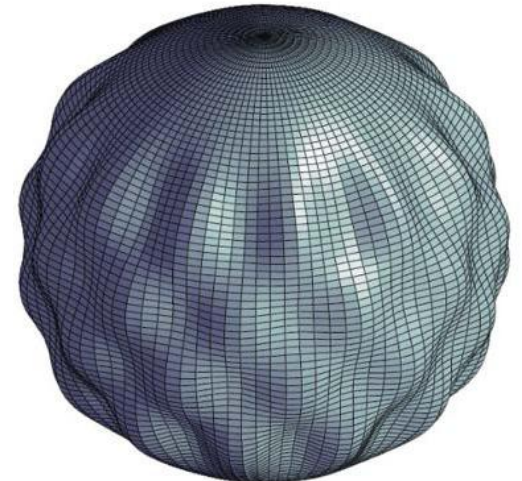


Astroseismology of NSs

Joint RIKEN/N3AS Workshop on Multi-Messenger Astrophysics

Hajime SOTANI (RIKEN ABBL/iTHMES)



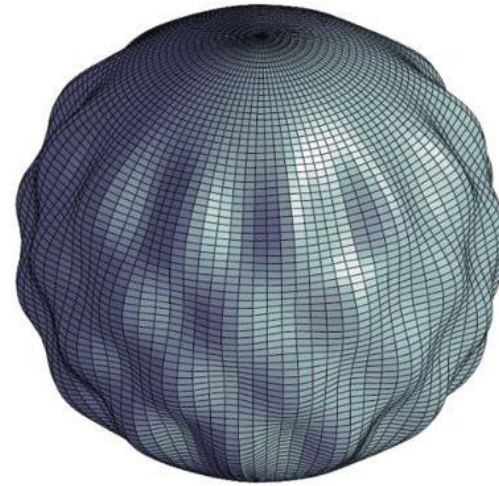
Asteroseismology

- how to know the best time to eat a watermelon?
 - inside can not be checked before cutting
- “empirical rule”
 - to check the best time, knock on a watermelon
 - high frequency “KIN-KIN”; too young
 - “BAN-BAN”; best time!
 - low frequency “BON-BON”; too old
 - may need many years to get this ability
- one could see the interior with specific sounds from objects.
 - **asteroseismology**
 - linear perturbation analysis is considered in this talk.



NS oscillation modes

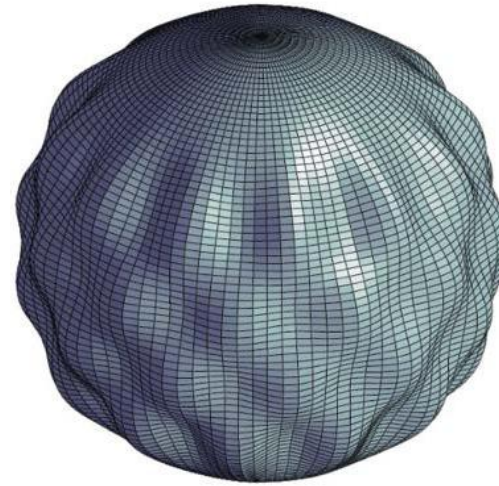
- axial parity
 - spacetime (w-) modes
 - torsional (t-) modes
 - rotational (r-) modes
 - magnetic modes
- polar parity
 - fundamental (f-) modes
 - pressure (p-) modes
 - gravity (g-) modes
 - spacetime (w-) modes
 - shear (s-) modes
 - interface (i-) modes
 - inertial (i-) modes
 - magnetic modes



under the angular transformation
 $(\theta \rightarrow \pi - \theta, \phi \rightarrow \pi + \phi)$,
a spherical harmonic function
with index ℓ transforms as
 $(-1)^{\ell+1}$: axial parity / $(-1)^\ell$: polar parity

NS oscillation modes

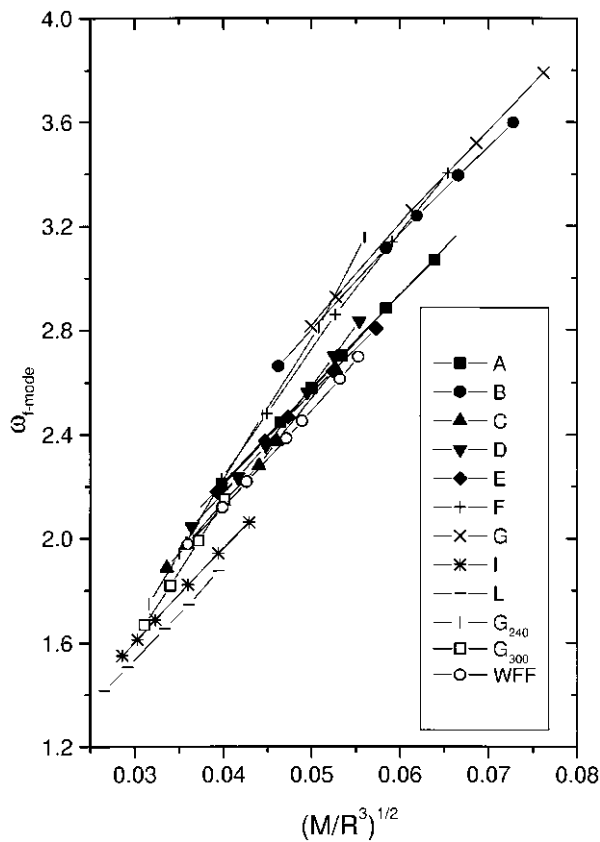
- axial parity
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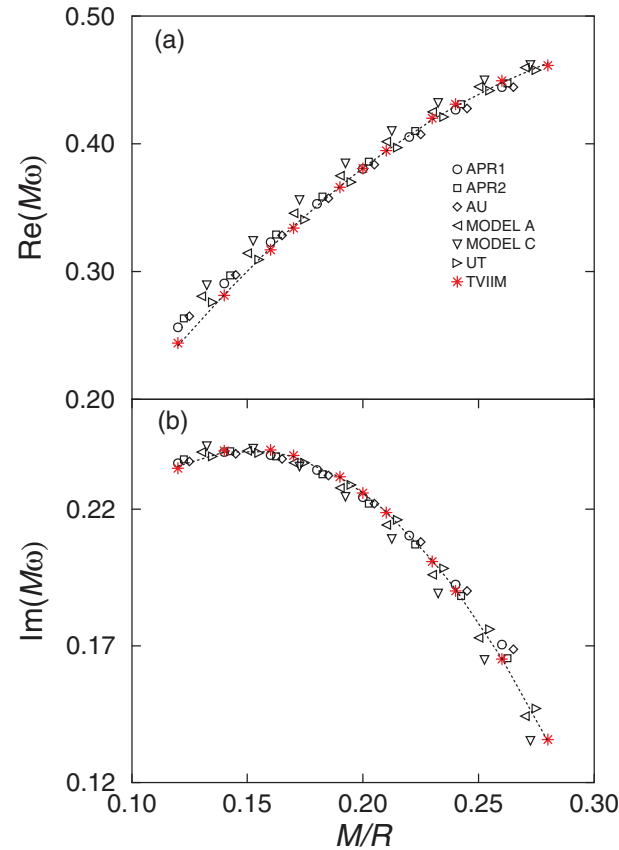
under the angular transformation
 $(\theta \rightarrow \pi - \theta, \phi \rightarrow \pi + \phi)$,
a spherical harmonic function
with index ℓ transforms as
 $(-1)^{\ell+1}$: axial parity / $(-1)^\ell$: polar parity

Universal (empirical) relations

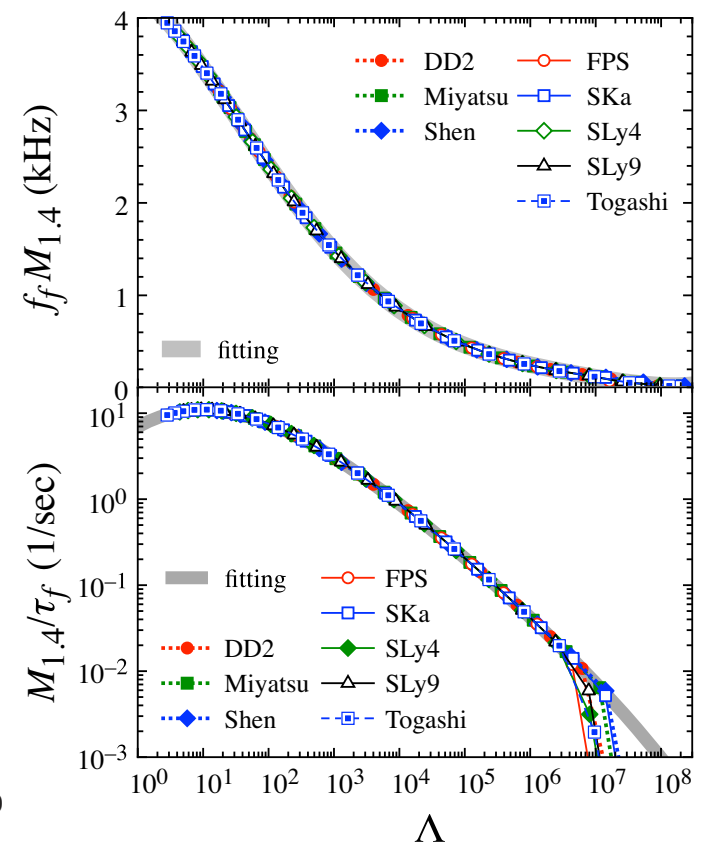
- To extract the physical properties from observables,
a universal relation (independently of the EOS) must be important



Anderson & Kokkotas 98



Tsui & Leung 05

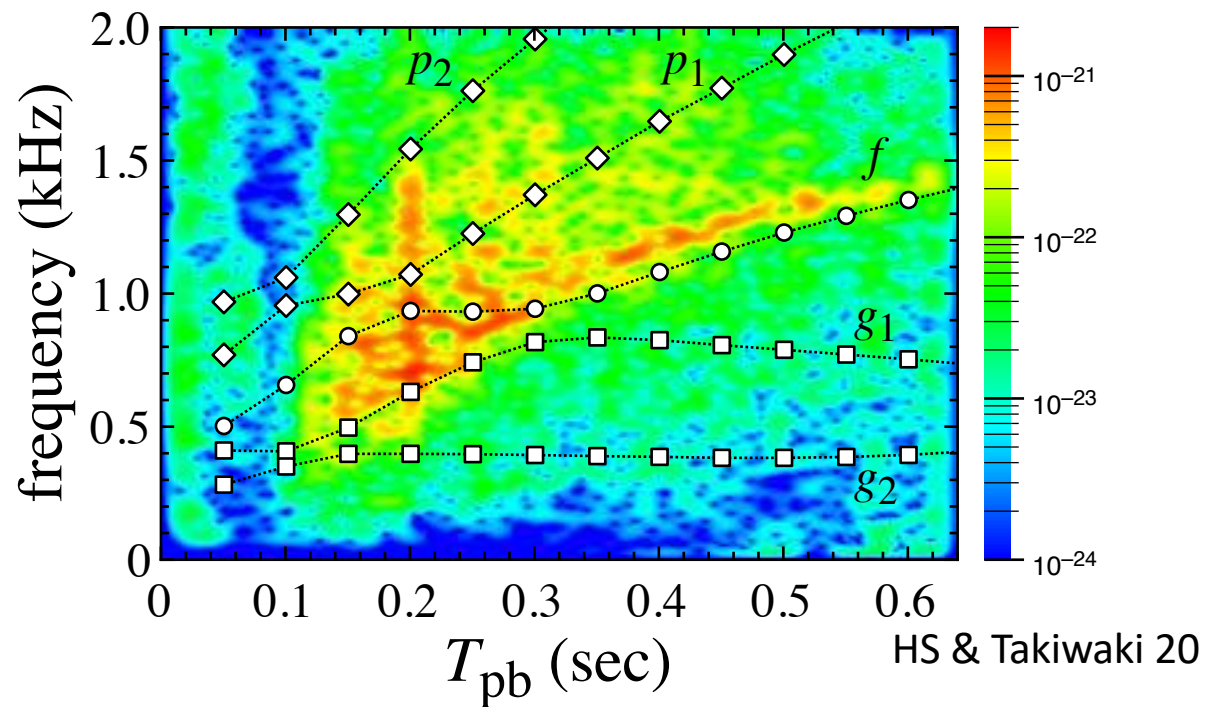


HS & Kumar 21

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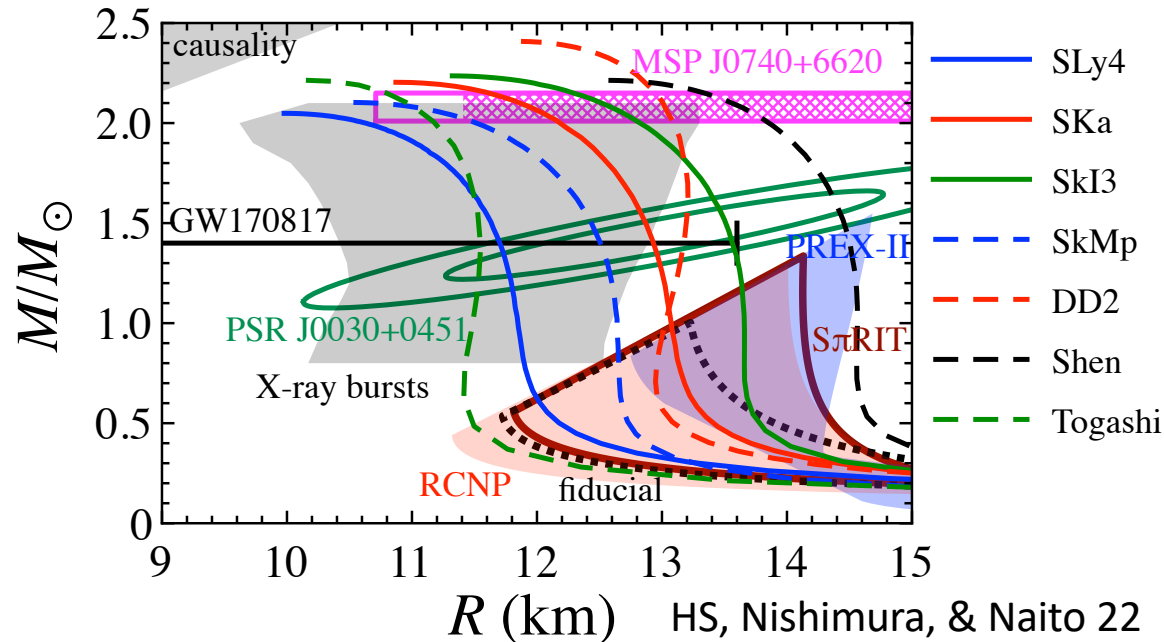
- supernova gravitational waves
- magnetar QPOs and torsional oscillations
- resonant shattering and shear/interface modes

Supernova gravitational waves

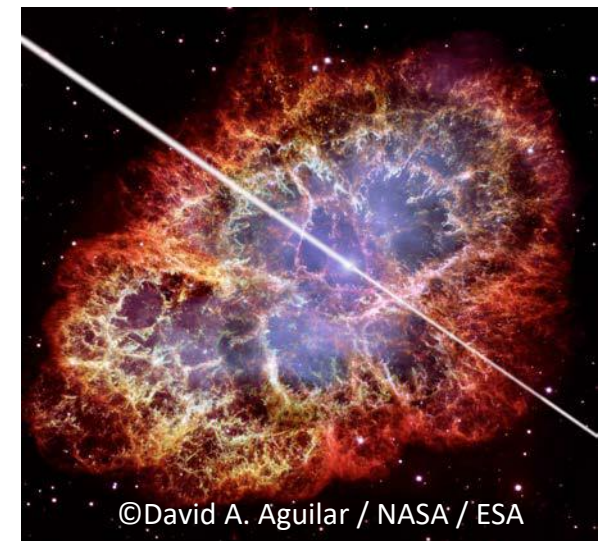
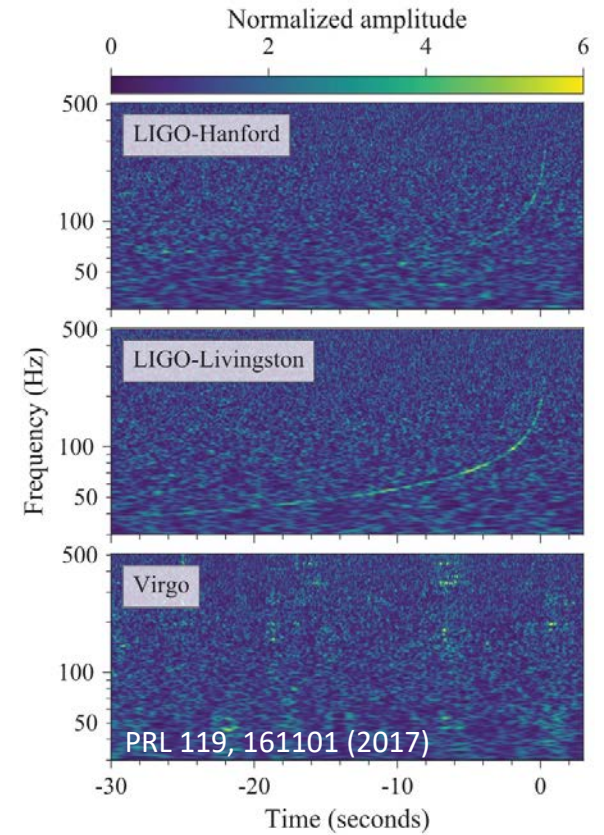


Dawn of GW astronomy

- GWs from the compact binary merger have been detected.
 - GWs become a new tool for extracting astronomical information.

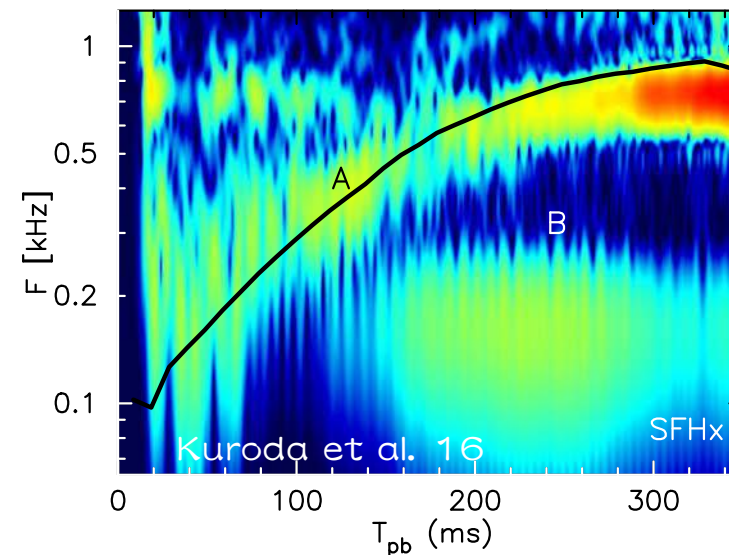
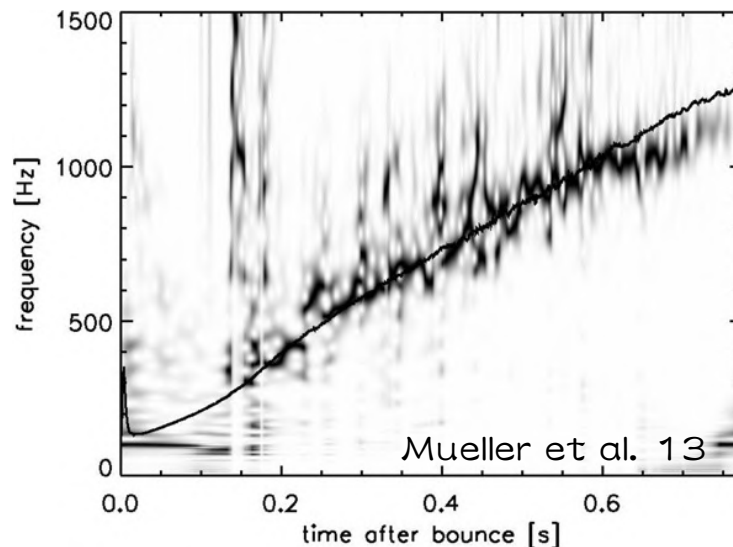


- The next candidate must be a supernova explosion.



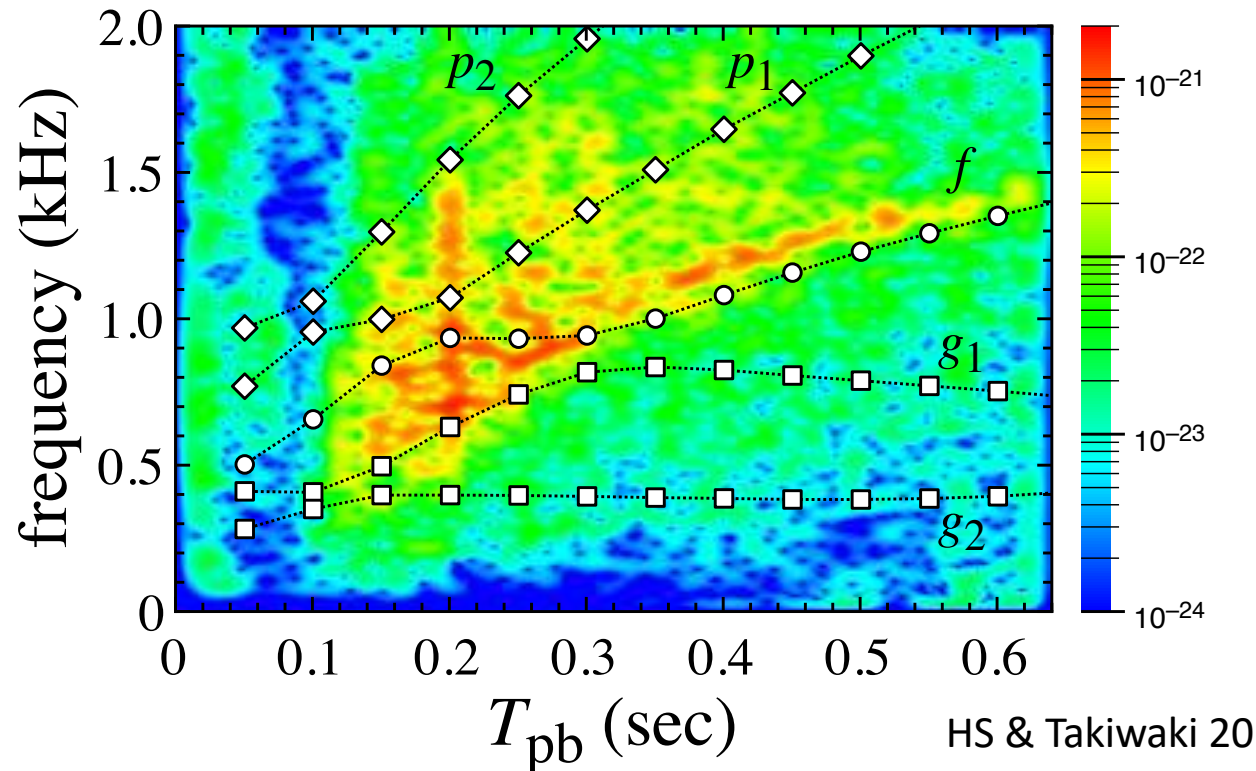
Next candidate of GW sources

- core-collapse supernovae
 - compared to the binary merger, the system is almost spherically symmetric
 - less energy of gravitational waves
 - many numerical simulations show the existence of GW signals
 - SN GWs depend on the SN models, such as progenitor mass and EOS
 - how to extract the astronomical information from the GW observations?
 - what is the origin of the SN GWs?



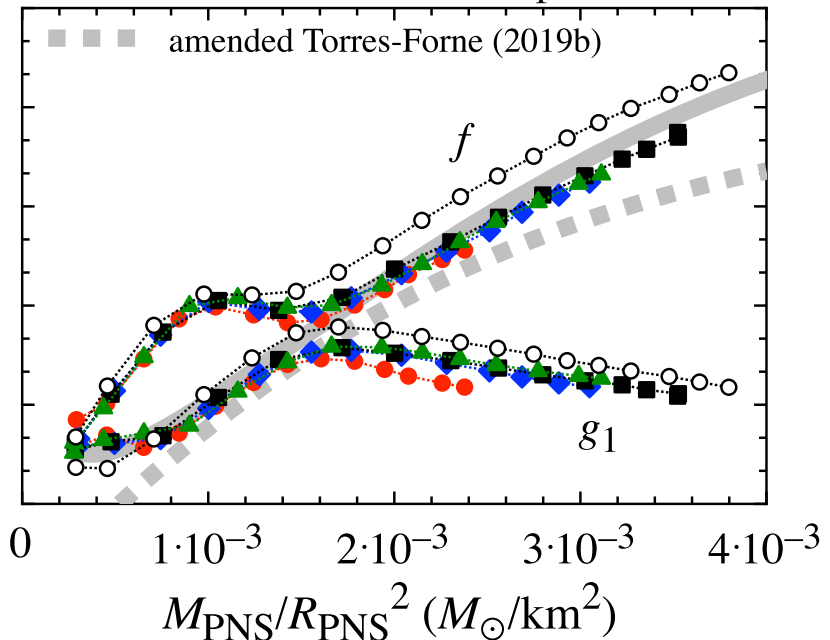
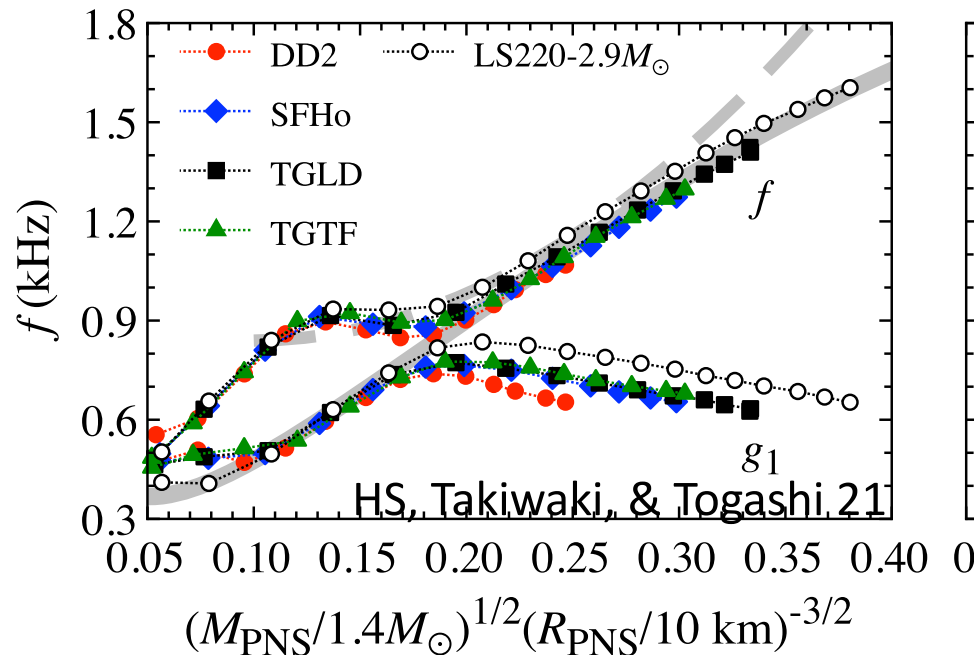
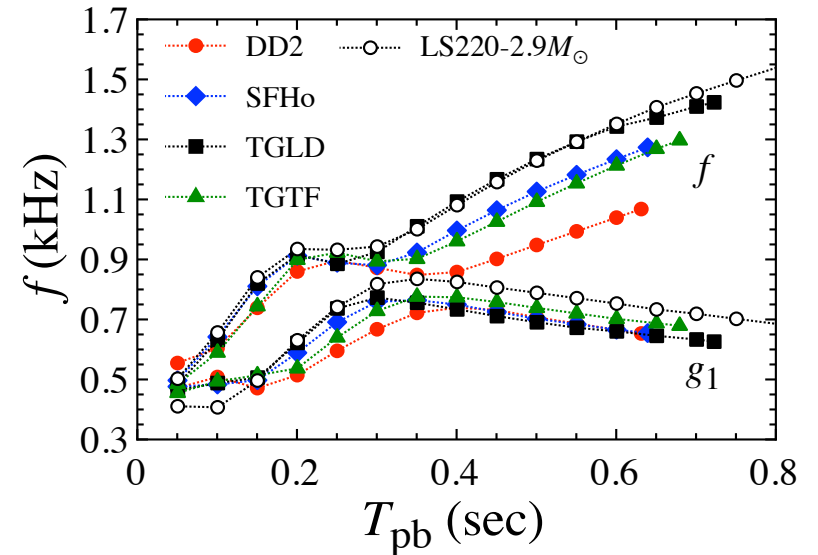
Comparison with GW signals in numerical simulation

- GW signals correspond to g_1 -mode in early phase and f-mode after avoided crossing.
 - similar correspondence has been seen even in various SN models

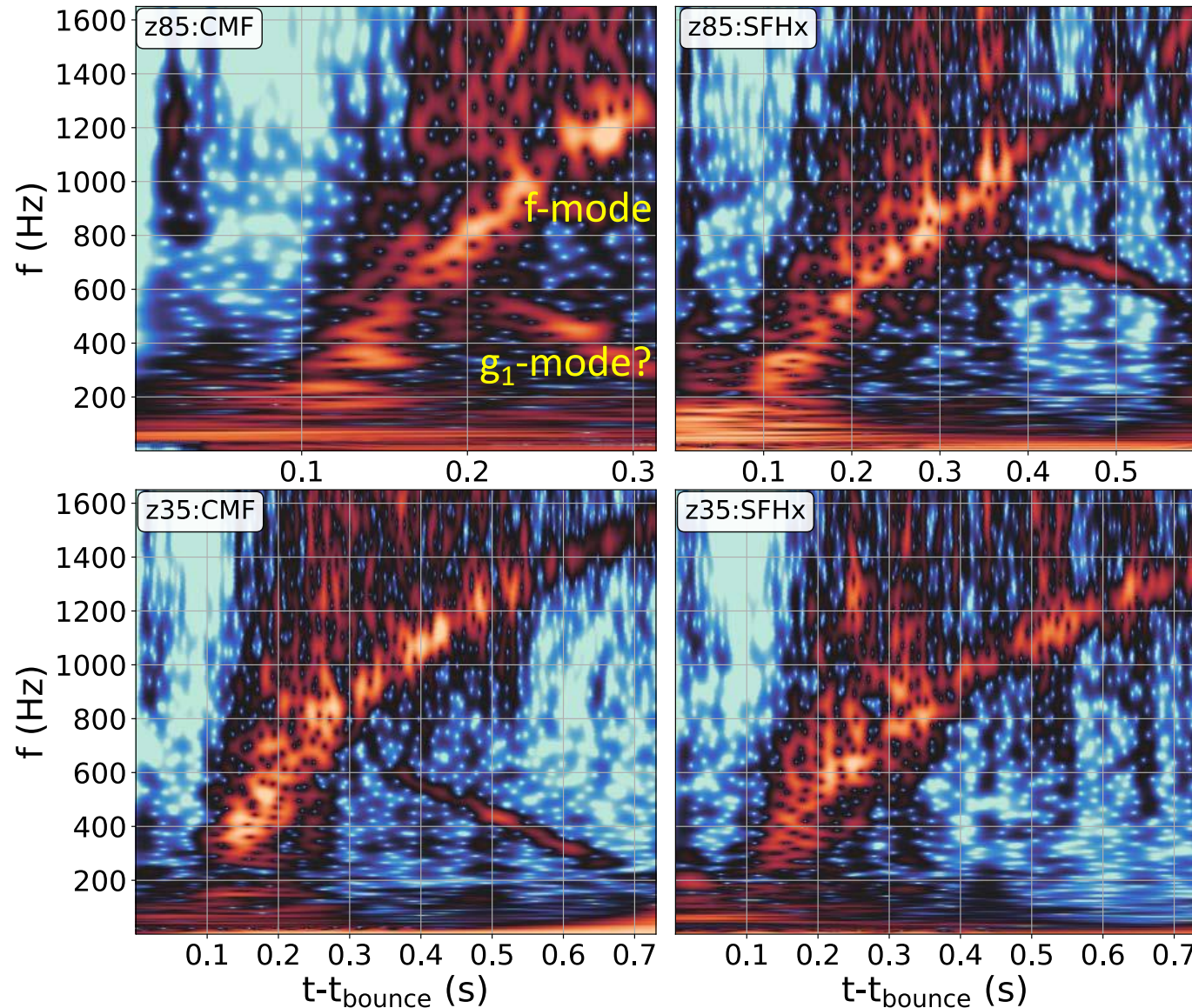


What can we learn from SN GWs

- GW freqs. evolution strongly depend on SN models, but...
- well expressed with average density or surface gravity of PNS



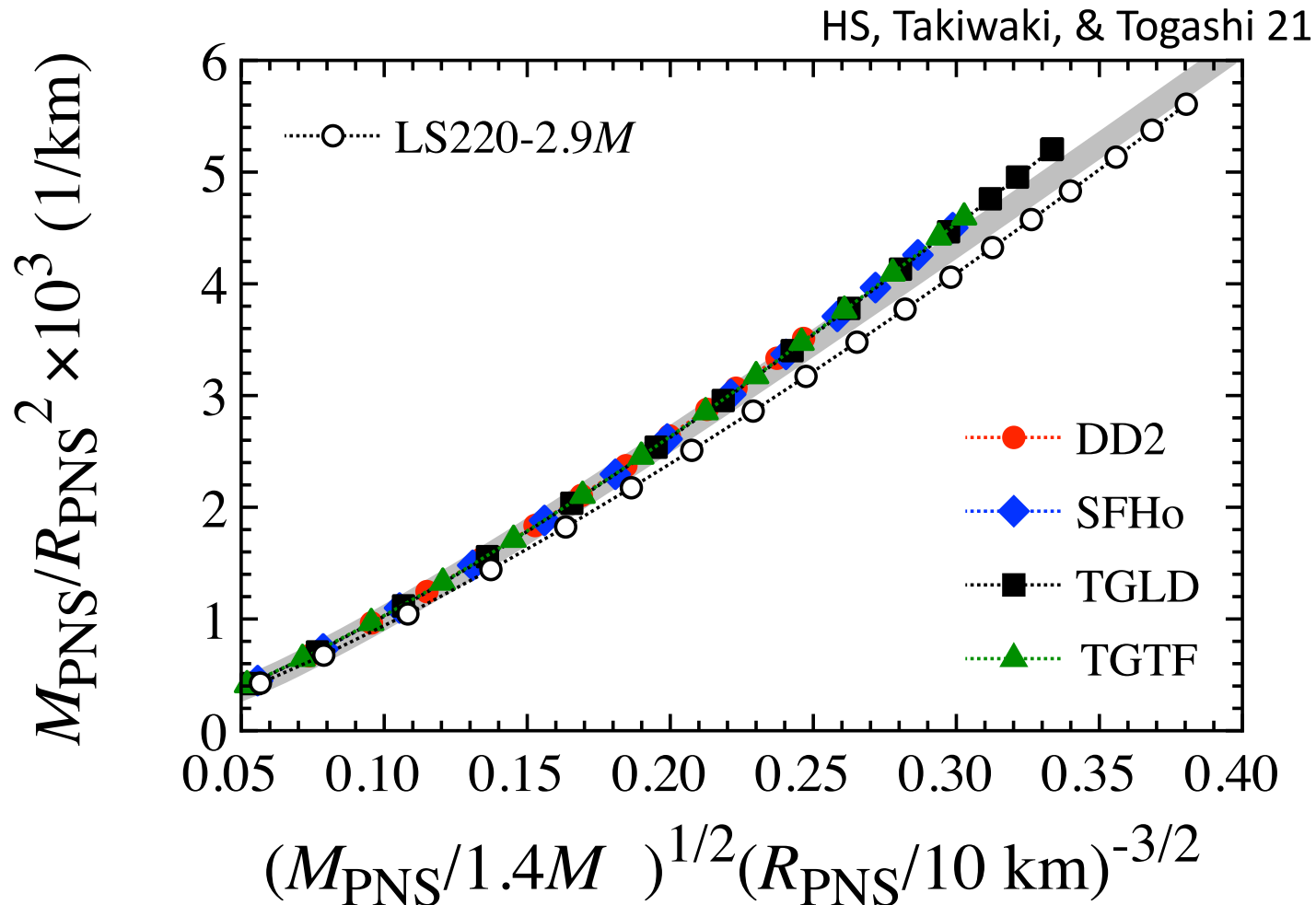
Signal of the g_1 -mode oscillations?



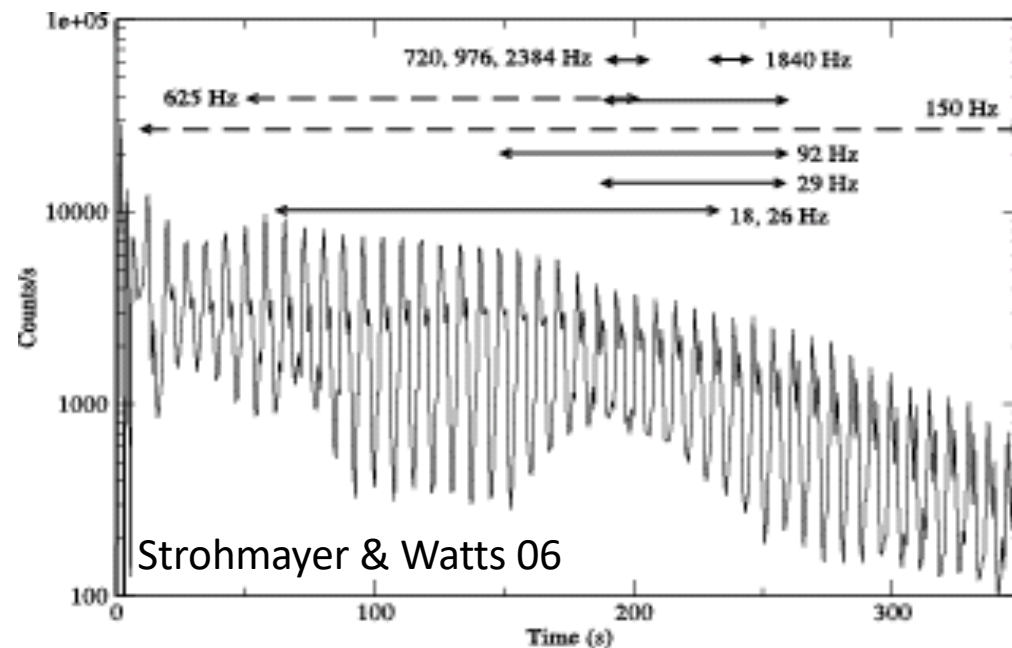
Jakobus+23

Strong correlations M/R^2 & M/R^3

- Unlike cold NSs, we find the strong correlations in PNS properties



Magnetar QPOs and torsional oscillations

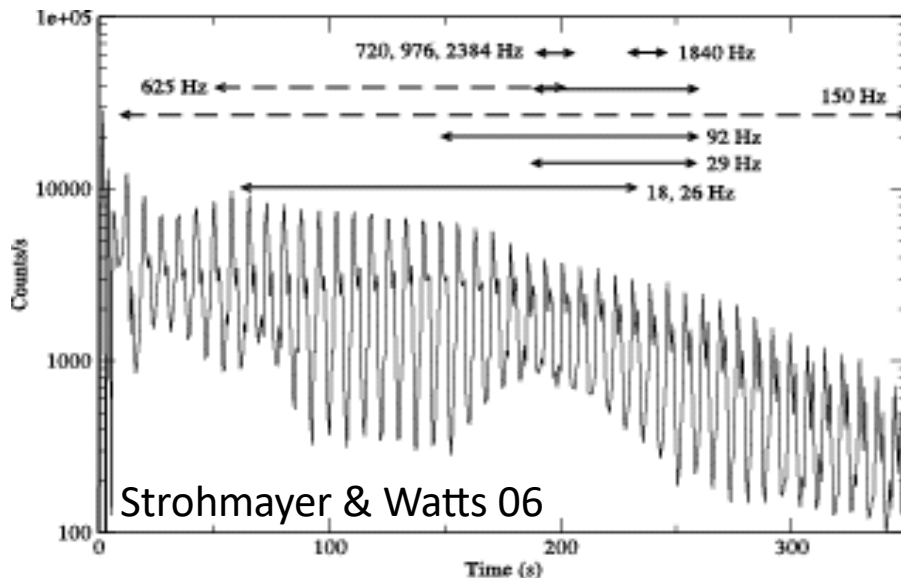


Magnetar QPOs

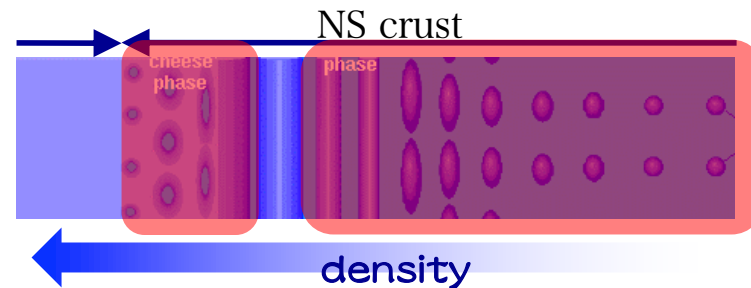
- Quasi-periodic oscillations (QPOs) in the afterglow of giant flares from soft-gamma repeaters (SGRs)

(Barat+83, Israel+05, Strohmayer & Watts 05, Watts & Strohmayer 06)

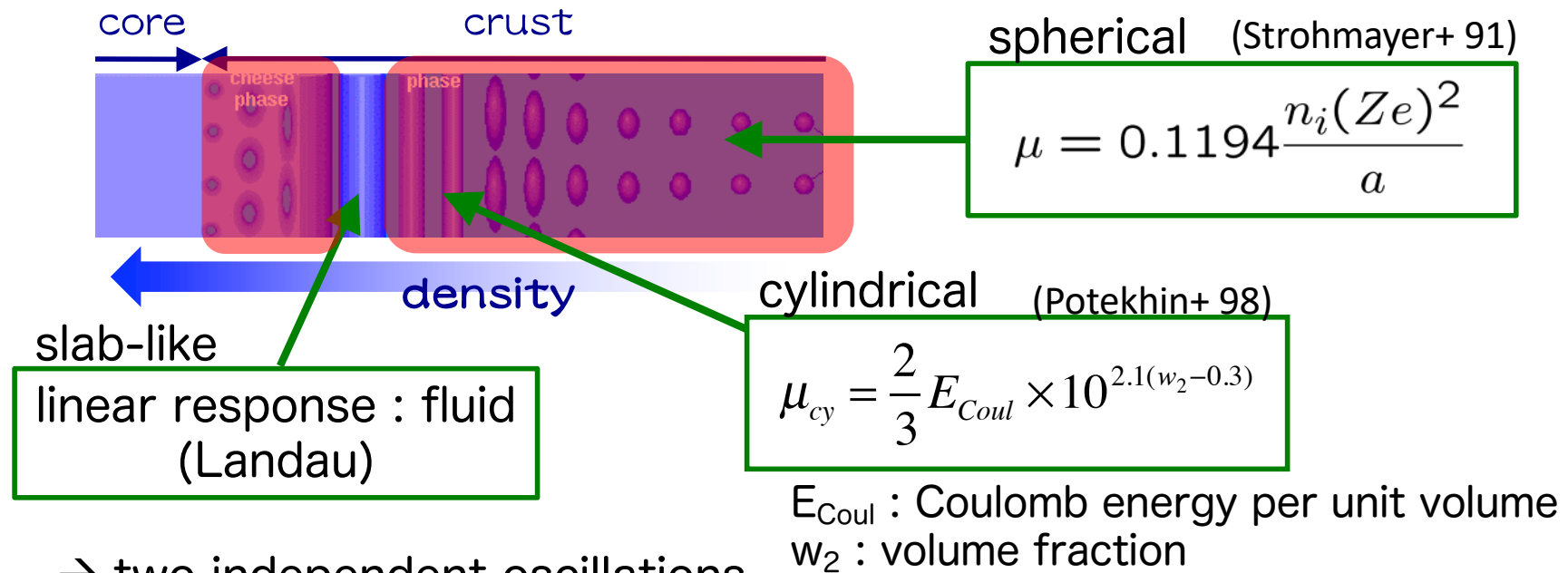
- SGR 0526-66 (5th/3/1979) : 43 Hz
- SGR 1900+14 (27th/8/1998) : 28, 54, 84, 155 Hz
- SGR 1806-20 (27th/12/2004) : 18, 26, 30, 92.5, 150, 626.5, 1837 Hz
 - additional QPO in SGR 1806-20 : 57 Hz (Huppenkothen+14)
 - additional QPOs : 51.4, 97.3, 157 Hz (Miller+18)



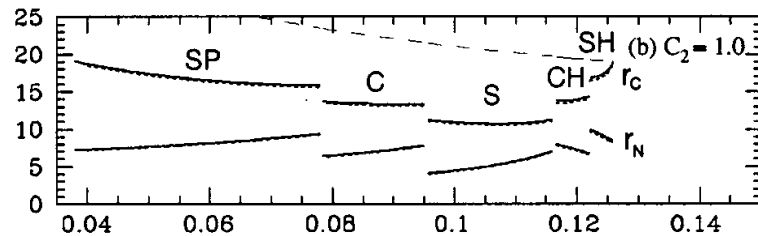
- Crustal torsional oscillation ?
- Magnetic oscillations ?



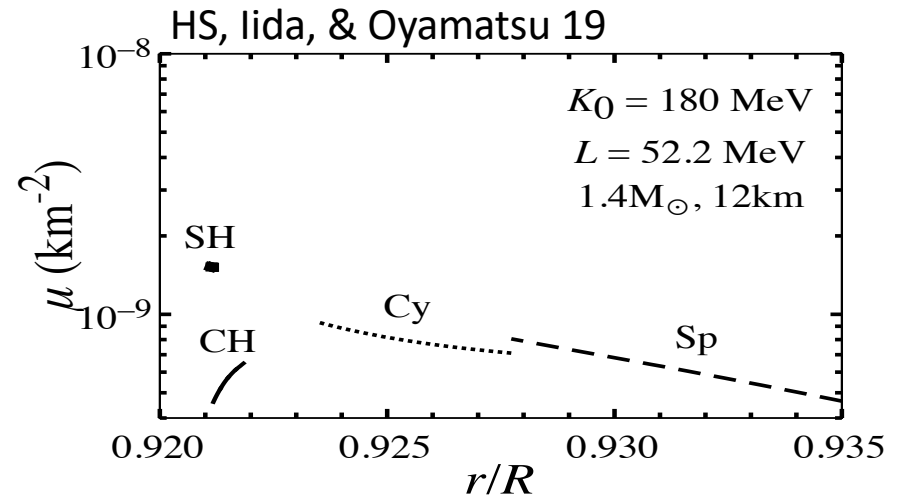
Elasticity in NS crust



- two independent oscillations
 - (i) spherical + cylindrical (sp+cy)
 - (ii) tube + bubble (tu+bu)
- bubble ~ spherical
 tube ~ cylindrical

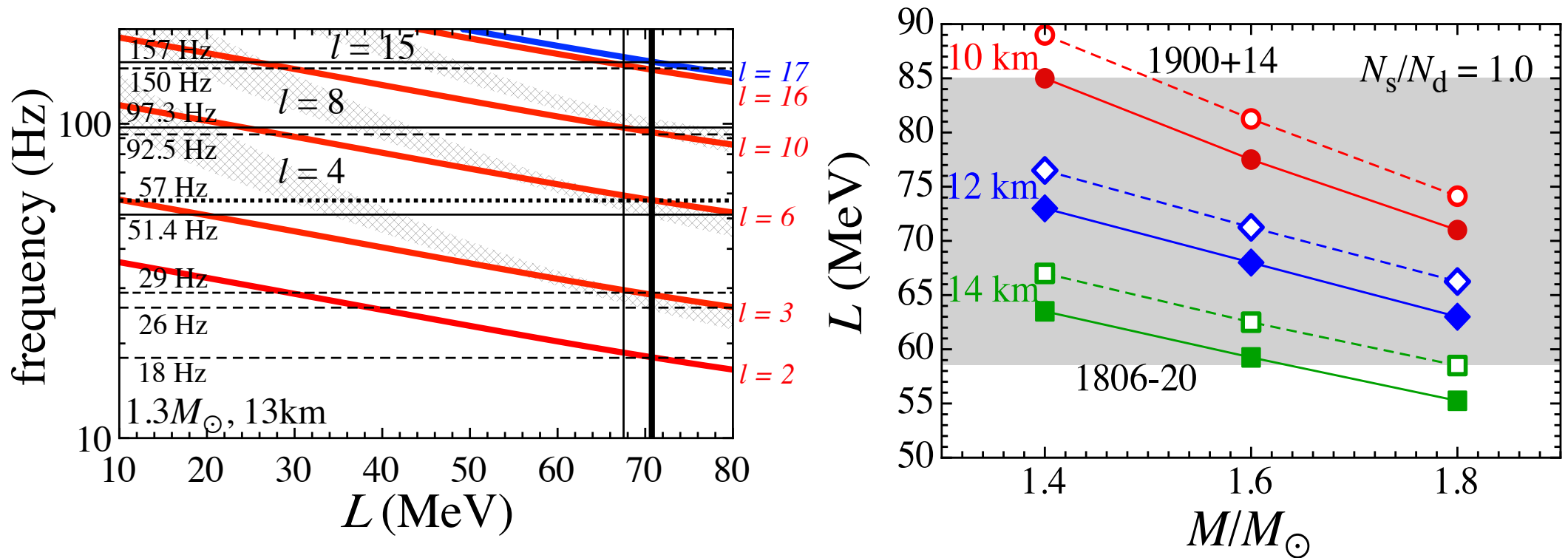


Watanabe & Iida 03



Constraint on nuclear parameters

- observed freq. are well identified with crustal torsional oscillations, which tell us the constraint on L

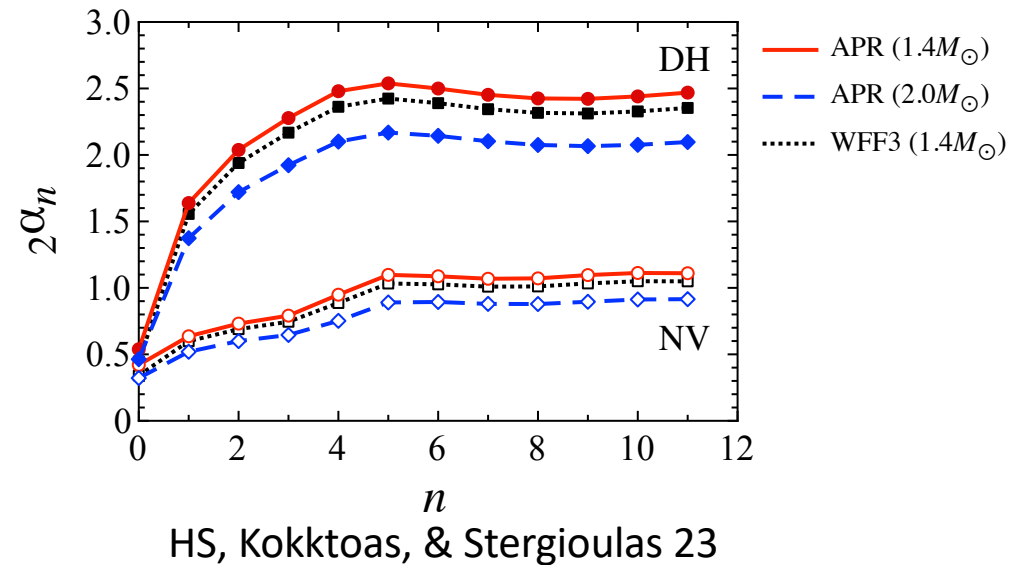
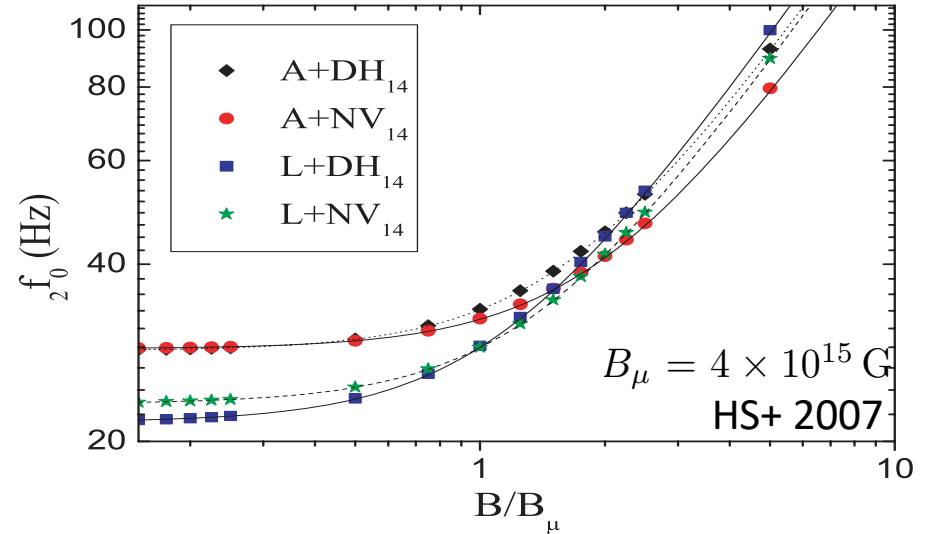


Magnetic effects

- the shift in the torsional oscillation freqs. obeys the following formula (HS+2007; Gabler+2018)

$$\frac{\ell f_n}{\ell f_n^{(0)}} \approx \left[1 + \ell \alpha_n \left(\frac{B}{B_\mu} \right)^2 \right]^{1/2} \quad B_\mu = 4 \times 10^{15} \text{ G}$$

- for the overtones,
 - for EOS NV ${}_2\alpha_n \approx 0.8 - 1.1$
 - for EOS DH ${}_2\alpha_n \approx 2 - 2.5$
- Deviation of the magnetized NS freqs. from those of the non-magnetized ones
 - $\lesssim 3.4\%$ for the EOS NV
 - $\lesssim 7.5\%$ for the EOS DH,
 if we assume $B \approx 10^{15} \text{ G}$



QPOs are newly found

Article

Very-high-frequency oscillations in the main peak of a magnetar giant flare

<https://doi.org/10.1038/s41586-021-04101-1>

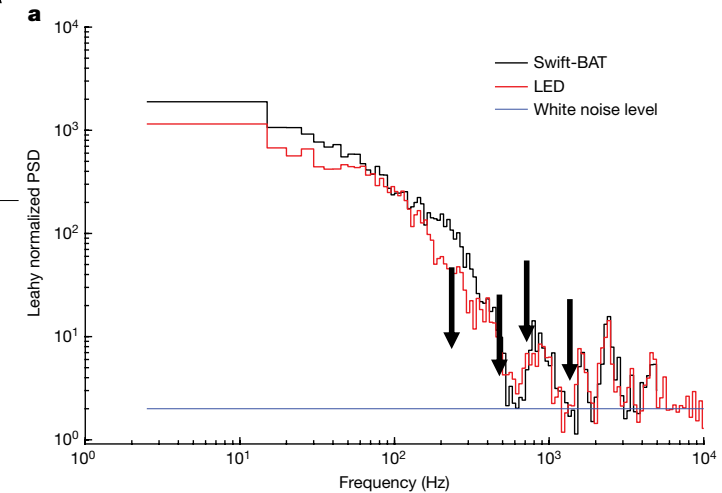
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 Check for updates

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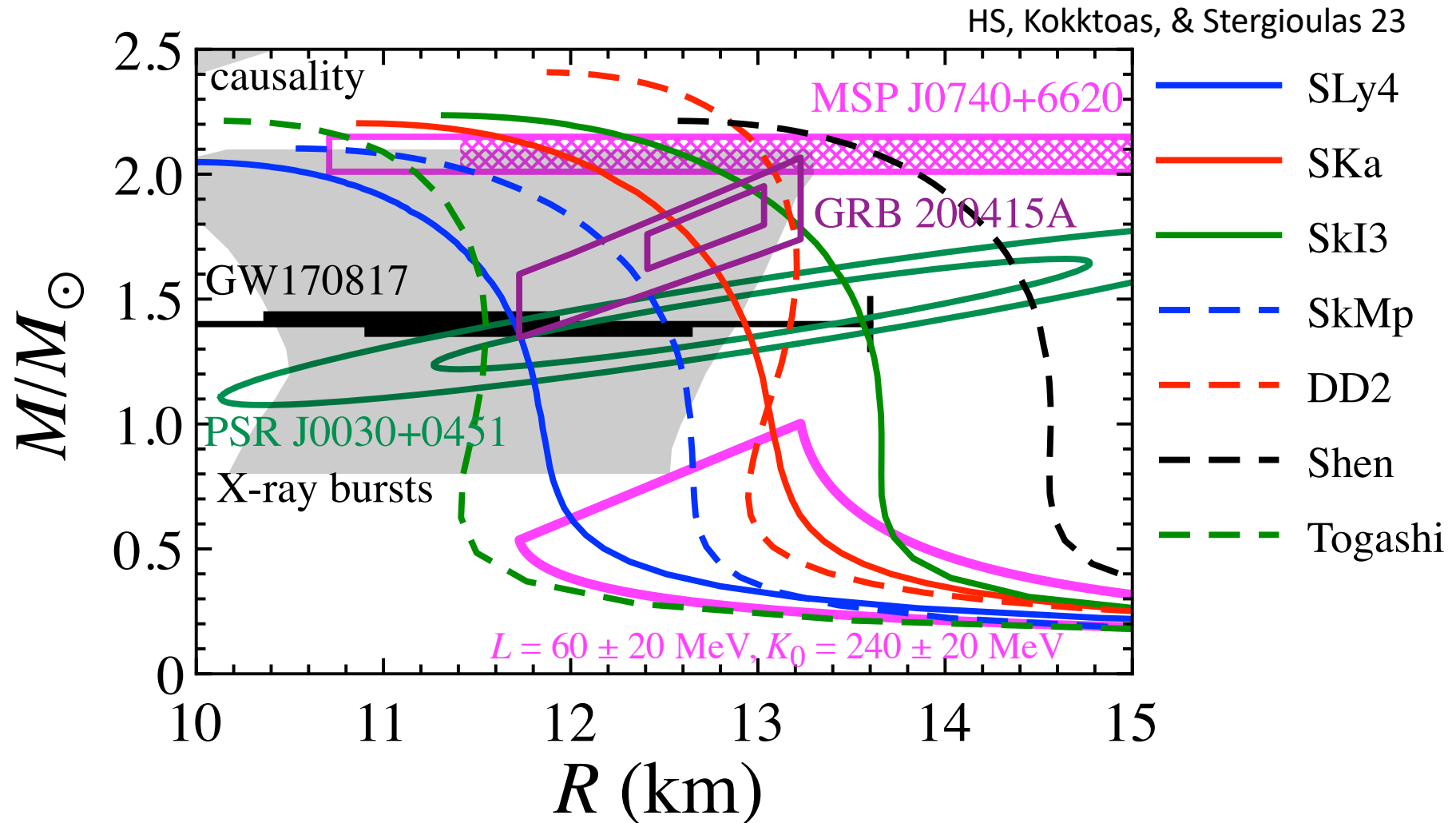


giant gamma-ray flare (GRB 200415A) in the direction of the NGC 253 galaxy, disappearing after 3.5 msec, on 15/4/2020.

Interval (Hz)	LED		HED	
	Peak Frequency (Hz)	Chance probability	Peak Frequency (Hz)	Chance probability
500 - 1100	835.9 ^{-84.7} _{+77.3}	1.2 x 10 ⁻⁴	-	-
1100 - 1700	1443.7 ^{-68.7} _{+74.8} ^a	4.9 x 10 ⁻²	1353.5 ^{-230.7} _{+217.7}	1.2 x 10 ⁻¹²
1800 - 2400	2131.7 ^{-151.0} _{+148.2}	2.4 x 10 ⁻⁹	2095.1 ^{-277.5} _{+180.8}	5.0 x 10 ⁻⁸
3900 - 4500	4249.7 ^{-102.7} _{+116.0}	1.7 x 10 ⁻⁴	4126.8 ^{-71.1} _{+73.0}	1.1 x 10 ⁻²

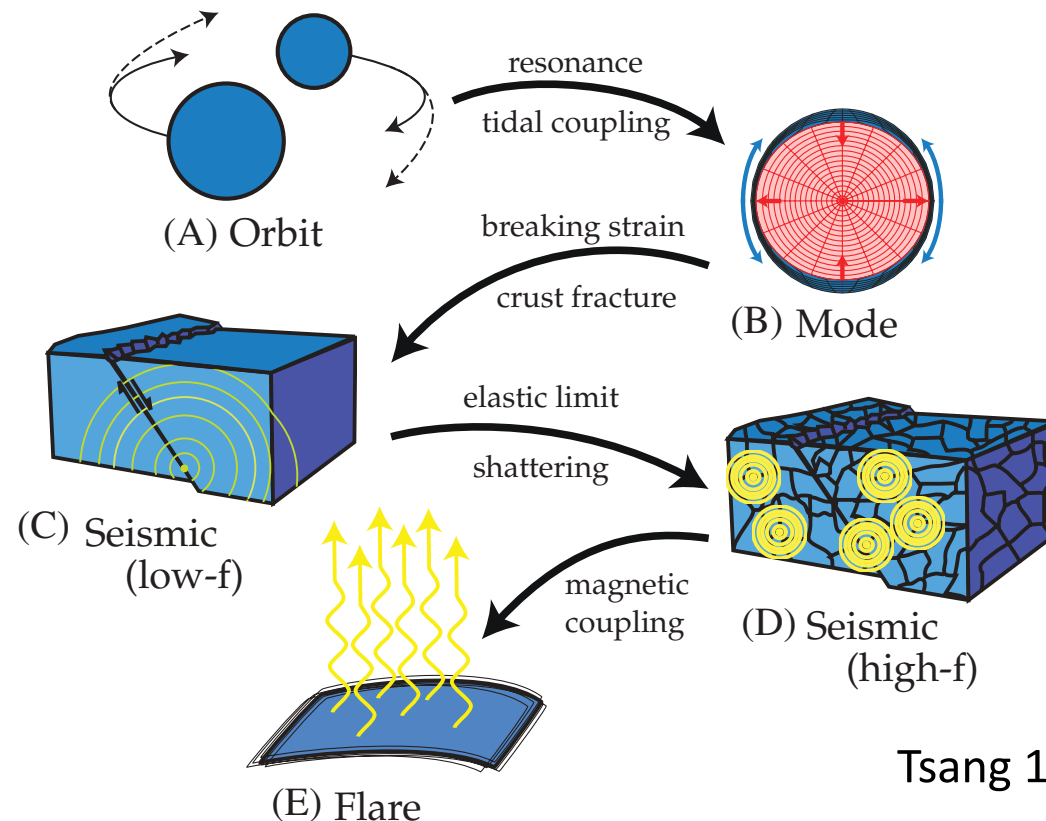
Observed fres. are high
- polar type oscillations, such as f, p_i-modes
- overtones of torsional modes

Constraints on M & R



- See in Session D08: Minisymposium: Solid State Physics in Neutron Stars: Crystallography and Superfluidity on Nov. 29th

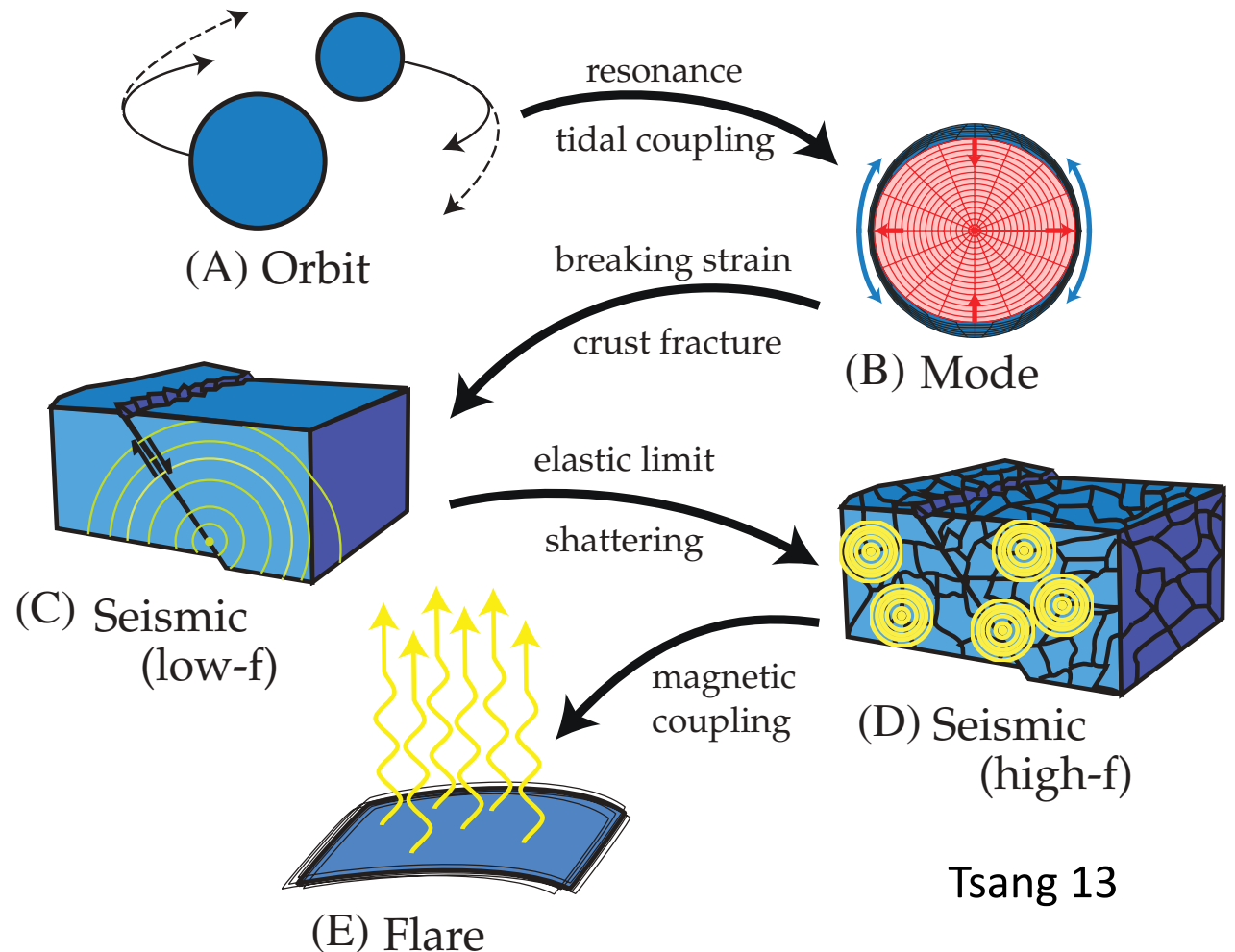
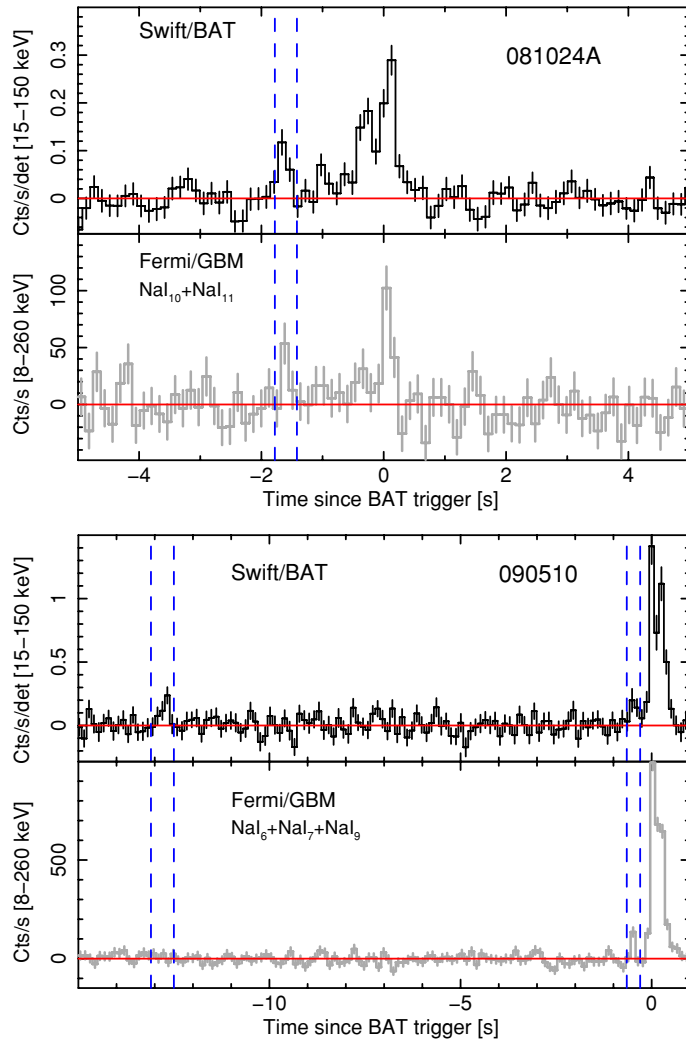
Resonant shattering and shear/interface modes



Tsang 13

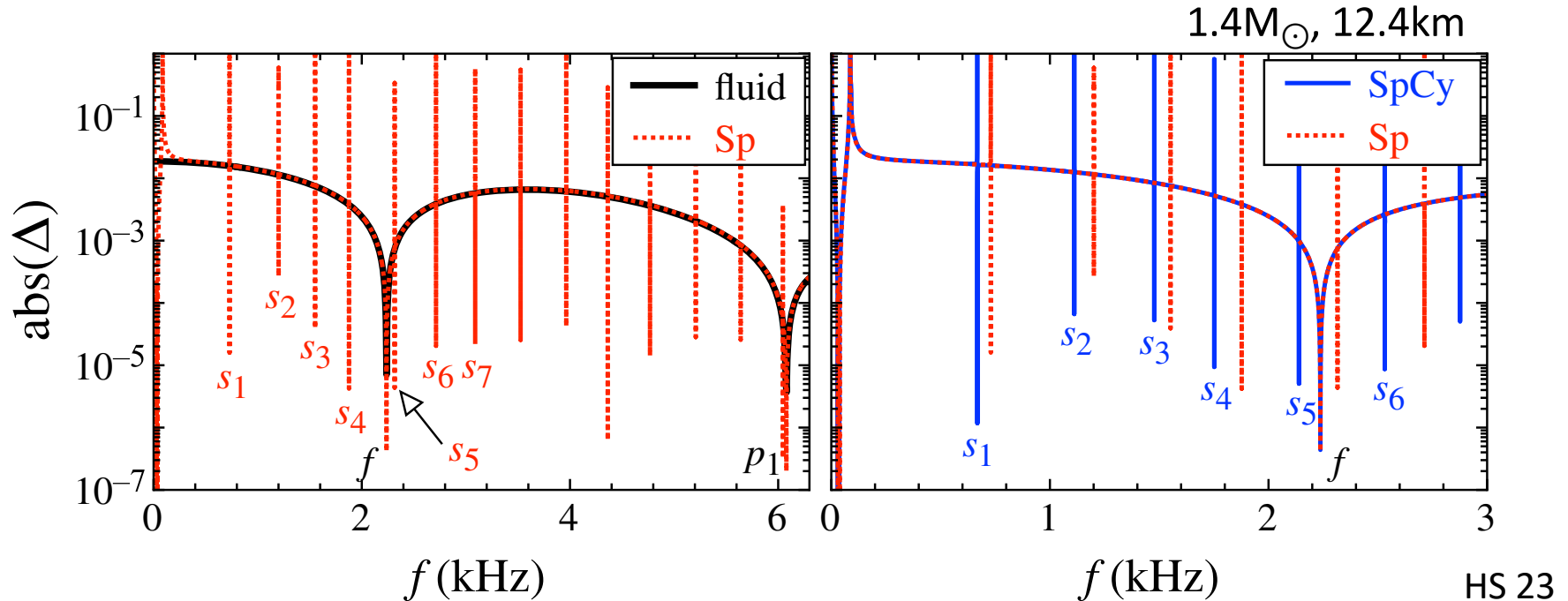
Resonant shattering

- Precursors 1–10 s prior to the main flare were detected with high significance for three SGRBs out of the 49 (Troja+10)



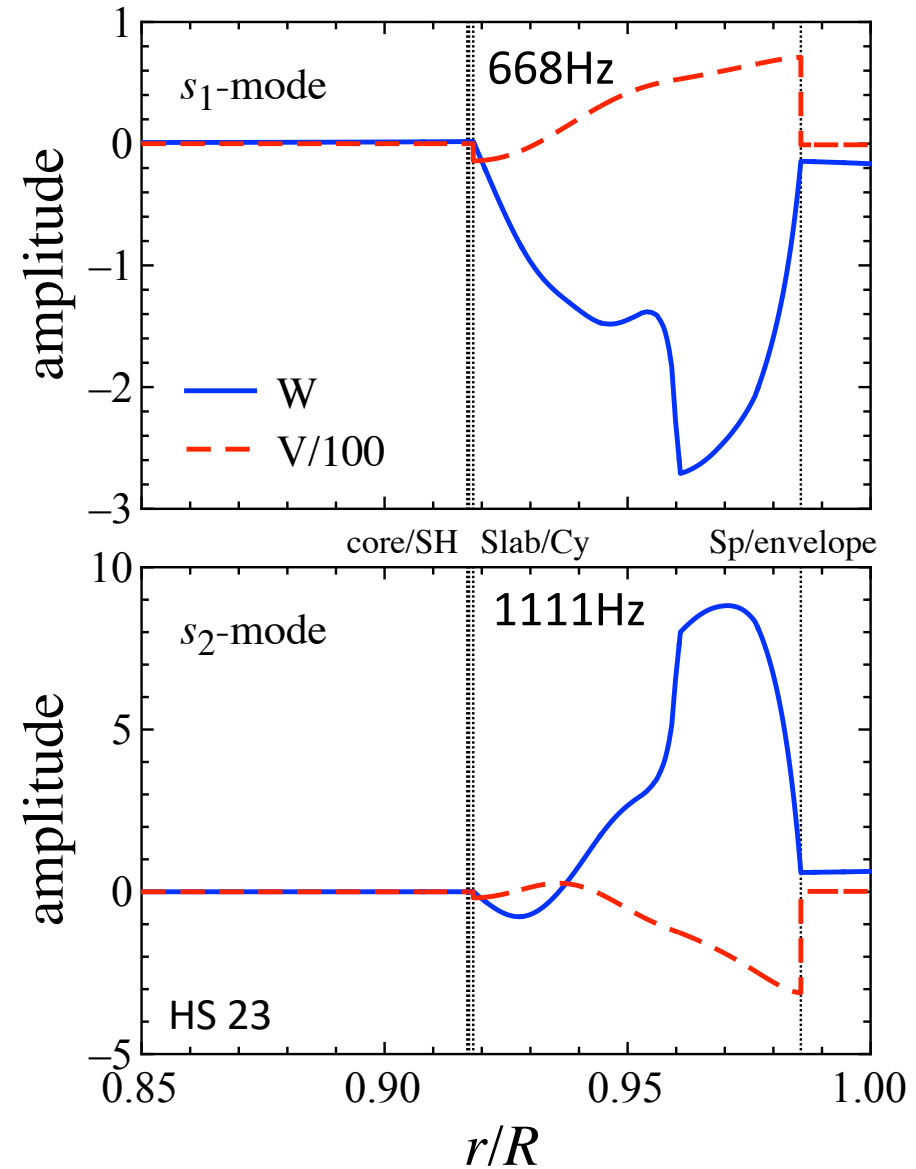
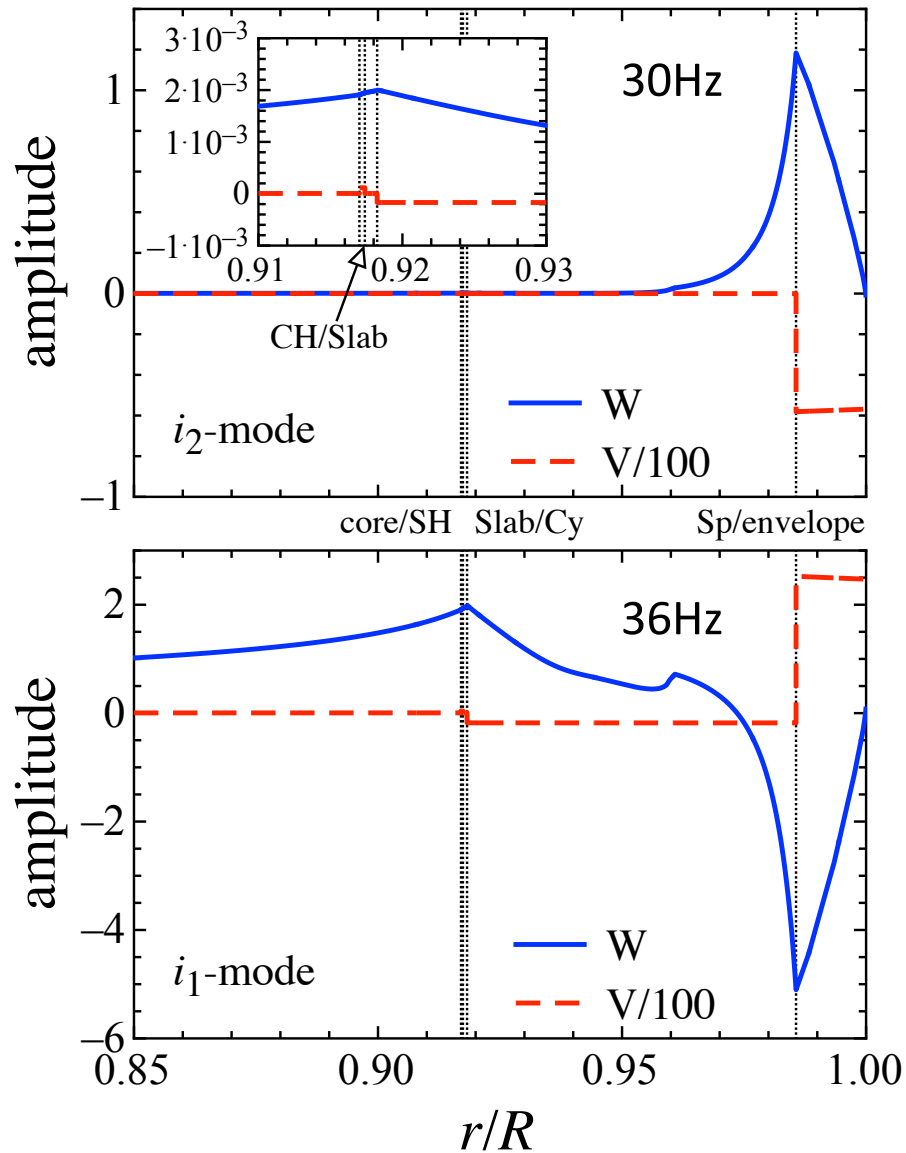
Tsang 13

Behavior of eigenfrequencies



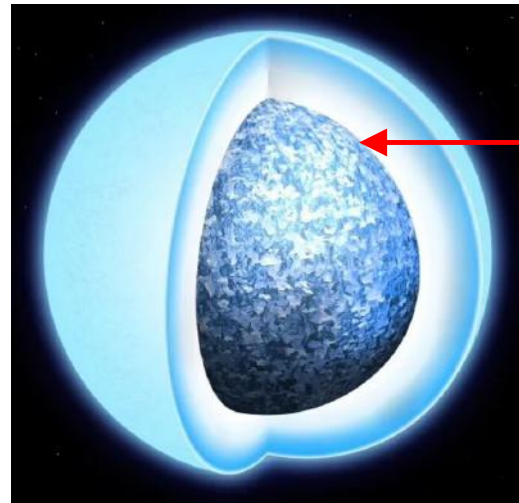
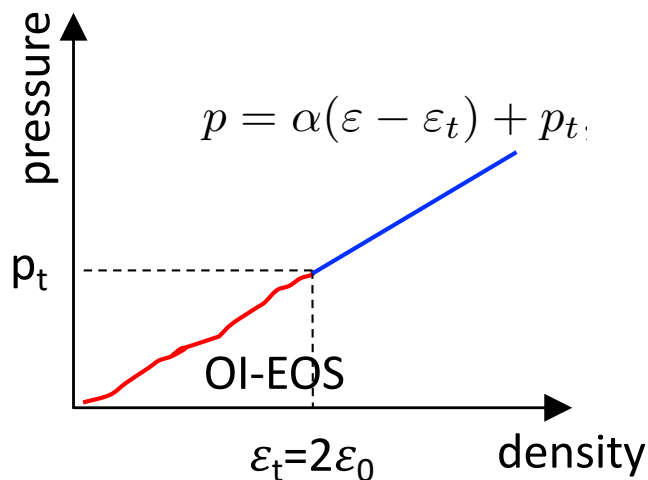
- Frequencies with $\Delta=0$ correspond to the eigenfrequencies
- f- and p_1 -mode freqs. hardly depend on the crust elasticity
- s_i -mode freqs. strongly depend on the density of interface(s)

Eigenfunctions (i/s-modes)



Uncertainties in core EOS

- To see the dependence on the EOS stiffness in a higher-density region, we adopt not only the original OI-EOSs but also the one-parameter EOS, such as
 - for a lower-density region ($\varepsilon \leq \varepsilon_t$): original OI-EOSs
 - for a higher-density region ($\varepsilon \geq \varepsilon_t$): $p = \alpha(\varepsilon - \varepsilon_t) + p_t$
- α is associated with the sound velocity as $c_s^2 = \alpha$
- we consider in the range of $1/3 \leq \alpha \leq 1$.

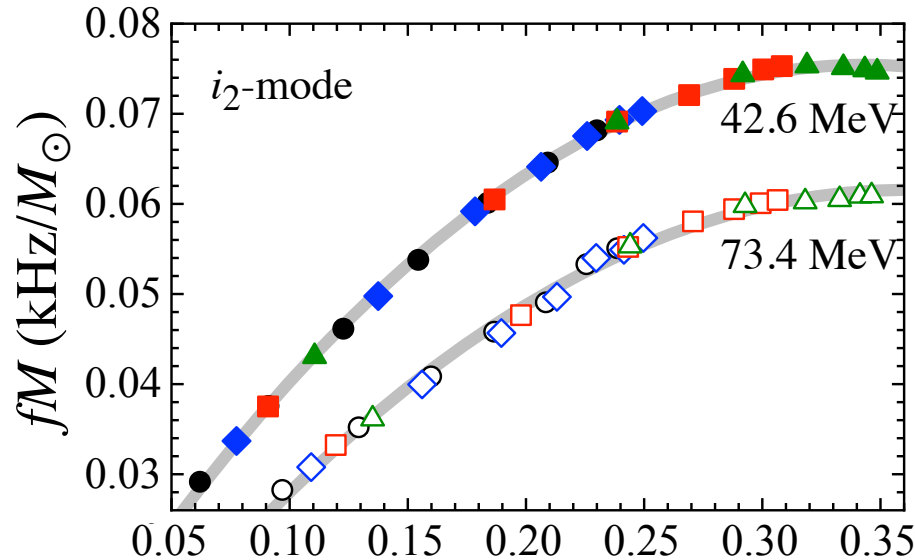
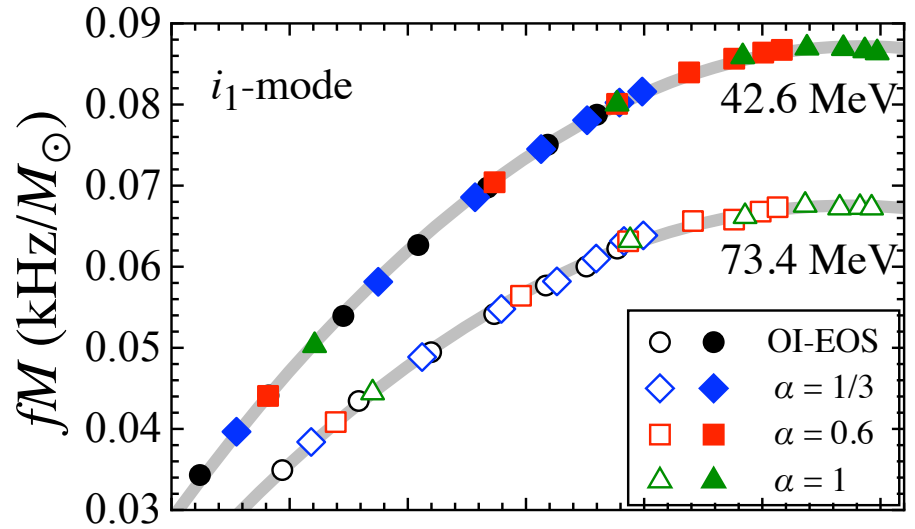


crust/core transition density
 $\simeq (0.3-0.5)n_0$

Empirical relation (i/s-modes)

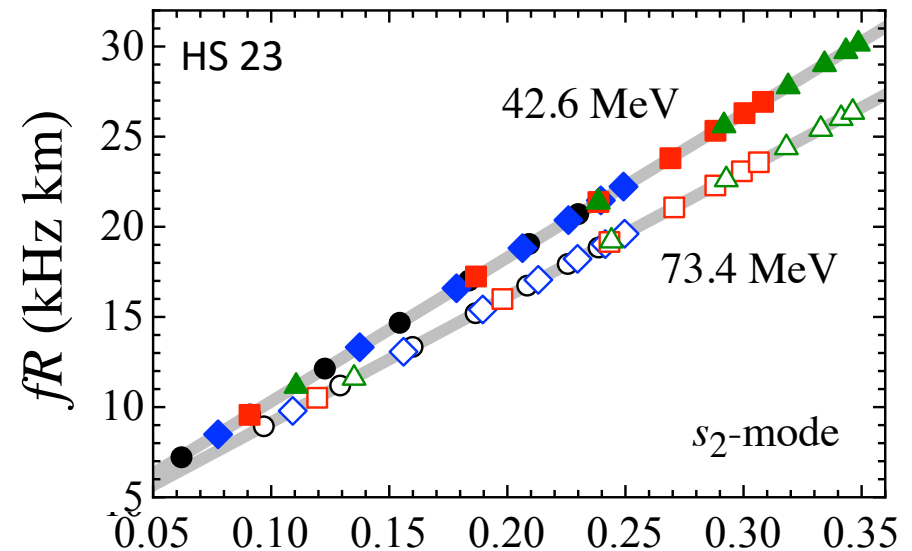
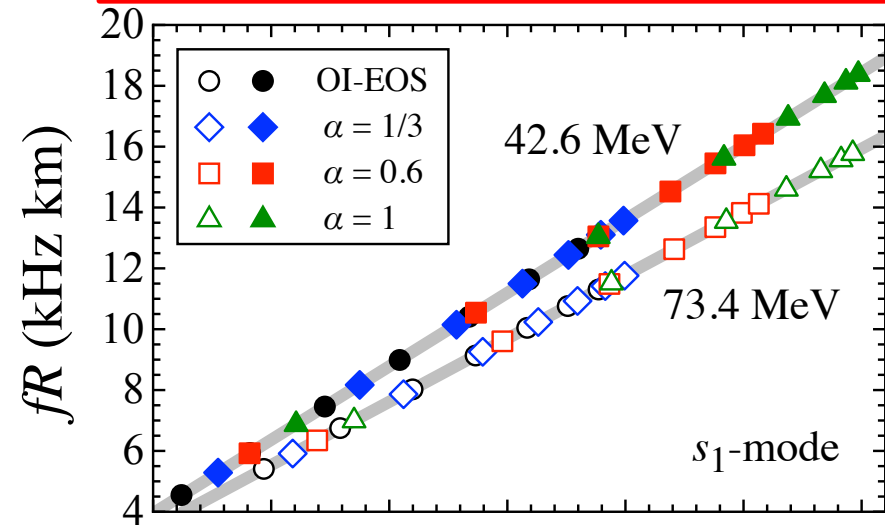
$x = M/R$

$$fM \text{ (kHz}/M_{\odot}) = a_0 + a_1(x/0.1) + a_2(x/0.1)^2$$



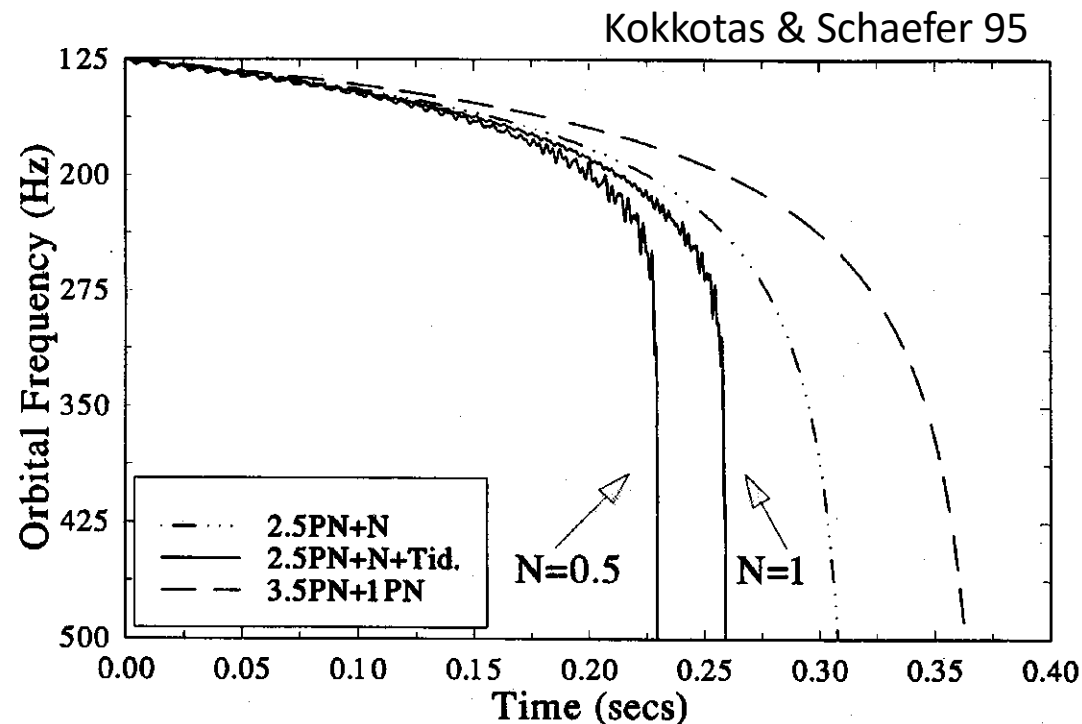
M/R

$$fR \text{ (kHz km)} = b_0 + b_1(x/0.1)$$



M/R

- we find two different types of fitting formulae for the i- and s-mode freqs.
 - depend only on the crust stiffness (crust EOS)
- If one would simultaneously observe the i- and s-modes, one might extract the stellar mass and radius with the help of the constraint on the crust stiffness from the terrestrial experiments.
- Moreover, it may affect the binary evolution



Conclusion

- Astero-seismology is a powerful technique for extracting the NS properties
- In this talk, we focus on
 - supernova gravitational waves
 - magnetar QPOs
 - resonant shuttering in binary NSs
- We are looking forward to getting new signals from NSs, which may help us to understand NS physics well by using the astero-seismology approach.