistant Director of the Mathematical and Physical Sciences Directorate requests that the Mathematical and Physical Sciences Advisory Committee (MPSAC) establish a Next Generation Gravitational Wave (GW) Detector Concept Subcommittee (NextGenGW SC) to assess and recommend a set of concepts for new GW observatories in the U.S.

Charge

Subcommittee Members

Call for White Papers

#### Submissions to Subcommittee

- Cosmic Explorer White Paper
- Voyager White Paper
- LIGO Lab White Paper
- LSC White Paper
- Rainer Weiss White Paper

#### Invited Presentations to the Subcommittee

- Einstein Telescope
- KAGRA
- LIGO
- LIGO-India
- LISA
- VIRGO

Report:

NSF MPS AC Subcommittee on Next-Generation Gravitational-Wave Detector Concepts Report, March 2024

# ngGW Subcommittee Recommendations



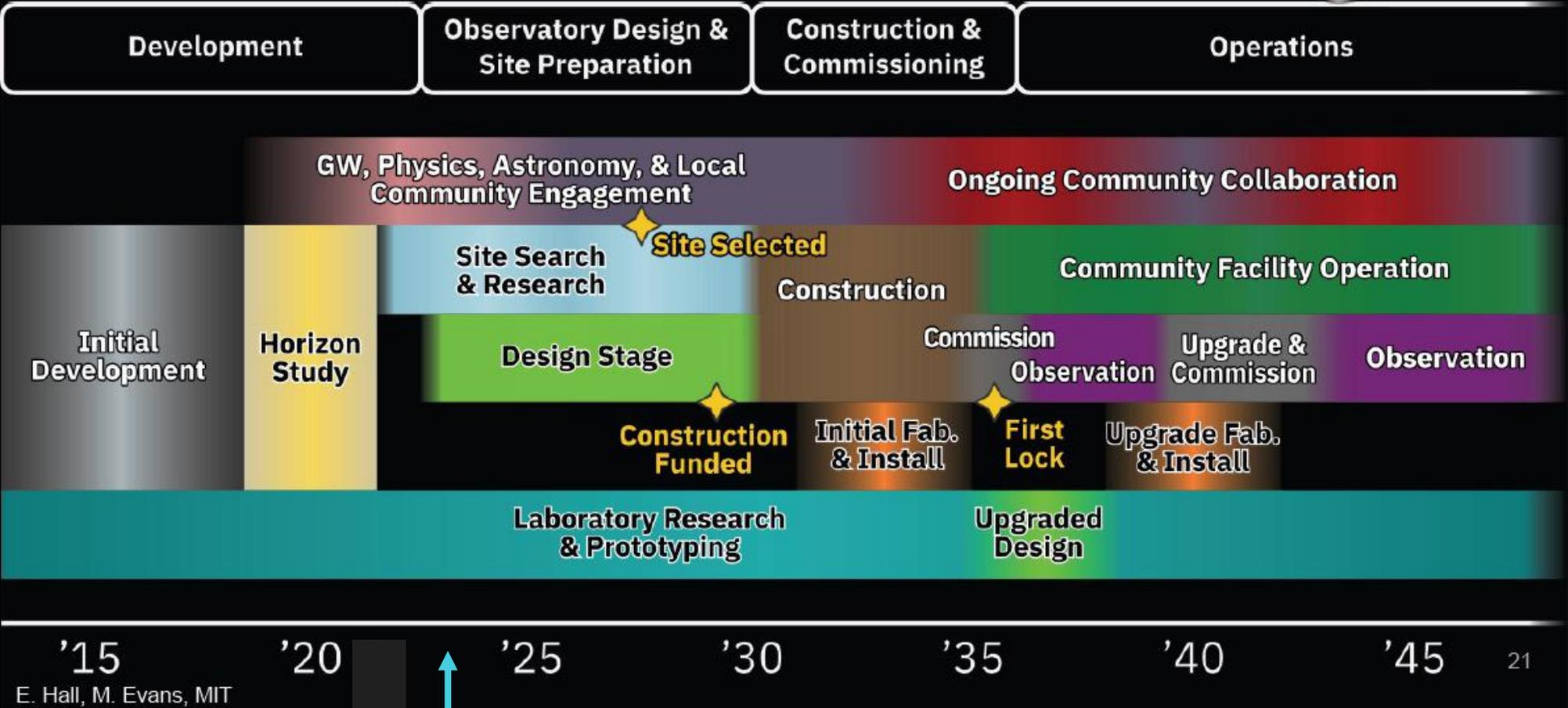
- aLIGO facilities to be phased out by the time the CE wide-band sensitivity (of one or two detectors) is better than that of the aLIGO detectors.
- The availability of the LIGO-India detector in the network is important for MMA and, in fact, critically important in the absence of ET. The absence of LIGO-India cannot be balanced by keeping the aLIGO detectors operational.

# ngGW Subcommittee Recommendations

Recommended list of GW detection network configurations that will deliver sensitivity an order of magnitude greater than the aLIGO A+ design.

- **CE40, ET, LIGO-India** (Network #1)
- **CE40, ET** (Network #2)
- **CE40, CE20, LIGO-India** (Network #3)
- **CE40, CE20** (Network #4)

# Cosmic Explorer Notional Timeline (see [CEHS](#))



## Take-away points

- GW astronomy is here, and we are starting to understand the actual source population.
- Advanced LIGO design works extraordinary well
  - Limiting:
    - Quantum noise
    - Coating Thermal noise
    - Power handing due to point absorbers
- US effort for designing the next-generation observatories is underway. Based on proven technology, but some R&D is needed.
  - Quantum sensing (optical squeezing, ...)
  - Large optics and coatings
  - Vacuum technology
  - ...



Thank you for the invite!



The End

Credit: Eddie Anaya, Cal State Fullerton Undergraduate