

Introduction

In the *r*-process, fission plays a fundamental role by recycling the matter during neutron irradiation and by shaping the final *r*-abundance distribution. In this study, we present a new method to describe the dynamical-fission process and following prompt neutron emission.

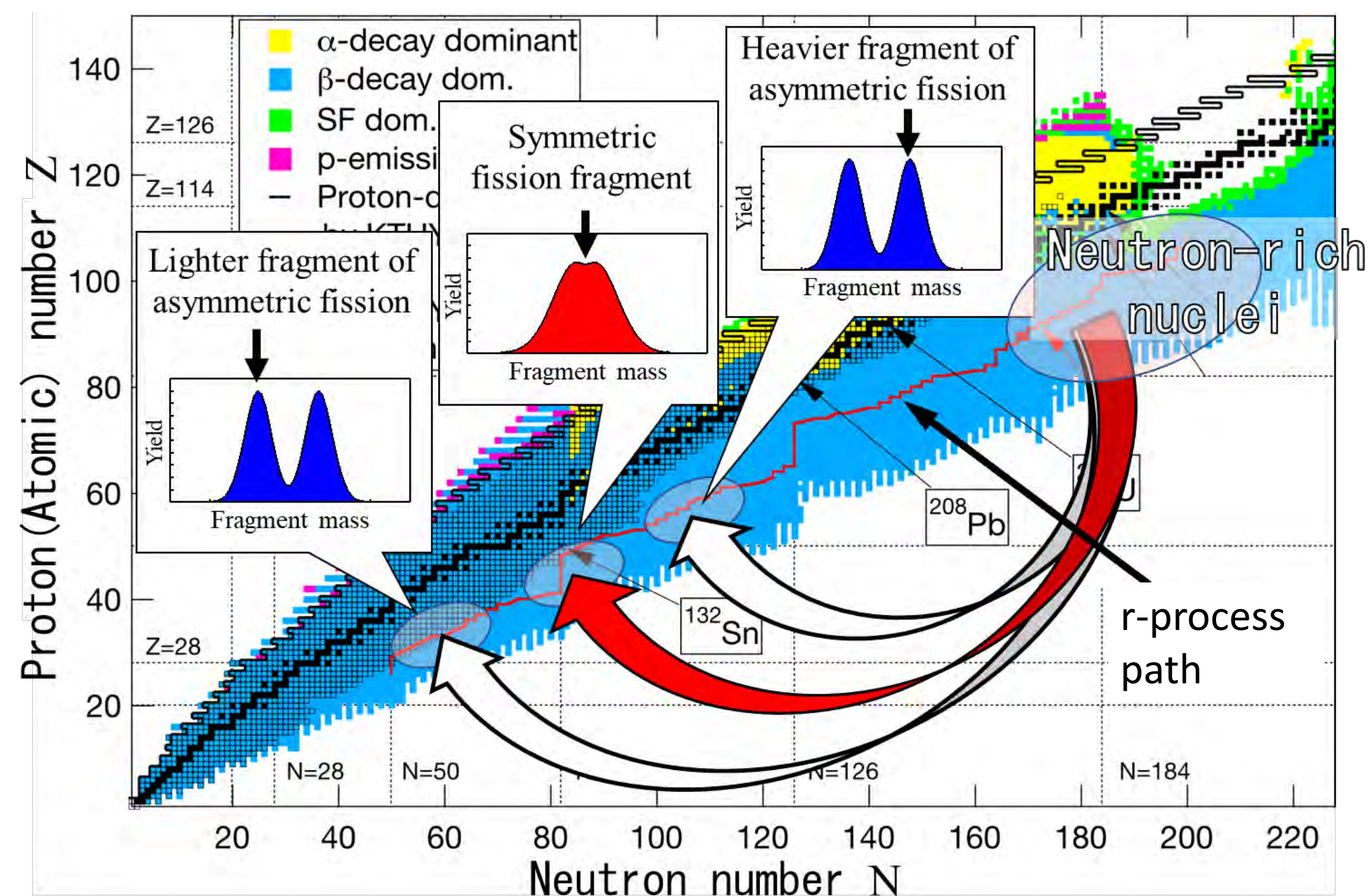


Fig. 1. *r*-process path and fission mode (mass-symmetric and asymmetric fission) effects in the nucleus chart [1].

Model

Multi-dimensional Langevin Equation

$$\frac{dq_i}{dt} = (m^{-1})_{ij} p_j$$

$$\frac{dp_i}{dt} = -\frac{\partial V}{\partial q_i} - \frac{1}{2} \frac{\partial}{\partial q_i} (m^{-1})_{jk} p_j p_k - \gamma_{ij} (m^{-1})_{jk} p_k + g_{ij} R_j(t)$$

$\langle R_i(t) \rangle = 0, \langle R_i(t_1) R_j(t_2) \rangle = 2\delta_{ij} \delta(t_1 - t_2)$: white noise (Markov process),

$\sum_k g_{ik} g_{jk} = T \gamma_{ij}$: Einstein relation (Fluctuation-dissipation theorem)

Nuclear Shape: $q = \{z, \delta, \alpha\}$ (z : center distance, δ : deformation, α : mass asymmetry)

m_{ij} : Hydrodynamical mass (inertia mass), γ_{ij} : Wall and Window (one-body) dissipation (friction)

- Time evolution of nuclear shape is traced from the compound state to the scission point by solving the Langevin equations.

Potential energy in dynamical model

$$V(q, l, T) = V_{LDM}(q) + \frac{\hbar^2 l(l+1)}{2I(q)} + V_{SH}(q, T)$$

$$V_{LDM}(q) = E_S(q) + E_C(q)$$

$$V_{SH}(q, T) = E_{shell}^{T=0}(q) \exp(-aT^2/E_d)$$

E_S : Generalized surface energy (finite range effect),

a : level density parameter (Toke and Swiatecki),

E_C : Coulomb repulsion for diffused surface,

$E_{shell}^{T=0}$: Shell correction energy, I : Moment of inertia for rigid body

Shell damping energy: $E_d = 20$ MeV [2]

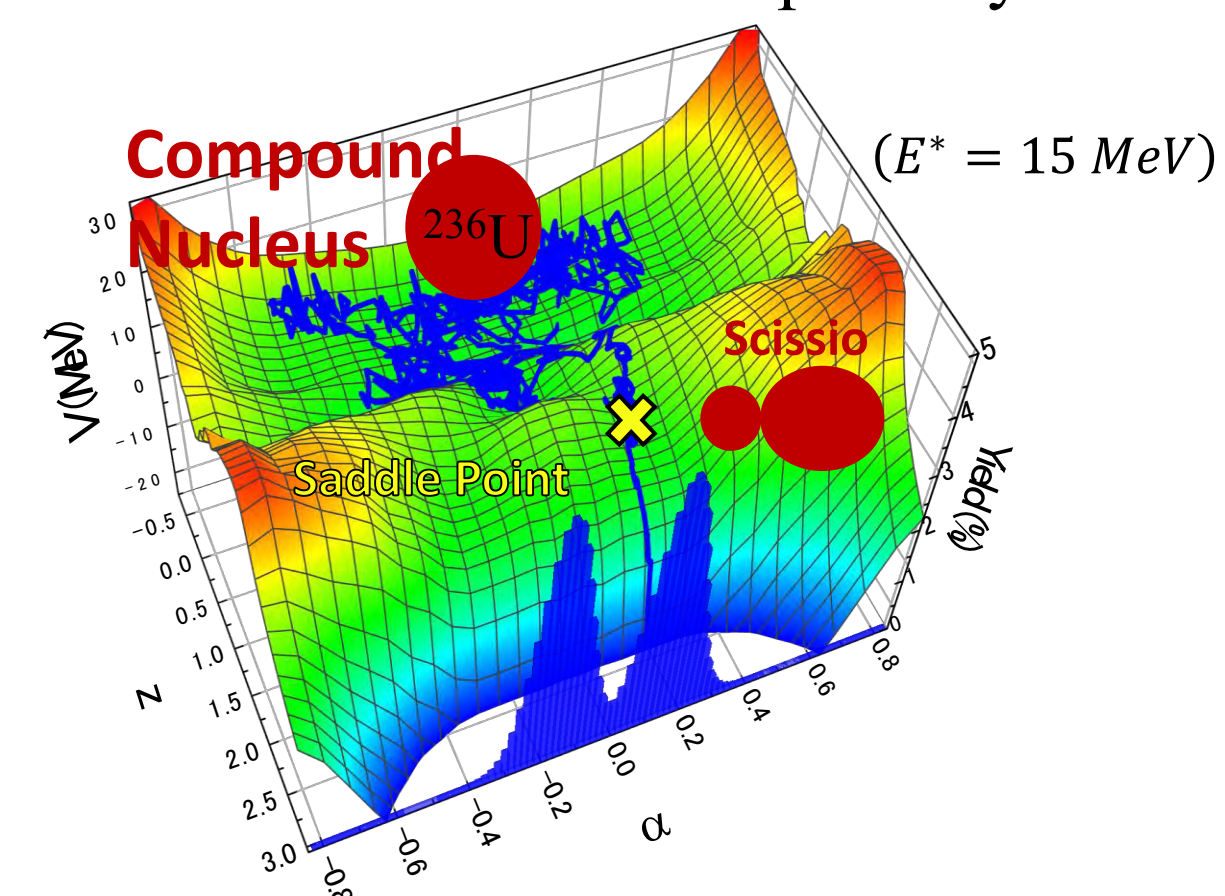


Fig. 2. Potential energy on the z - α plane for ^{236}U and a sample nuclear shape trajectory of asymmetric fission.

CCONE: comprehensive code for nuclear data evaluation

The CCONE code system integrates various nuclear reaction models needed to describe nucleon, light charged nuclei up to alpha-particle and photon induced reactions [3].

Results and Discussion

1. Results of fission fragment yields (^{236}U , $E^* = 9$ MeV)

- Using a certain set of model parameters, we successfully reproduce the experimental data.
- The calculated $\langle \nu_n \rangle = 2.517$, the experimental $\langle \nu_n \rangle = 2.43$ [4].

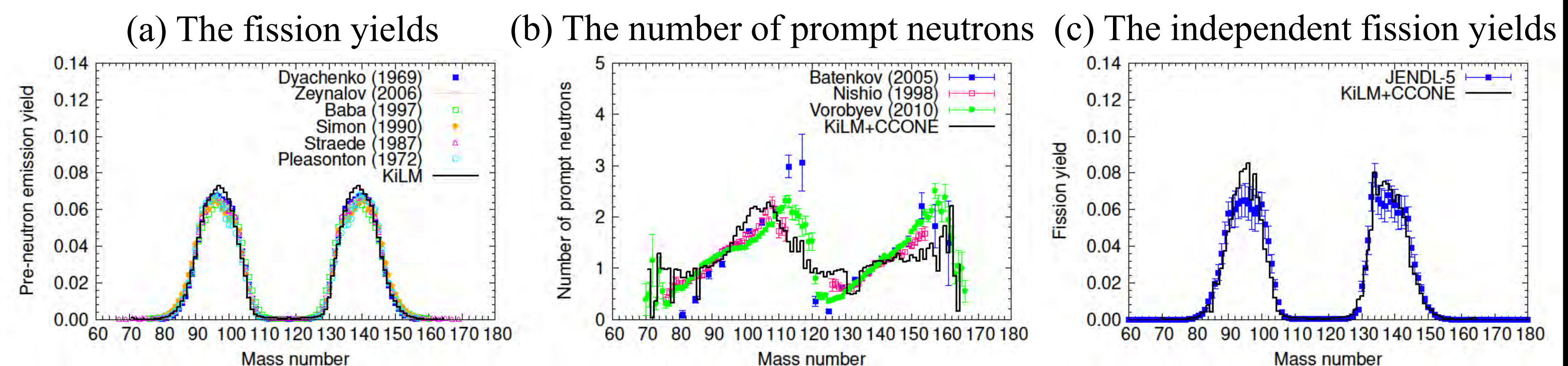


FIG. 3. The normalized fission yields of ^{236}U , which is the compound nucleus of $^{235}\text{U} + n$. The numerical results are compared with several experimental data.

2. Fission of neutron-rich nuclei at two uranium isotopes

- We performed neutron emission calculations of very neutron-rich uranium isotopes where experimental data are unavailable.

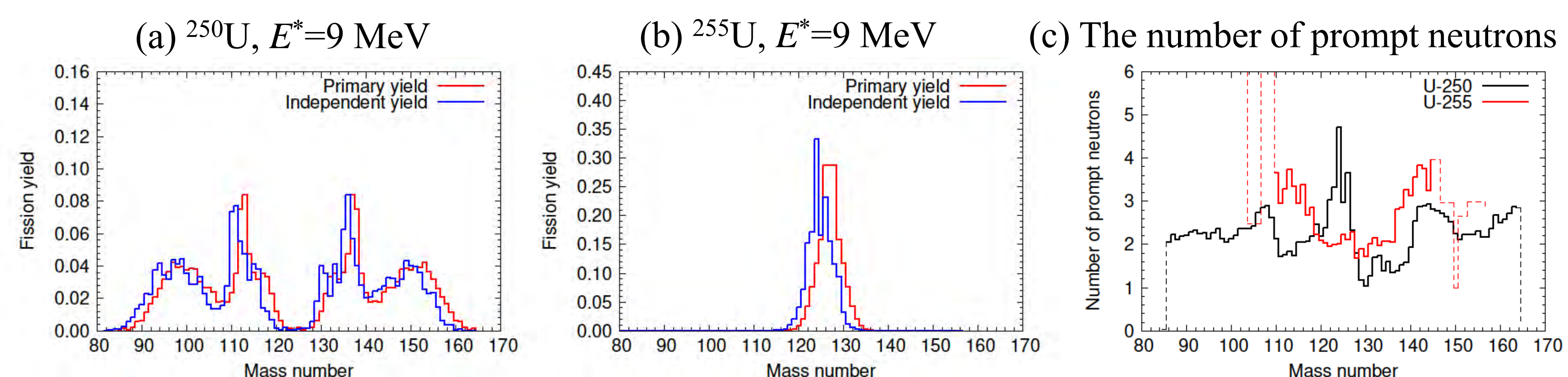


FIG. 4. The normalized fission yields of ^{250}U (a) and ^{255}U (b), which compare the primary yield distribution and the independent fission yields. The number of prompt neutrons as a function of fragment mass for ^{250}U (black line) and ^{255}U (red line) as shown in graph (c).

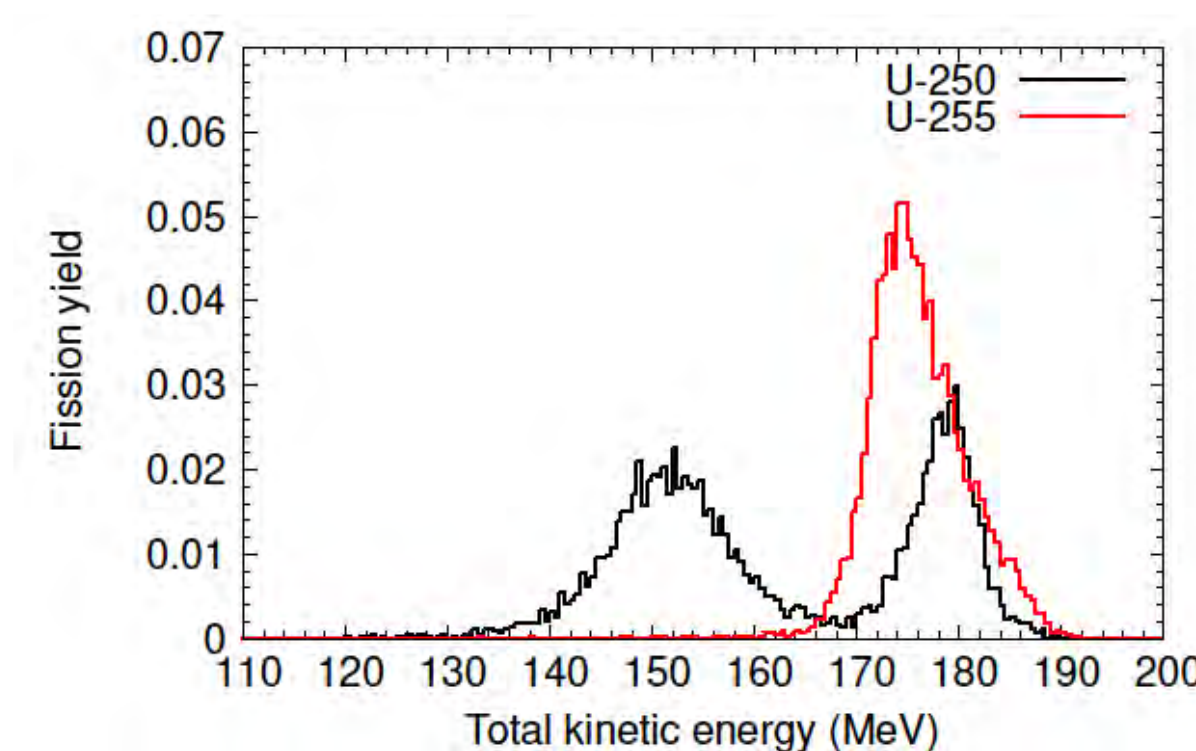


FIG. 5. The fission yield distributions in the TKE for ^{250}U (black line) and ^{255}U (red line).

- The dramatic change of fission mode was observed for neutron-rich uranium isotopes.
- ^{250}U : $\langle \nu_n \rangle = 4.185$, and ^{255}U : $\langle \nu_n \rangle = 3.434$.
- ^{250}U : $\langle \text{TKE} \rangle = 162.50$, and ^{255}U : $\langle \text{TKE} \rangle = 175.85$ MeV.
- From these results, the number of prompt neutrons does not necessarily increase with neutron number.

Summary

- Our framework is highly reproducible in the experiments and shows that the number of emitted neutrons after fission differs significantly in neutron-rich uranium fission depending on distributions of fission variables.

References

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